

A Theory of Optimal Capital Taxation

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Motivation: The Failure of Capital Tax Theory

- 1) Standard theory:** optimal tax rate $\tau_K=0\%$ for all forms of capital taxes (stock- or flow-based)
 - Complete suppression of inheritance tax, property tax, corporate tax, K income tax, etc. is desirable... including from the viewpoint of individuals with zero property!
- 2) Practice:** EU27: tax/GDP = 39%, capital tax/GDP = 9%
US: tax/GDP = 27%, capital tax/GDP = 8%
(inheritance tax: <1% GDP, but high top rates)
 - Nobody seems to believe this extreme zero-tax result – which indeed relies on very strong assumptions
- 3) Huge gap** between theory and practice on optimal capital taxation is a major failure of modern economics

This Paper: Two Ingredients

In this paper we attempt to develop a realistic, tractable K tax theory based upon two key ingredients

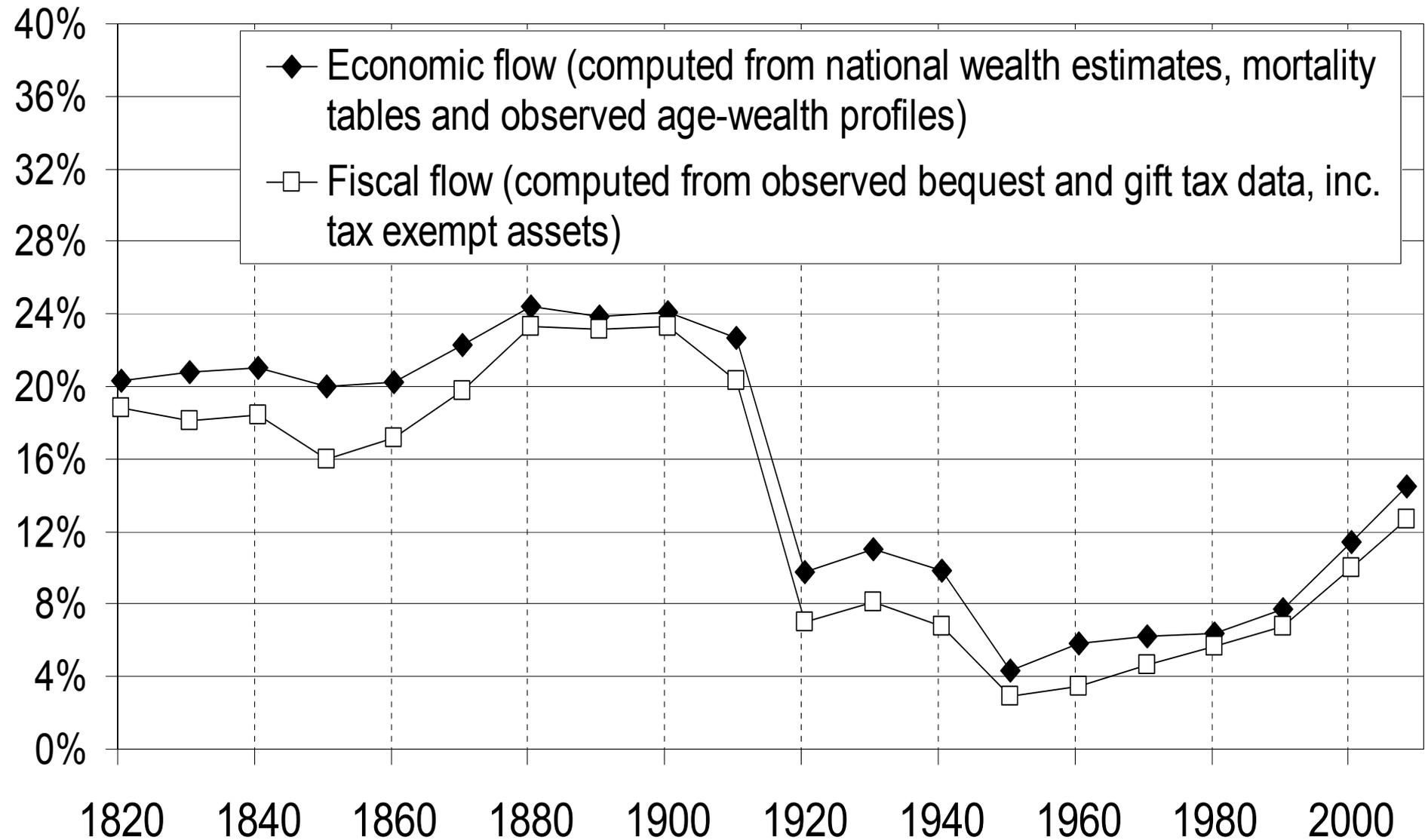
1) Inheritance: life is not infinite, inheritance is a large part of aggregate wealth accumulation

2) Imperfect K markets: with uninsurable return risk, use lifetime K tax to implement optimal inheritance tax

With no inheritance (100% life-cycle wealth or infinite life) **and** perfect K markets, then the case for $\tau_K=0\%$ is indeed very strong: $1+r$ = relative price of present consumption
→ do not tax r , instead use redistributive labor income taxation τ_L only (Atkinson-Stiglitz)

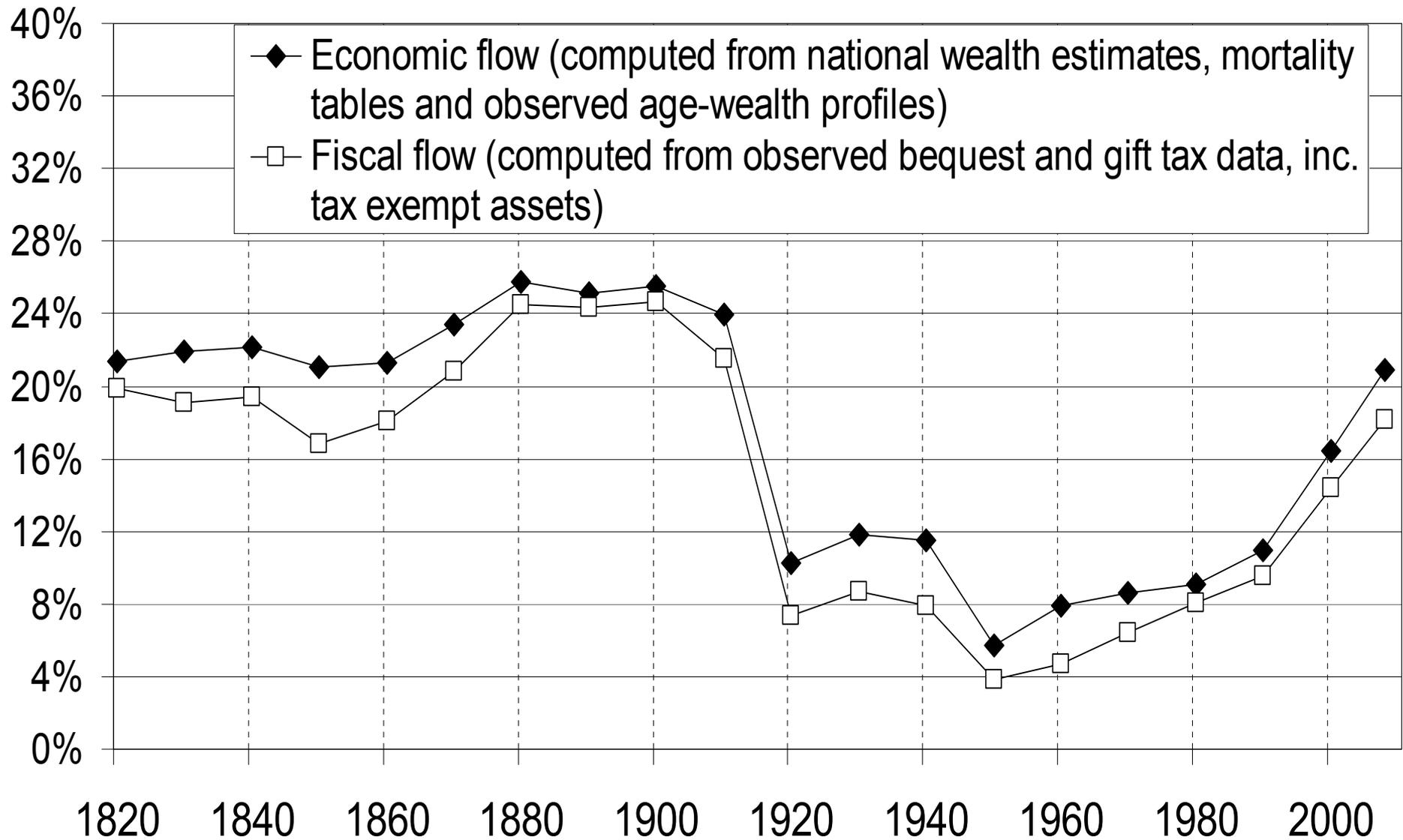
- **Key parameter: $b_y = B/Y$**
= aggregate annual bequest flow B /national income Y
 - Huge historical variations:
 $b_y = 20\text{-}25\%$ in 19^C & until WW1 (=very large: rentier society)
 $b_y < 5\%$ in 1950-60 (Modigliani lifecycle) (~A-S)
 b_y back up to ~15% by 2010 → inheritance matters again
 - See « On the Long-Run Evolution of Inheritance – France 1820-2050 », Piketty QJE'11
 - **$r > g$ story:** g small & $r \gg g$ → inherited wealth is capitalized faster than growth → b_y high
 - U-shaped pattern probably less pronounced in US
- **Optimal τ_B is increasing with b_y (or $r-g$)**

Annual inheritance flow as a fraction of national income, France 1820-2008



Source: T. Piketty, "On the long-run evolution of inheritance", QJE 2011

Annual inheritance flow as a fraction of disposable income, France 1820-2008



Source: T. Piketty, "On the long-run evolution of inheritance", QJE 2011

Result 1: Optimal Inheritance Tax Formula

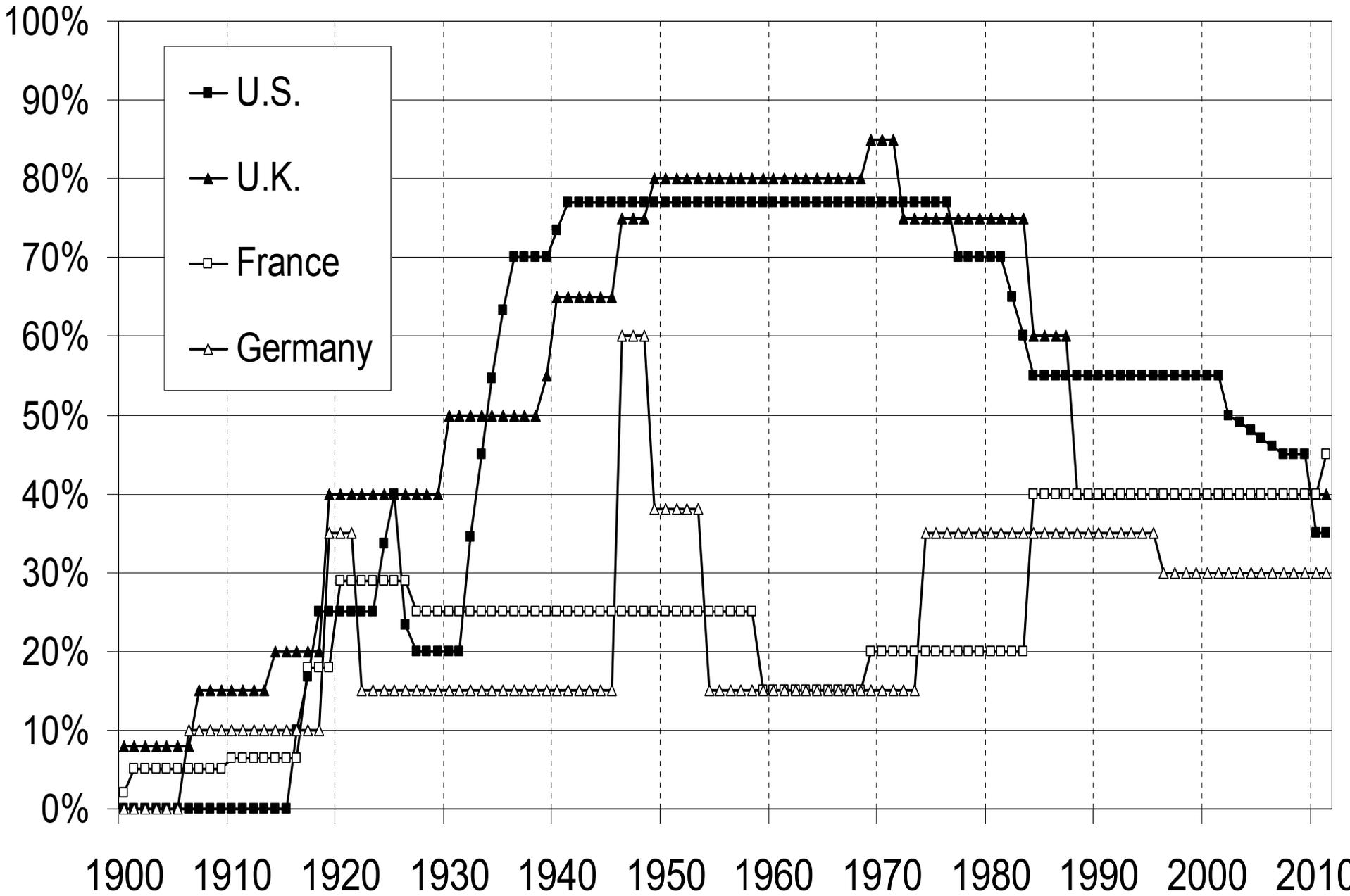
- **Simple formula** for optimal bequest tax rate expressed in terms of estimable parameters:

$$\tau_B = \frac{1 - (1 - \alpha - \tau) s_{b0} / b_y}{1 + e_B + s_{b0}}$$

with: b_y = bequest flow, e_B = elasticity, s_{b0} = bequest taste
→ τ_B increases with b_y and decreases with e_B and s_{b0}

- For realistic parameters: $\tau_B = 50\text{-}60\%$ (or more..or less...)
→ **our theory can account for the variety of observed top bequest tax rates (30%-80%)**
→ hopefully our approach can contribute to a tax debate based more upon empirical estimates of key distributional & behavioral parameters (and less about abstract theory)

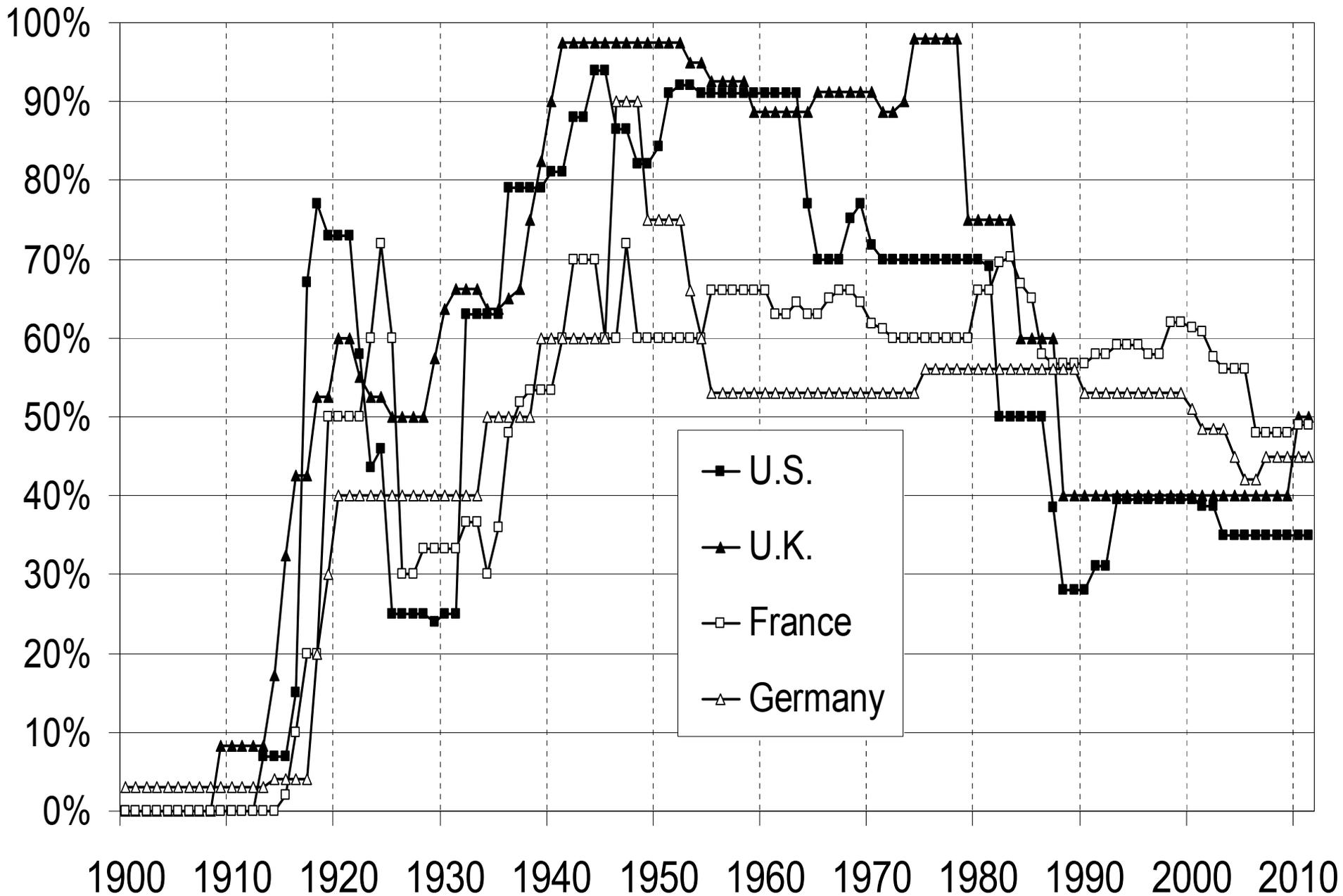
Top Inheritance Tax Rates 1900-2011



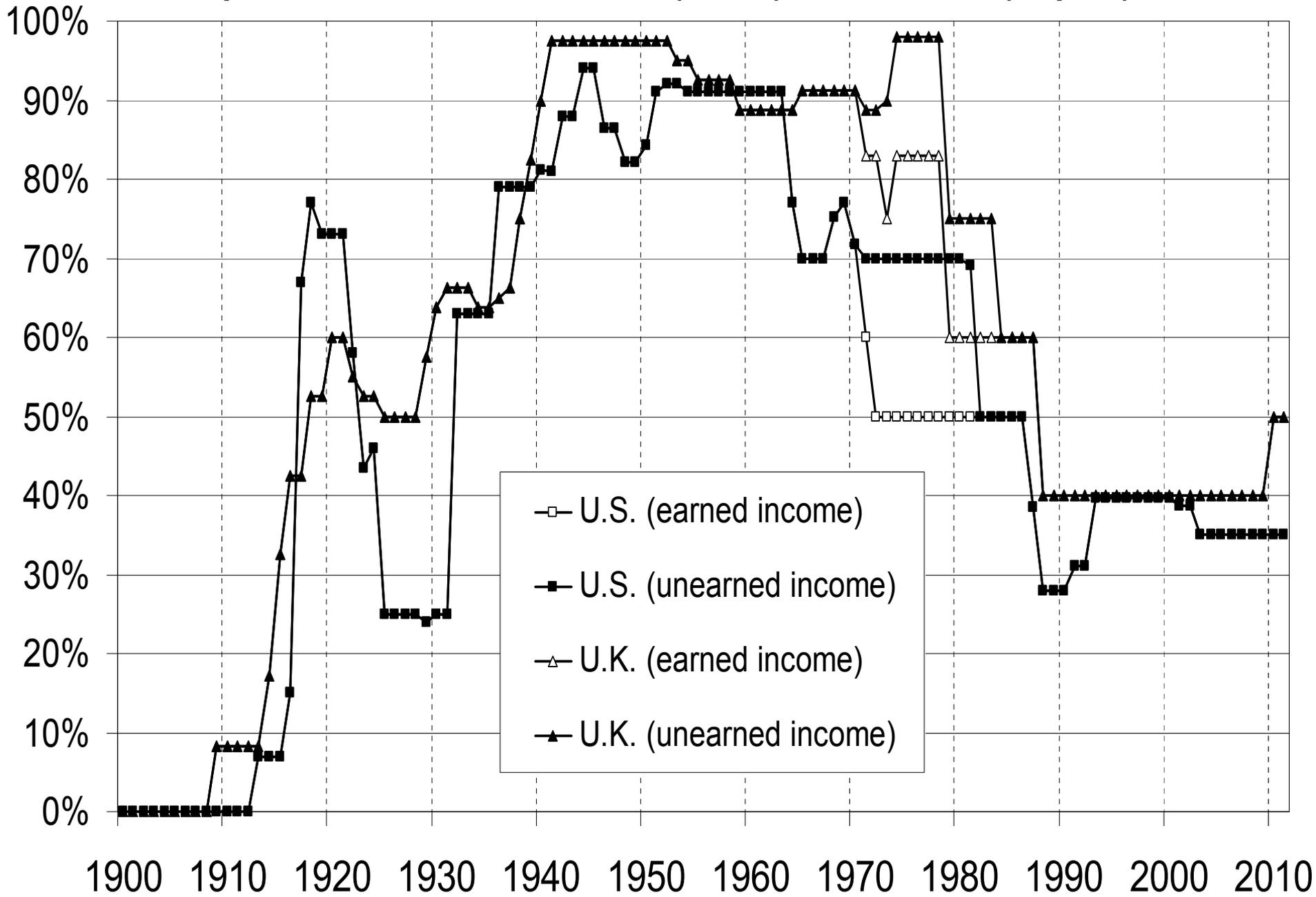
Result 2: Optimal Capital Tax Mix

- **K market imperfections** (e.g. uninsurable idiosyncratic shocks to rates of return) can justify shifting one-off inheritance taxation toward lifetime capital taxation (property tax, K income tax,..)
 - **Intuition:** what matters is capitalized bequest, not raw bequest; but at the time of setting the bequest tax rate, there is a lot of uncertainty about what the rate of return is going to be during the next 30 years → so it is more efficient to split the tax burden
- **our theory can explain the actual structure & mix of inheritance vs lifetime capital taxation**
(& why high top inheritance and top capital income tax rates often come together, e.g. US-UK 1930s-1980s)

Top Income Tax Rates 1900-2011



Top Income Tax Rates: Earned (Labor) vs Unearned (Capital)



Link with previous work

1. **Atkinson-Stiglitz JPupE'76**: No capital tax in life-cycle model with homogenous tastes for savings, consumption-leisure separability and nonlinear labor income tax
2. **Chamley EMA'86-Judd JPubE'85**: No capital tax in the long run in an infinite horizon model with homogenous discount rate
3. **Precautionary Savings**: Capital tax desirable when uncertainty about future earnings ability affect savings decisions
4. **Credit Constraints** can restore desirability of capital tax to redistribute from the unconstrained to the constrained
5. **Time Inconsistent Governments** always want to tax existing capital → here we focus on long-run optima with full commitment (most difficult case for $\tau_K > 0$)

Atkinson-Stiglitz fails with inheritances

A-S applies when sole source of lifetime income is labor:

$$c_1 + c_2 / (1+r) = \theta l - T(\theta l) \quad (\theta = \text{productivity}, l = \text{labor supply})$$

Bequests provide an additional source of life-income:

$$c + b(\text{left}) / (1+r) = \theta l - T(\theta l) + b(\text{received})$$

→ conditional on θl , high $b(\text{left})$ is a signal of high $b(\text{received})$ [and hence low u_c] → “commodity” $b(\text{left})$ should be taxed even with optimal $T(\theta l)$

→ **two-dimensional heterogeneity requires two-dim. tax policy tool**

Extreme example: no heterogeneity in productivity θ but pure heterogeneity in bequests motives → bequest taxation is desirable for redistribution

Note: bequests generate positive externality on donors and hence should be taxed less (but still >0)

Chamley-Judd fails with finite lives

C-J in the dynastic model implies that inheritance tax rate τ_K should be zero in the long-run

- (1) If social welfare is measured by the discounted utility of first generation then $\tau_K=0$ because inheritance tax creates an infinitely growing distortion but...
this is a crazy social welfare criterion that does not make sense when each period is a generation
- (2) If social welfare is measured by long-run steady state utility then $\tau_K=0$ because supply elasticity e_B of bequest wrt to price is infinite but...
we want a theory where e_B is a free parameter

A Good Theory of Optimal Capital Taxation

Should follow the optimal labor income tax progress and hence needs to capture key trade-offs robustly:

- 1) **Welfare effects:** people dislike taxes on bequests they leave, or inheritances they receive, but people also dislike labor taxes → interesting trade-off
- 2) **Behavioral responses:** taxes on bequests might (a) discourage wealth accumulation, (b) affect labor supply of inheritors (Carnegie effect) or donors
- 3) **Results should be robust** to heterogeneity in tastes and motives for bequests within the population and formulas should be expressed in terms of estimable “**sufficient statistics**”

Part 1: Optimal Inheritance Taxation

- Agent i in cohort t (1 cohort = 1 period = H years, $H \approx 30$)
- Receives bequest $b_{ti} = z_i b_t$ at beginning of period t
- Works during period t
- Receives labor income $y_{Lti} = \theta_i y_{Lt}$ at end of period t
- Consumes c_{ti} & leaves bequest b_{t+1i} so as to maximize:

$$\begin{aligned} & \text{Max } V_i(c_{ti}, b_{t+1i}, \underline{b}_{t+1i}) \\ \text{s.c. } & c_{ti} + b_{t+1i} \leq (1 - \tau_B) b_{ti} e^{rH} + (1 - \tau_L) y_{Lti} \end{aligned}$$

With: b_{t+1i} = end-of-life wealth (wealth loving)

$\underline{b}_{t+1i} = (1 - \tau_B) b_{t+1i} e^{rH}$ = net-of-tax capitalized bequest left
(bequest loving)

τ_B = bequest tax rate, τ_L = labor income tax rate

$V_i(\cdot)$ homogeneous of degree one (to allow for growth)

- **Special case: Cobb-Douglas preferences:**

$$V_i(c_{ti}, b_{t+1i}, \underline{b}_{t+1i}) = c_{ti}^{1-s_i} b_{t+1i}^{s_{wi}} \underline{b}_{t+1i}^{s_{bi}} \quad (\text{with } s_i = s_{wi} + s_{bi} \text{)}$$

$$\rightarrow b_{t+1i} = s_i [(1-\tau_B)z_i b_t e^{rH} + (1-\tau_L)\theta_i y_{Lt}] = s_i \underline{y}_{ti}$$

- **General preferences: $V_i()$ homogenous of degree one:**

$$\text{Max } V_i() \rightarrow \text{FOC } V_{ci} = V_{wi} + (1-\tau_B)e^{rH} V_{bi}$$

All choices are linear in total life-time income \underline{y}_{ti}

$$\rightarrow b_{t+1i} = s_i \underline{y}_{ti}$$

$$\text{Define } s_{bi} = s_i (1-\tau_B)e^{rH} V_{bi}/V_{ci}$$

Same as Cobb-Douglas but s_i and s_{bi} now depend on $1-\tau_B$
(income and substitution effects no longer offset each other)

- We allow for any distribution and any ergodic random process for taste shocks s_i and productivity shocks θ_i
- **endogenous dynamics of the joint distribution $\Psi_t(z, \theta)$ of normalized inheritance z and productivity θ**

- **Macro side:** open economy with exogenous return r , domestic output $Y_t = K_t^\alpha L_t^{1-\alpha}$, with $L_t = L_0 e^{gHt}$ and g =exogenous productivity growth rate
(inelastic labor supply $l_{ti}=1$, fixed population size = 1)

- **Period by period government budget constraint:**

$$\tau_L Y_{Lt} + \tau_B B_t e^{rH} = \tau Y_t$$

$$\text{i.e. } \tau_L (1-\alpha) + \tau_B b_{yt} = \tau$$

With τ = exogenous tax revenue requirement (e.g. $\tau=30\%$)

$b_{yt} = e^{rH} B_t / Y_t$ = capitalized inheritance-output ratio

- **Government objective:**

We take $\tau \geq 0$ as given and solve for the optimal tax mix τ_L, τ_B

maximizing steady-state SWF = $\int \omega_{z\theta} V_{z\theta} d\Psi(z, \theta)$

with $\Psi(z, \theta)$ = steady-state distribution of z and θ

$\omega_{z\theta}$ = social welfare weights

Equivalence between τ_B and τ_K

- In basic model, tax τ_B on inheritance is equivalent to tax τ_K on annual return r to capital as:

$$\underline{b}_{tj} = (1 - \tau_B)b_{tj}e^{rH} = b_{tj}e^{(1-\tau_K)rH}, \text{ i.e. } \tau_K = -\log(1-\tau_B)/rH$$

- E.g. with $r=5\%$ and $H=30$, $\tau_B=25\% \leftrightarrow \tau_K=19\%$,
 $\tau_B=50\% \leftrightarrow \tau_K=46\%$, $\tau_B=75\% \leftrightarrow \tau_K=92\%$
- This equivalence no longer holds with
(a) tax enforcement constraints, or **(b)** life-cycle savings,
or **(c)** uninsurable risk in $r=r_{tj}$
→ Optimal mix τ_B, τ_K then becomes an interesting
question (see below)

- **Special case:** taste and productivity shocks s_i and θ_i are i.e. across and within periods (no memory)

→ $s = E(s_i | \theta_i, z_i)$ → simple aggregate transition equation:

$$b_{t+1i} = s_i [(1 - \tau_B)z_i b_t e^{rH} + (1 - \tau_L)\theta_i y_{Lt}]$$

$$\rightarrow b_{t+1} = s [(1 - \tau_B)b_t e^{rH} + (1 - \tau_L)y_{Lt}]$$

Steady-state convergence: $b_{t+1} = b_t e^{gH}$

$$\rightarrow b_{yt} \rightarrow b_y = \frac{s(1 - \tau - \alpha)e^{(r-g)H}}{1 - se^{(r-g)H}}$$

- b_y increases with $r-g$ (capitalization effect, Piketty QJE'11)
- If $r-g=3\%$, $\tau=10\%$, $H=30$, $\alpha=30\%$, $s=10\%$ → $b_y=20\%$
- If $r-g=1\%$, $\tau=30\%$, $H=30$, $\alpha=30\%$, $s=10\%$ → $b_y=6\%$

- **General case:** under adequate ergodicity assumptions for random processes s_i and θ_i :

Proposition 1 (unique steady-state): for given τ_B, τ_L , then as $t \rightarrow +\infty$, $b_{yt} \rightarrow b_y$ and $\Psi_t(z, \theta) \rightarrow \Psi(z, \theta)$

- Define:
$$e_B = \frac{db_y}{d(1-\tau_B)} \frac{1-\tau_B}{b_y}$$
 - e_B = elasticity of steady-state bequest flow with respect to net-of-bequest-tax rate $1-\tau_B$
 - With $V_i(\cdot)$ = Cobb-Douglas and i.i.d. shocks, $e_B = 0$
 - For general preferences and shocks, $e_B > 0$ (or < 0)
- we take e_B as a free parameter

- Meritocratic rawlsian optimum, i.e. social optimum from the viewpoint of zero bequest receivers ($z=0$):

Proposition 2 (zero-receivers tax optimum)

$$\tau_B = \frac{1 - (1 - \alpha - \tau) s_{b0} / b_y}{1 + e_B + s_{b0}}$$

with: s_{b0} = average bequest taste of zero receivers

- τ_B increases with b_y and decreases with e_B and s_{b0}
- If bequest taste $s_{b0}=0$, then $\tau_B = 1/(1+e_B)$
→ standard revenue-maximizing formula
- If $e_B \rightarrow +\infty$, then $\tau_B \rightarrow 0$: back to Chamley-Judd
- If $e_B=0$, then $\tau_B < 1$ as long as $s_{b0} > 0$
- I.e. zero receivers do not want to tax bequests at 100%, because they themselves want to leave bequests
→ **trade-off between taxing rich successors from my cohort vs taxing my own children**

Example 1: $\tau=30\%$, $\alpha=30\%$, $s_{b0}=10\%$, $e_B=0$

- If $b_y=20\%$, then $\tau_B=73\%$ & $\tau_L=22\%$
- If $b_y=15\%$, then $\tau_B=67\%$ & $\tau_L=29\%$
- If $b_y=10\%$, then $\tau_B=55\%$ & $\tau_L=35\%$
- If $b_y=5\%$, then $\tau_B=18\%$ & $\tau_L=42\%$

→ with high bequest flow b_y , zero receivers want to tax inherited wealth at a higher rate than labor income (73% vs 22%); with low bequest flow they want the opposite (18% vs 42%)

Intuition: with low b_y (high g), not much to gain from taxing bequests, and this is bad for my own children

With high b_y (low g), it's the opposite: it's worth taxing bequests, so as to reduce labor taxation and allow zero receivers to leave a bequest

Example 2: $\tau=30\%$, $\alpha=30\%$, $s_{b0}=10\%$, $b_y=15\%$

- If $e_B=0$, then $\tau_B=67\%$ & $\tau_L=29\%$
- If $e_B=0.2$, then $\tau_B=56\%$ & $\tau_L=31\%$
- If $e_B=0.5$, then $\tau_B=46\%$ & $\tau_L=33\%$
- If $e_B=1$, then $\tau_B=35\%$ & $\tau_L=35\%$

→ behavioral responses matter but not hugely as long as the elasticity e_B is reasonable

Kopczuk-Slemrod 2001: $e_B=0.2$ (US)

(French experiments with zero-children savers: $e_B=0.1-0.2$)

- **Proposition 3** (z%-bequest-receivers optimum):

$$\tau_B = \frac{1 - (1 - \alpha - \tau) s_{b_z} / b_y - (1 + e_B + s_{b_z}) z / \theta_z}{(1 + e_B + s_{b_z}) (1 - z / \theta_z)}$$

- If z large, $\tau_B < 0$: top successors want bequest subsidies
 - But since the distribution of inheritance is highly concentrated (bottom 50% successors receive ~5% of aggregate flow), the bottom-50%-receivers optimum turns out to be very close to the zero-receivers optimum
 - Perceptions about wealth inequality & mobility matter a lot: if bottom receivers expect to leave large bequests, then they may prefer low bequest tax rates
- it is critical to estimate the right distributional parameters

- **Proposition 7** (optimum with elastic labor supply):

$$\tau_B = \frac{1 - (1 - \alpha - \tau \cdot (1 + e_L)) s_{b0} / b_y}{1 + e_B + s_{b0} \cdot (1 + e_L)}$$

- Race between two elasticities: e_B vs e_L
- τ_B decreases with e_B but increases with e_L

Example : $\tau=30\%$, $\alpha=30\%$, $s_{b0}=10\%$, $b_y=15\%$

- If $e_B=0$ & $e_L=0$, then $\tau_B=67\%$ & $\tau_L=29\%$
- If $e_B=0.2$ & $e_L=0$, then $\tau_B=56\%$ & $\tau_L=31\%$
- If $e_B=0.2$ & $e_L=0.2$, then $\tau_B=59\%$ & $\tau_L=30\%$
- If $e_B=0.2$ & $e_L=1$, then $\tau_B=67\%$ & $\tau_L=29\%$

Other extensions

- **Optimal non-linear bequest tax:** simple formula for top rate; numerical solutions for full schedule
- **Closed economy:** $F_K = R = e^{rH} - 1 =$ generational return
 - optimal tax formulas continue to apply as in open economy with e_B, e_L being the pure supply elasticities
- **Lifecycle saving:** assume agents consume between age A and D , and have a kid at age H . E.g. $A=20, D=80, H=30$, so that everybody inherits at age $I=D-H=50$.
 - Max $V(U, b, b)$ with $U = [\int_{A \leq a \leq D} e^{-\delta a} c_a^{1-\gamma}]^{1/(1-\gamma)}$
 - same b_y and τ_B formulas as before, except for a factor λ correcting for when inheritances are received relative to labor income: $\lambda \approx 1$ if inheritance received around mid-life
(early inheritance: $b_y, \tau_B \uparrow$; late inheritance: $b_y, \tau_B \downarrow$)

Part 2: From inheritance tax to lifetime K tax

- One-period model, perfect K markets: equivalence btw bequest tax and lifetime K tax as $(1 - \tau_B)e^{rH} = e^{(1-\tau_K)rH}$
- Life-cycle savings, perfect K markets: it's always better to have a big tax τ_B on bequest, and zero lifetime capital tax τ_K , so as to avoid intertemporal consumption distortion
- However in the real world most people seem to prefer paying a property tax $\tau_K=1\%$ during 30 years rather than a big bequest tax $\tau_B=30\%$
- Total K taxes = 9% GDP, but bequest tax <1% GDP
- **In our view, the observed collective choice in favour of lifetime K taxes is a rational consequence of K markets imperfections, not of tax illusion**

Simplest imperfection: fuzzy frontier between capital income and labor income flows, can be manipulated by taxpayers (self-employed, top executives, etc.) (= tax enforcement problem)

Proposition 4: With fully fuzzy frontier, then $\tau_K = \tau_L$ (capital income tax rate = labor income tax rate), and bequest tax $\tau_B > 0$ is optimal iff bequest flow b_y sufficiently large

Define $\underline{\tau}_B = \tau_B + (1 - \tau_B)\tau_K R / (1 + R)$, with $R = e^{rH} - 1$.

$\tau_K = \tau_L \rightarrow$ adjust τ_B down to keep $\underline{\tau}_B$ the same as before

**\rightarrow comprehensive income tax + bequest tax
= what we observe in many countries**

Uninsurable uncertainty about future rate of return:

what matters is $b_{ti}e^{r_{ti}H}$, not b_{ti} ; but at the time of setting the bequest tax rate τ_B , nobody knows what the rate of return $1+R_{ti}=e^{r_{ti}H}$ is going to be during the next 30 or 40 years...

(idiosyncratic + aggregate uncertainty)

→ **with uninsurable shocks on returns r_{ti} , it's more efficient to split the tax burden between one-off transfer taxes and lifetime capital taxes**

Exemple: when you inherit a Paris apartment worth 100 000€ in 1972, nobody knows what the total cumulated return will be btw 1972 & 2012; so it's better to charge a moderate bequest tax and a larger annual tax on property values & flow returns

- Assume rate of return $R_{ti} = \varepsilon_{ti} + \xi e_{ti}$

With: ε_{ti} = i.i.d. random shock with mean R_0

e_{ti} = effort put into portfolio management (how much time one spends checking stock prices, looking for new investment opportunities, monitoring one's financial intermediary, etc.)

$c(e_{ti})$ = convex effort cost proportional to portfolio size

- **Define e_R = elasticity of aggregate rate of return R with respect to net-of-capital-income-tax rate $1-\tau_K$**
- If returns mostly random (effort parameter small as compared to random shock), then $e_R \approx 0$
- Conversely if effort matters a lot, then e_R large

- **Proposition 5.** Depending on parameters, optimal capital income tax rate τ_K can be $>$ or $<$ than optimal labor income tax rate τ_L ; if e_R small enough and/or b_y large enough, then $\tau_K > \tau_L$

(=what we observe in UK & US during the 1970s)

Example : $\tau=30\%$, $\alpha=30\%$, $s_{bo}=10\%$, $b_y=15\%$, $e_B=e_L=0$

- If $e_R=0$, then $\tau_K=100\%$, $\tau_B=9\%$ & $\tau_L=34\%$
- If $e_R=0.1$, then $\tau_K=78\%$, $\tau_B=35\%$ & $\tau_L=35\%$
- If $e_R=0.3$, then $\tau_K=40\%$, $\tau_B=53\%$ & $\tau_L=36\%$
- If $e_R=0.5$, then $\tau_K=17\%$, $\tau_B=56\%$ & $\tau_L=37\%$
- If $e_R=1$, then $\tau_K=0\%$, $\tau_B=58\%$ & $\tau_L=38\%$

Govt Debt and Capital Accumulation

- So far we imposed period-by-period govt budget constraint: no accumulation of govt debt or assets allowed
- In closed-economy, optimum capital stock should be given by modified Golden rule: $F_K = r^* = \delta + \Gamma g$
 - with δ = govt discount rate, Γ = curvature of SWF
- If govt cannot accumulate debt or assets, then capital stock may be too large or too small
- If govt can accumulate debt or assets, then govt can achieve modified Golden rule
- In that case, long run optimal τ_B is given by a formula similar to previous one (as $\delta \rightarrow 0$): capital accumulation is **orthogonal** to redistributive bequest and capital taxation

Conclusion

- **(1)** Main contribution: simple, tractable formulas for analyzing optimal tax rates on inheritance and capital
- **(2)** Main idea: economists' emphasis on $1+r =$ relative price is excessive (intertemporal consumption distortions exist but are probably second-order)
- **(3)** The important point about the rate of return to capital r is that
 - (a)** r is large: $r > g \rightarrow$ tax inheritance, otherwise society is dominated by rentiers
 - (b)** r is volatile and unpredictable \rightarrow use lifetime K taxes to implement optimal inheritance tax

Extension to optimal consumption tax τ_C

- Consumption tax τ_C redistributes between agents with different tastes s_i for wealth & bequest, not between agents with different inheritance z_i ; so τ_C cannot be a substitute for τ_B
 - But τ_C can be a useful complement for τ_B , τ_L (Kaldor'55)
 - E.g. a positive $\tau_C > 0$ can finance a labor subsidy $\tau_L < 0$: as compared to $\tau_B > 0$, $\tau_L < 0$, this allows to finance redistribution by taxing rentiers who consume a lot more than rentiers who save a lot; given the bequest externality, this is a smart thing to do
- extended optimal tax formulas for τ_B , τ_L , τ_C
- Extension to optimal wealth tax τ_w vs τ_K (2-period model)