

Wealth, Inequality & Taxation

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Wealth and inequality in the long run

- Long run distributional trends = key question asked by 19^C economists
- Many came with apocalyptic answers
- Ricardo-Marx: a small group in society (land owners or capitalists) will capture an ever growing share of income & wealth
 - no “balanced development path” can occur
- During 20^C, a more optimistic consensus emerged: “growth is a rising tide that lifts all boats”
(Kuznets 1953; cold war context)

- But inequality ↑ since 1970s destroyed this fragile consensus (US 1976-2007: ≈60% of total growth was absorbed by top 1%)
 - 19^C economists raised the right questions; we need to address these questions again; we have no strong reason to believe in balanced development path
- 2007-2011 world financial crisis also raised doubts about balanced devt path... will stock options & bonuses, or oil-rich countries, or China, or tax havens, absorb an ever growing share of world resources in 21^C capitalism?

Convergence vs divergence

- **Convergence forces do exist:** diffusion of knowledge btw countries (fostered by econ & fin integration) & wth countries (fostered by adequate educ institutions)
- **But divergence forces can be stronger:**
 - (1) When top earners set their own pay, there's no limit to rent extraction → top income shares can diverge
 - (2) The wealth accumulation process contains several divergence forces, especially with $r > g$ → a lot depends on the net-of-tax global rate of return r on large diversified portfolios : if $r=5\%-6\%$ in 2010-2050 (=what we observe in 1980-2010 for large Forbes fortunes, or Abu Dhabi sovereign fund, or Harvard endowment), then global wealth divergence is very likely

This lecture: two issues

- **1. The rise of the working rich** (≈1h, slides 1-22)
 - Atkinson-Piketty-Saez, « Top Incomes in the Long Run of History », JEL 2011
 - New results from *World Top Incomes Database (WTID)*
 - Piketty-Saez-Stantcheva, « Optimal Taxation of Top Labor Income: A Tale of Three Elasticities », NBER WP 2011

(key mechanism: grabbing hand)

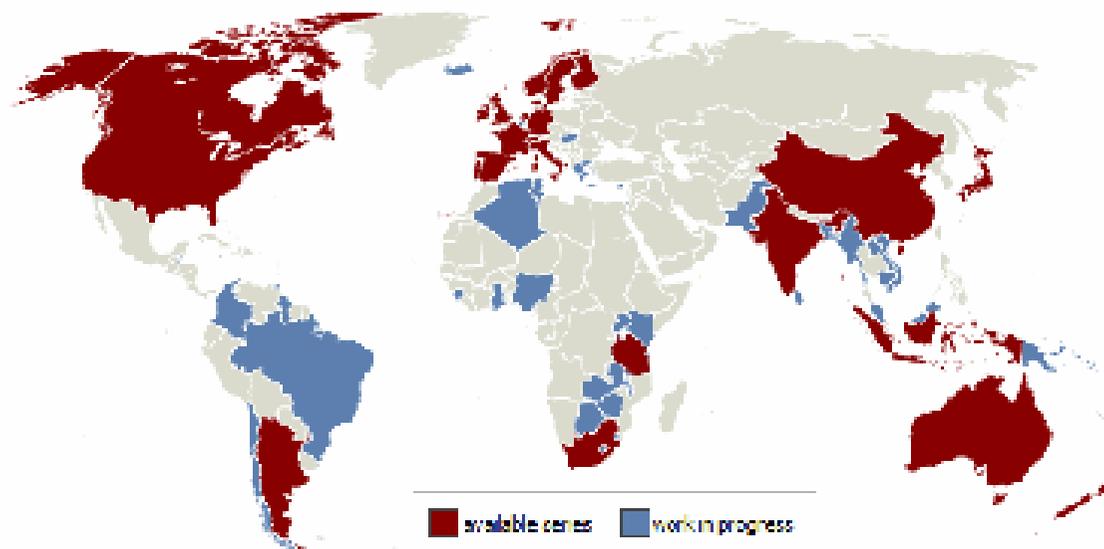
- **2. The return of wealth & inheritance** (≈1h30, slides 23-76)
 - Piketty, « On the Long Run Evolution of Inheritance », QJE 2011
 - Piketty-Zucman, « Capital is Back: Wealth-Income Ratios in Rich Countries 1870-2010 », WP PSE 2012
 - First results from *World Wealth Database (preliminary)*
 - Piketty-Saez, « A Theory of Optimal Capital Taxation », NBER WP 2012

(key mechanism: $r > g$)
(r = rate of return to wealth, g = growth rate)

1. The Rise of the Working Rich

- **World top incomes database:** 25 countries, annual series over most of 20^C, largest historical data set
- **Two main findings:**
 - **The fall of rentiers:** inequality ↓ during first half of 20^C = top capital incomes hit by 1914-1945 capital shocks; did not fully recover so far (long lasting shock + progressive taxation)
 - without war-induced economic & political shock, there would have been no long run decline of inequality; nothing to do with a Kuznets-type spontaneous process
 - **The rise of working rich:** inequality ↑ since 1970s; mostly due to top labor incomes, which rose to unprecedented levels; top wealth & capital incomes also recovering, though less fast
 - **what happened?**

THE WORLD TOP INCOMES DATABASE



- Home
- Introduction
- The Database
- Graphics
- Country Information
- Work In Progress
- Acknowledgments



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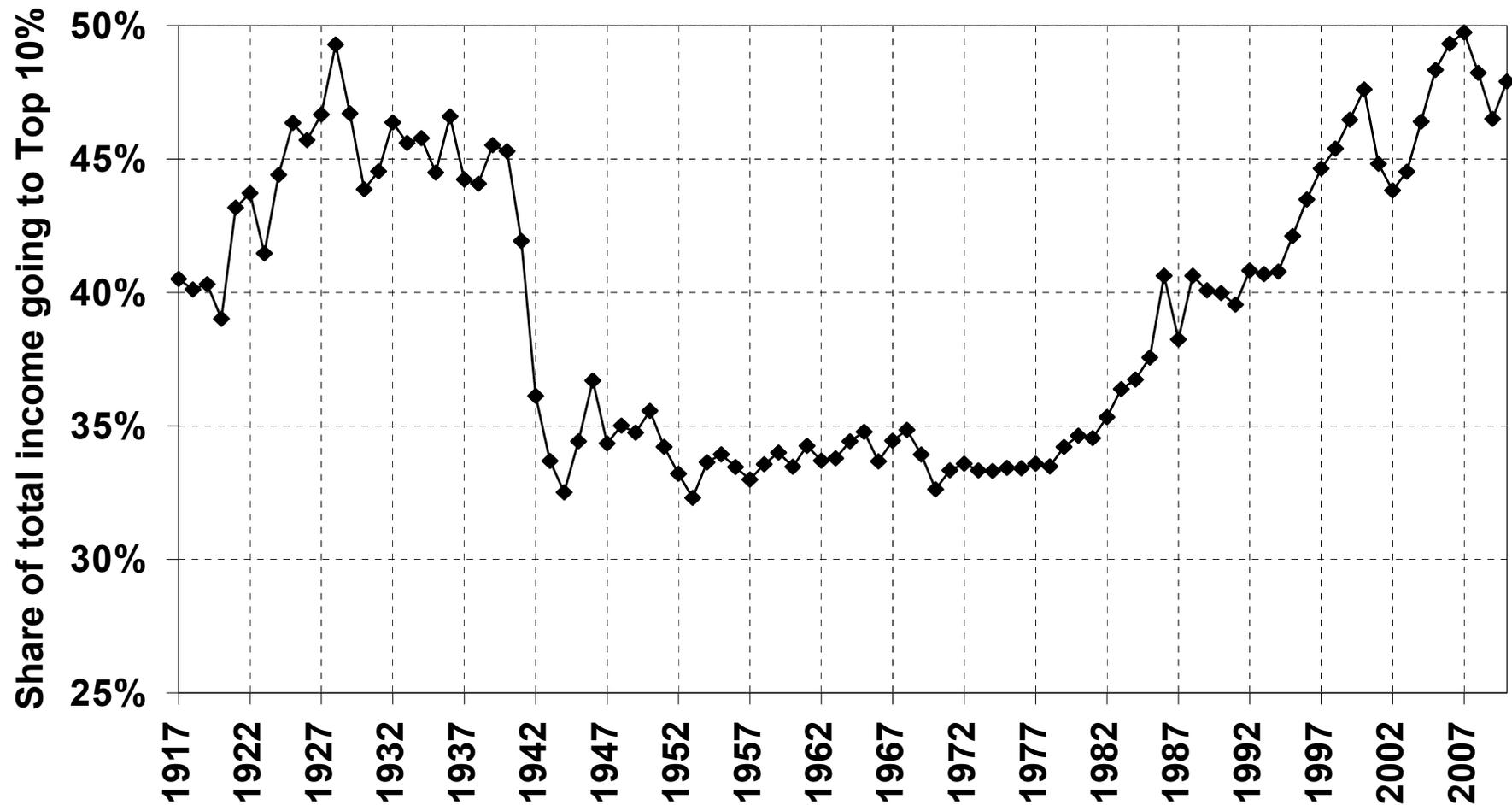


FIGURE 1

The Top Decile Income Share in the United States, 1917-2010

Source: Piketty and Saez (2003), series updated to 2010.

Income is defined as market income including realized capital gains (excludes government transfers).

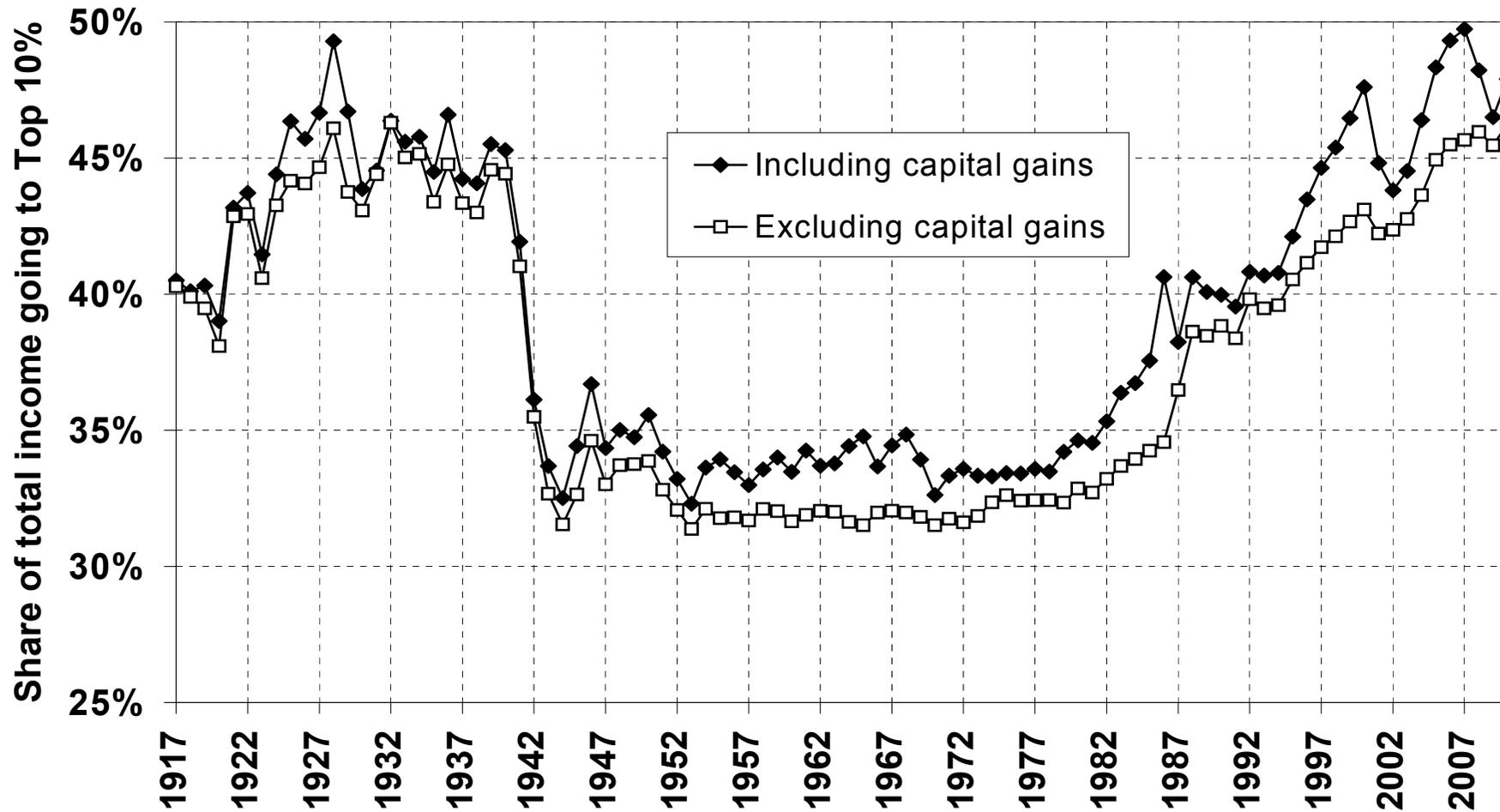


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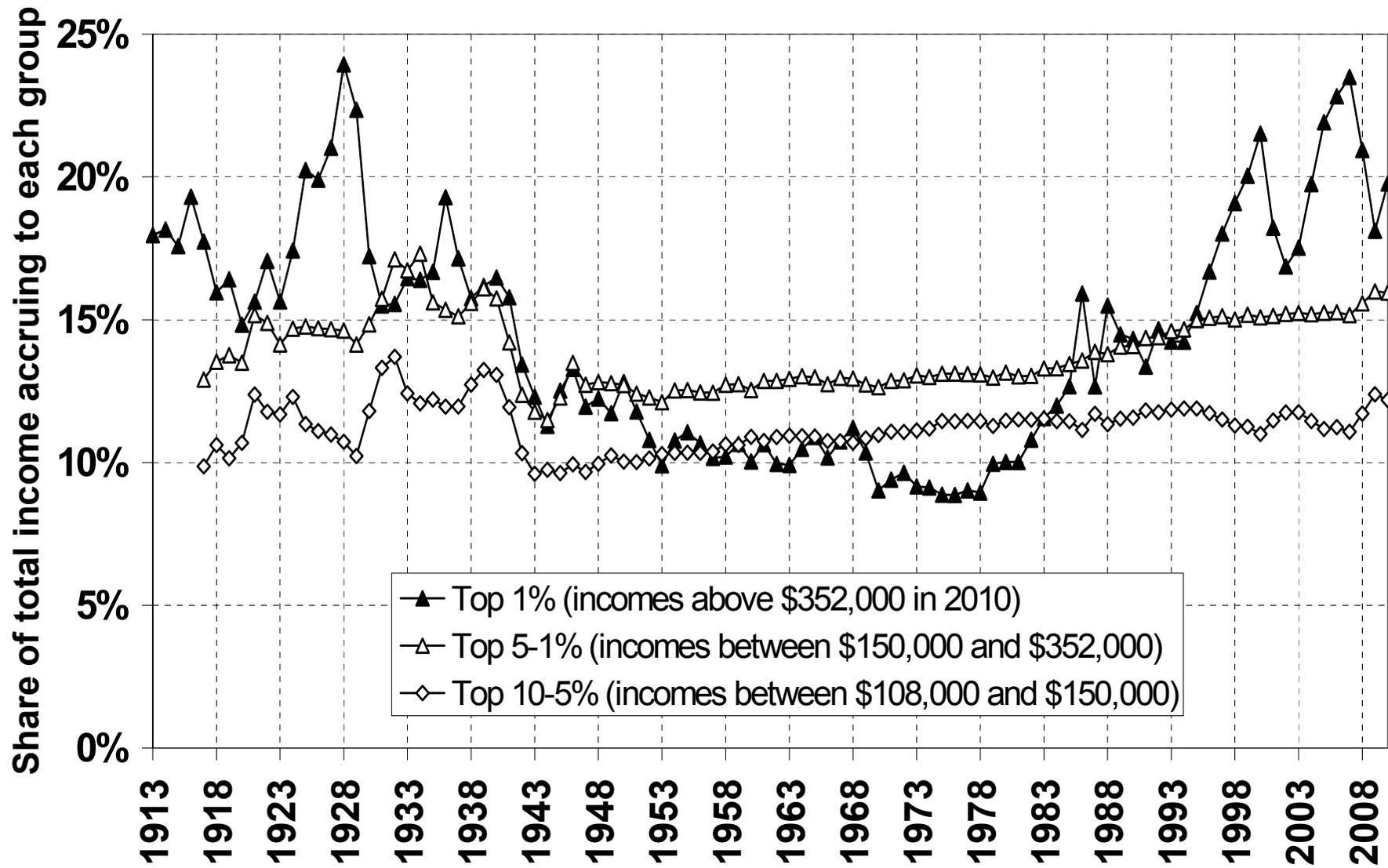
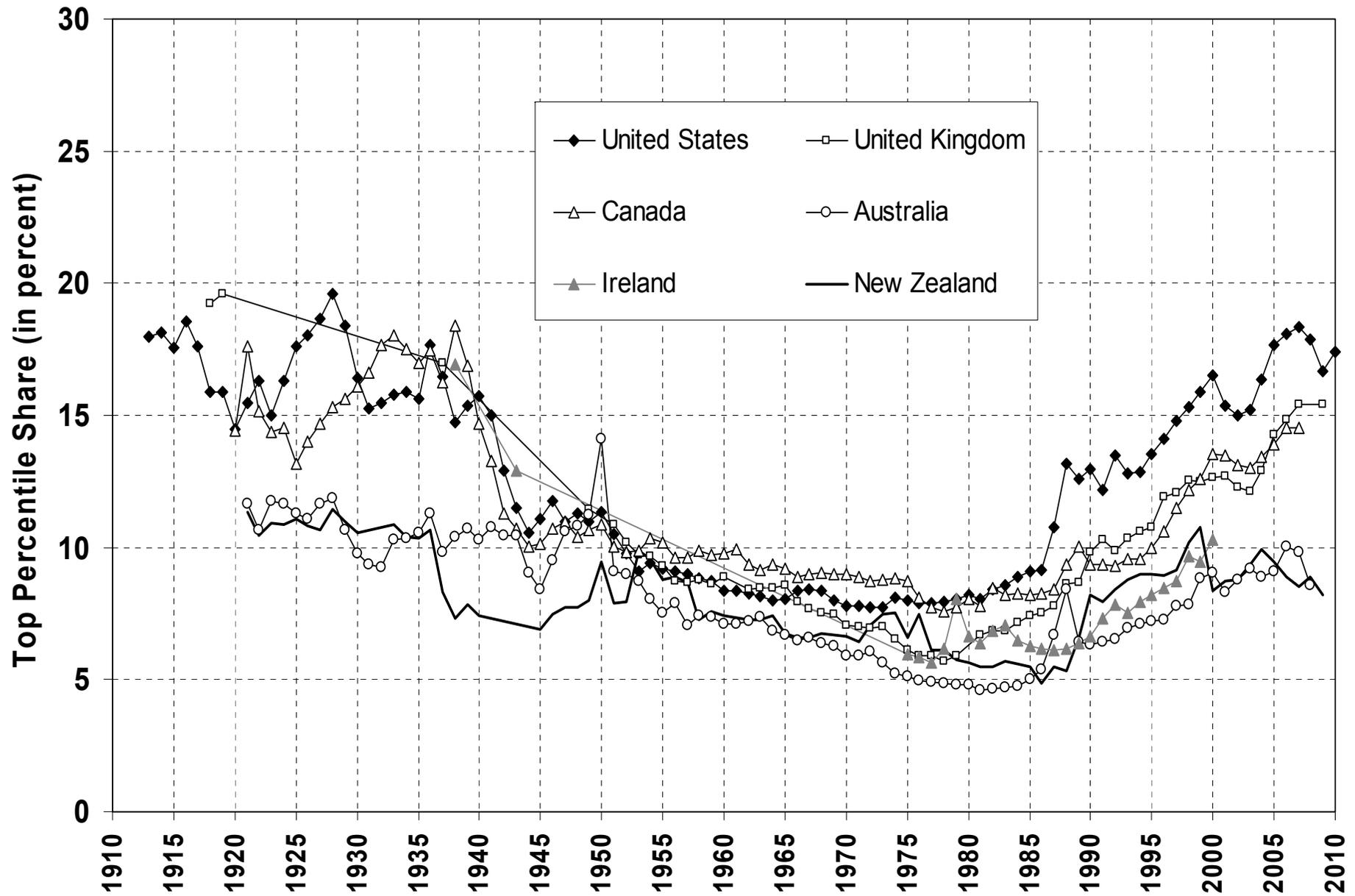


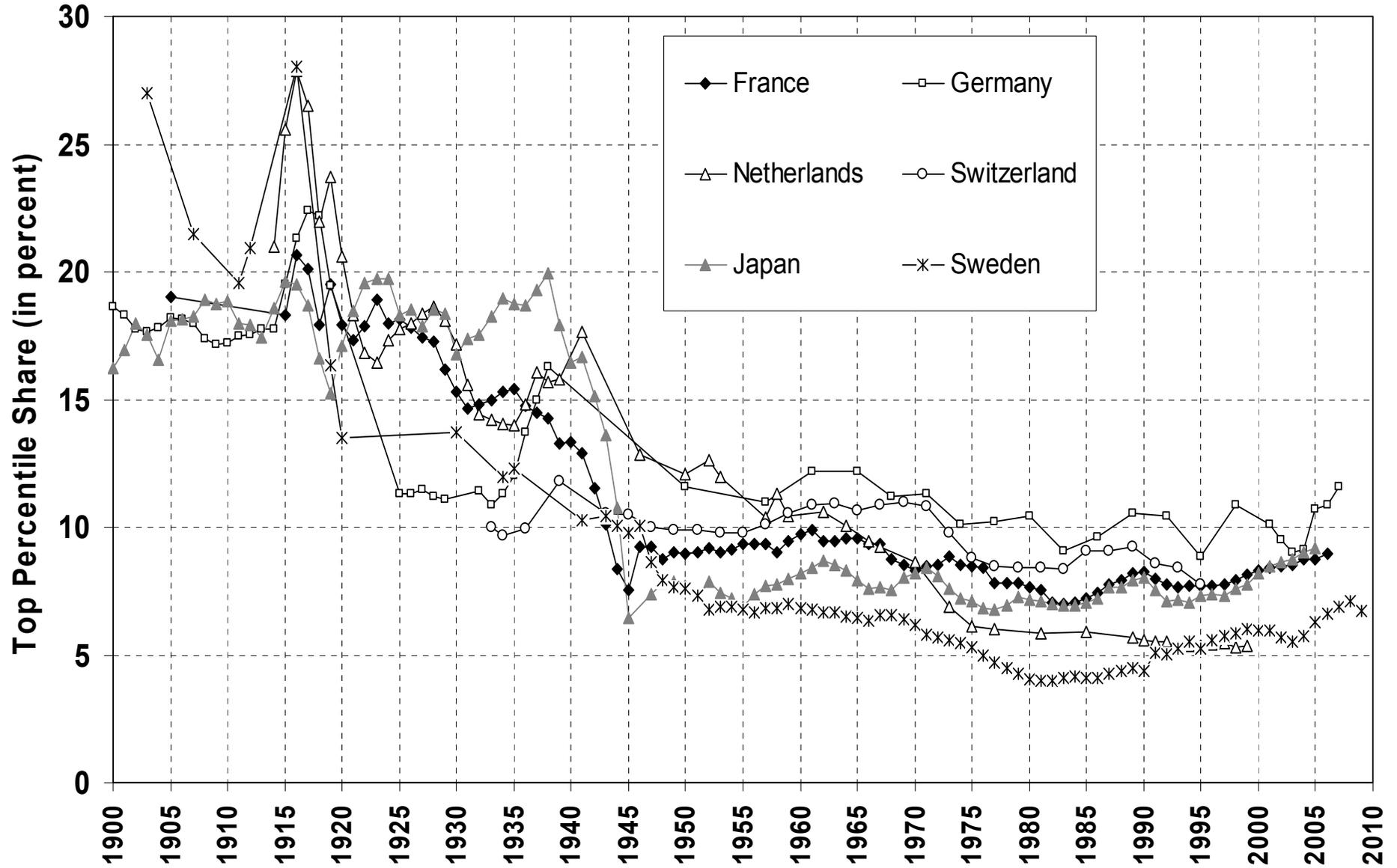
FIGURE 2

Decomposing the Top Decile US Income Share into 3 Groups, 1913-2010

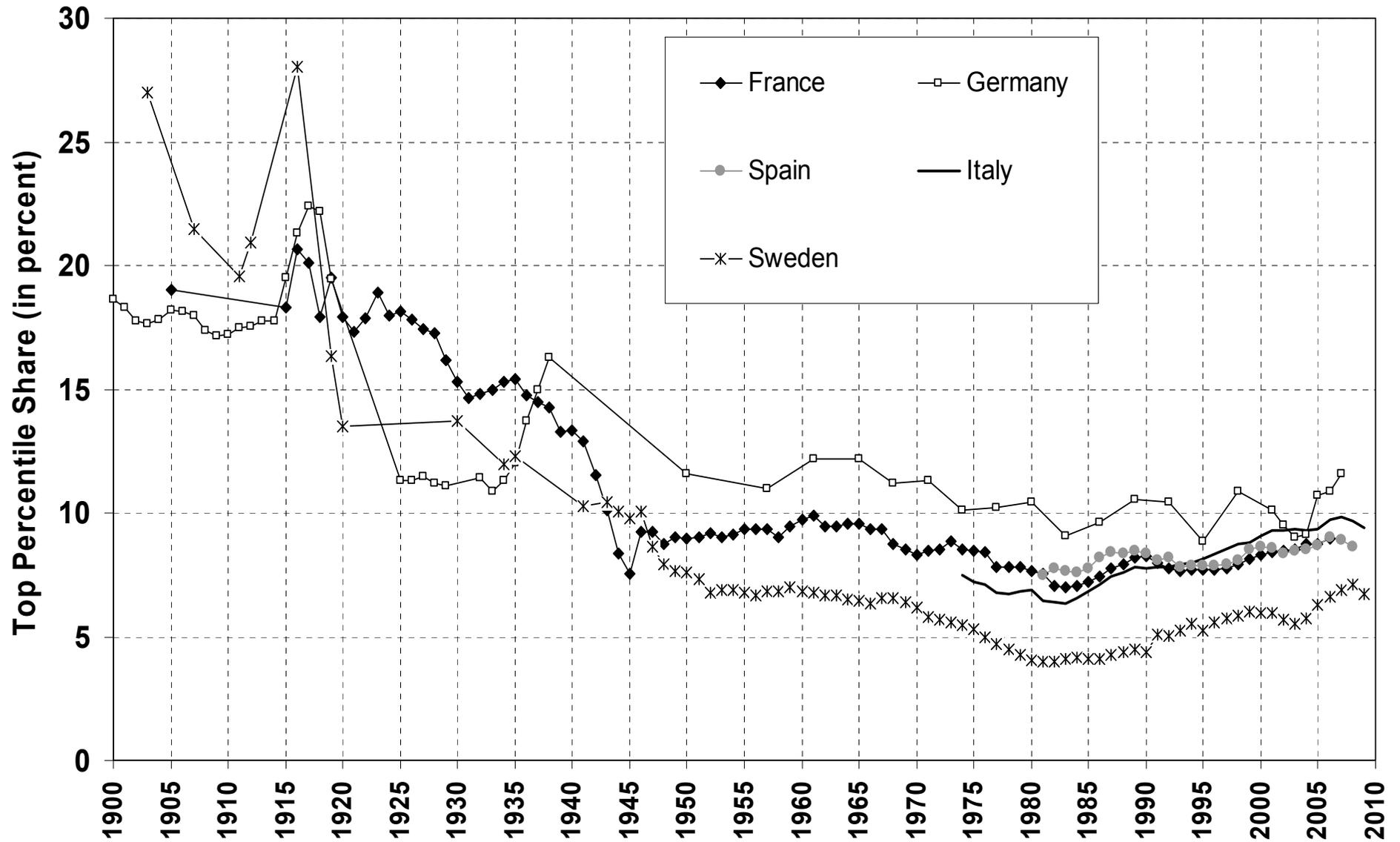
Top 1% share: English Speaking countries (U-shaped), 1910-2010



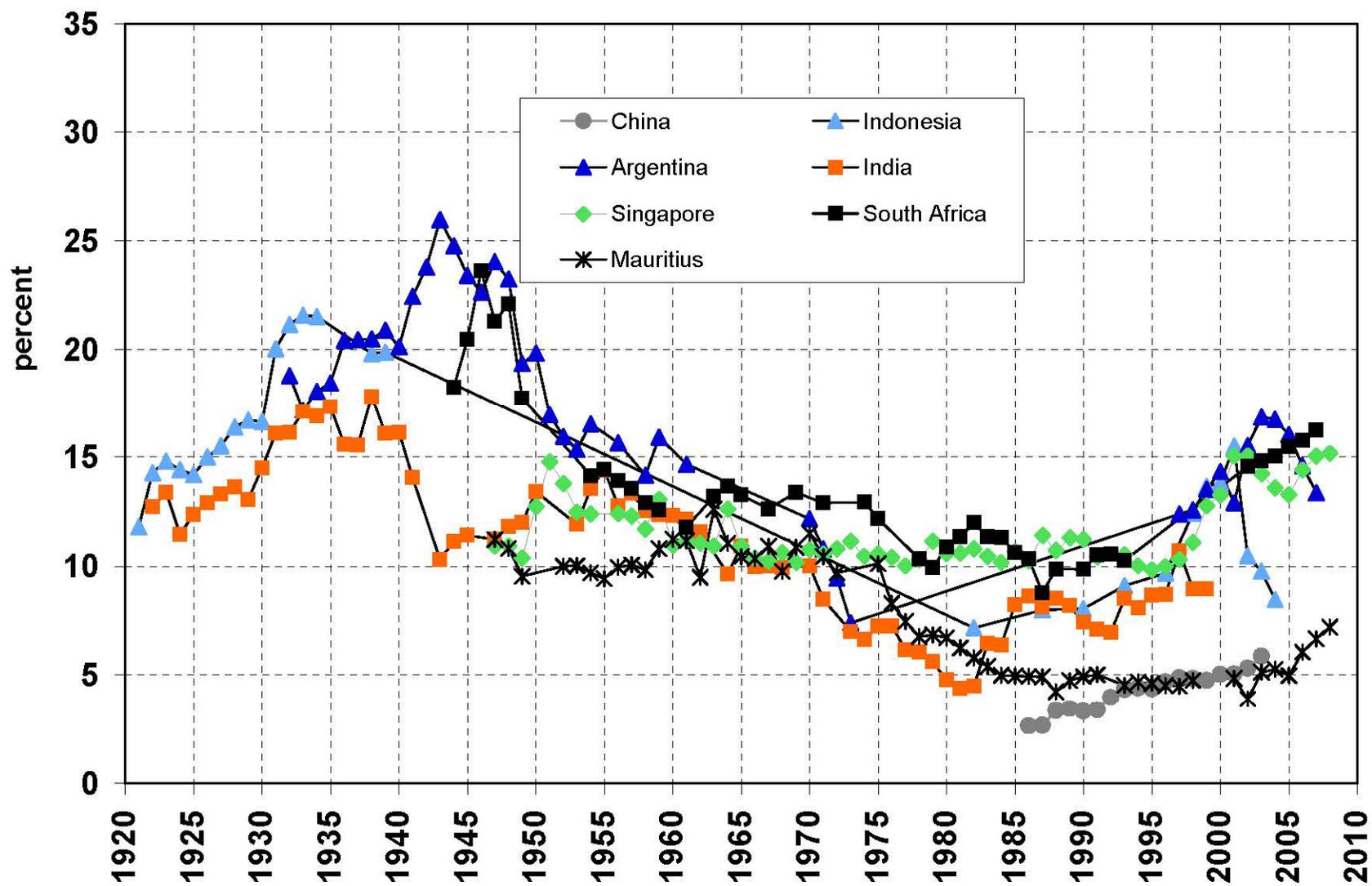
Top 1% share: Continental Europe and Japan (L-shaped), 1900-2010



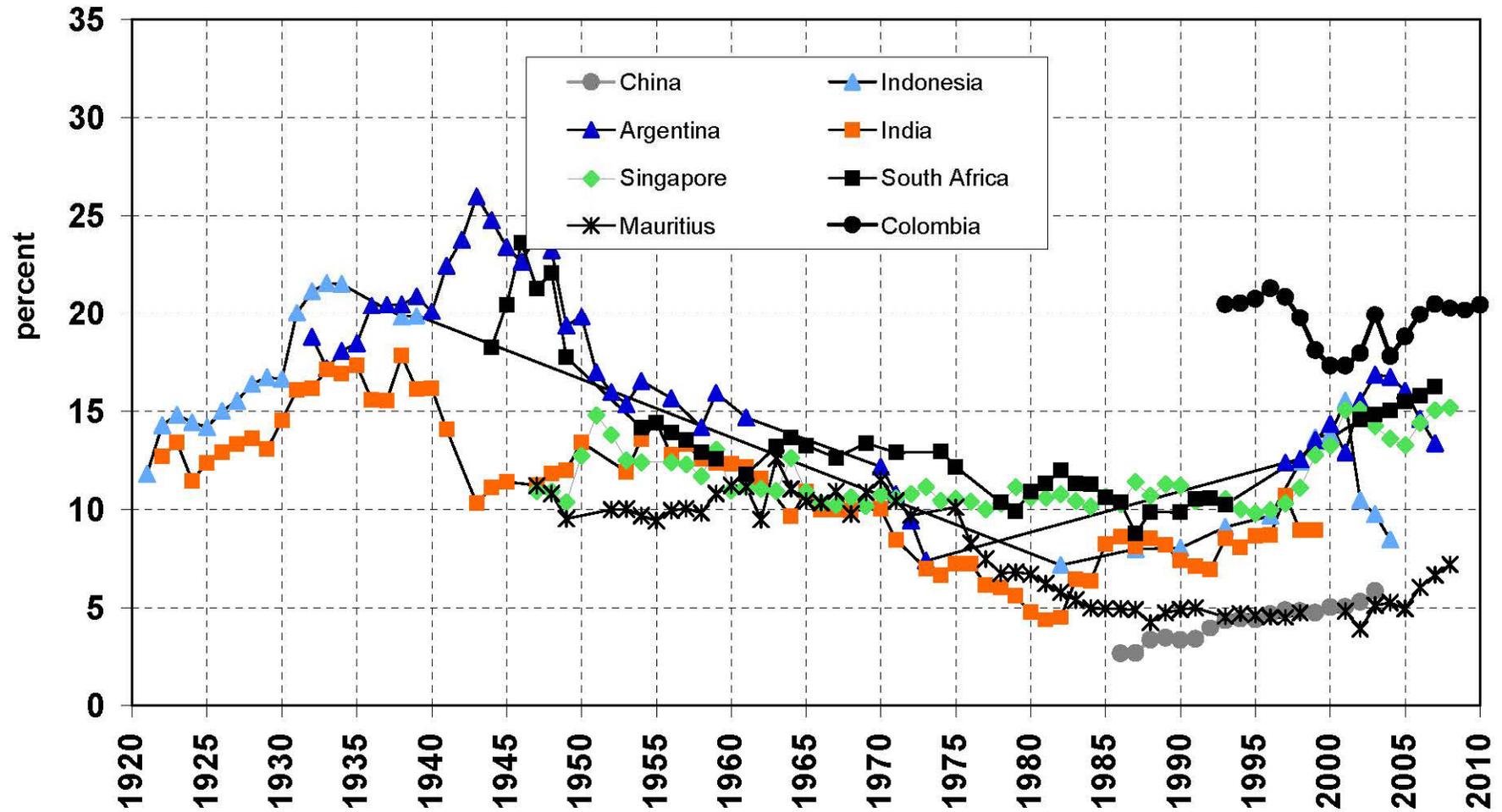
Top 1% share: Continental Europe, North vs South (L-shaped), 1900-2010



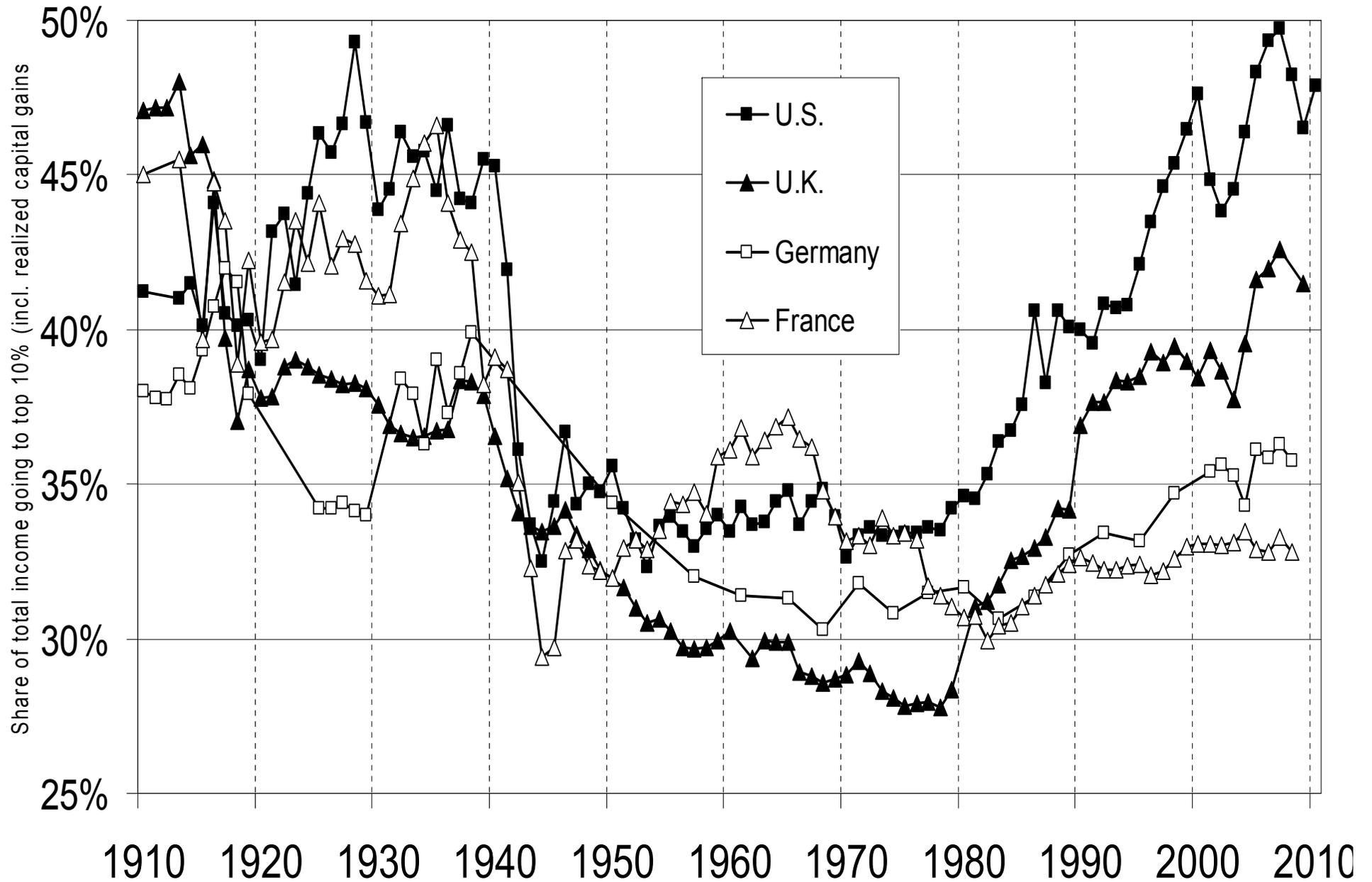
Top 1% share: Developing and emerging countries, 1920-2010



Top 1% share: Developing and emerging countries, 1920-2010



Top Decile Income Shares 1910-2010



Source: World Top Incomes Database, 2012. Missing values interpolated using top 5% and top 1% series.

Why did top incomes rise so much?

- Hard to account for observed cross-country variations with a pure technological, marginal-product story
 - One popular view: US today = working rich get their marginal product (globalization, superstars); Europe today (& US 1970s) = market prices for high skills are distorted downwards (social norms, etc.)
- very naïve view of the top end labor market...
- & very ideological: we have zero evidence on the marginal product of top executives; it could well be that prices are distorted upwards...

- A more realistic view: grabbing hand model = marginal products are unobservable; top executives have an obvious incentive to convince shareholders & subordinates that they are worth a lot; no market convergence because constantly changing corporate & job structure (& costs of experimentation → **competition not enough**)

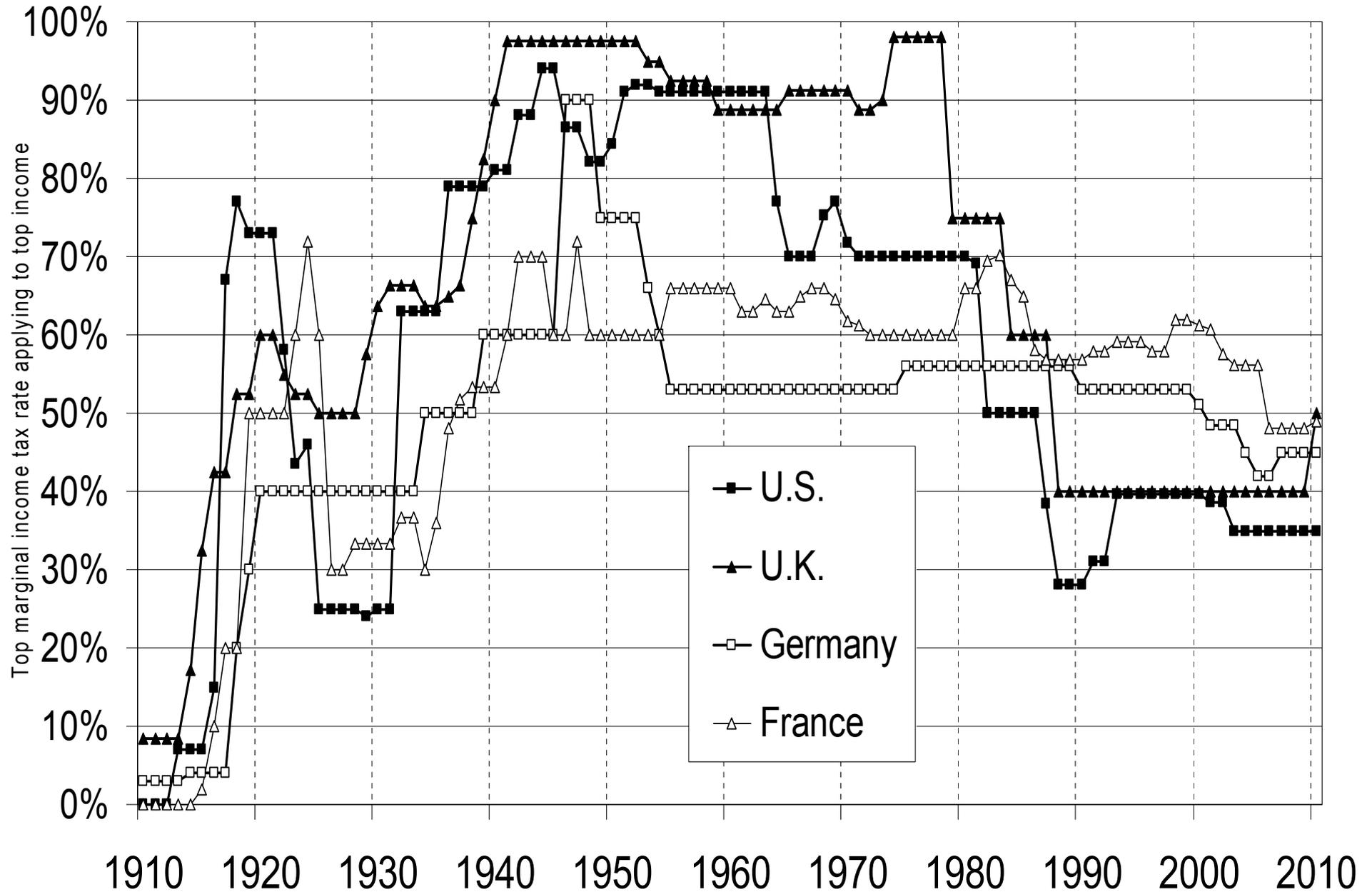
→ when pay setters set their own pay, there's no limit to rent extraction... **unless confiscatory tax rates at the very top**

(memo: US top tax rate (1m\$+) 1932-1980 = 82%)

(no more fringe benefits than today)

→ see Piketty-Saez-Stantcheva, NBER WP 2011

Top Income Tax Rates 1910-2010



Source: World Top Incomes Database, 2012.

Optimal Taxation of Top Labor Incomes

- **Standard optimal top tax rate formula: $\tau = 1/(1+ae)$**

With: e = elasticity of labor supply, a = Pareto coefficient

- $\tau \downarrow$ as elasticity $e \uparrow$: don't tax elastic tax base
- $\tau \uparrow$ as inequality \uparrow , i.e. as Pareto coefficient $a \downarrow$
(US: $a \approx 3$ in 1970s $\rightarrow \approx 1.5$ in 2010s; $b = a/(a-1) \approx 1.5 \rightarrow \approx 3$)
(memo: $b = E(y|y > y_0)/y_0$ = measures fatness of the top)

- **Augmented formula: $\tau = (1+tae_2+ae_3)/(1+ae)$**

With $e = e_1 + e_2 + e_3$ = labor supply elasticity + income shifting elasticity + bargaining elasticity (rent extraction)

- **Key point: $\tau \uparrow$ as elasticity $e_3 \uparrow$**

**Table 4: How Much Should We Tax Top Incomes ?
A Tale of Three Elasticities**

Total elasticity $e = e_1 + e_2 + e_3 =$	0.5
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Scenario 1: Standard supply side tax effects	
$e_1 =$	0.5
$e_2 =$	0.0
$e_3 =$	0.0

Scenario 2: Tax avoidance effects	
(a) current narrow tax base	(b) after base broadening
$e_1 = 0.2$	$e_1 = 0.2$
$e_2 = 0.3$	$e_2 = 0.1$
$e_3 = 0.0$	$e_3 = 0.0$

Scenario 3: Compensation bargaining effects	
$e_1 =$	0.2
$e_2 =$	0.0
$e_3 =$	0.3

Optimal top tax rate $\tau^* = (1 + ae_2 + ae_3)/(1 + ae)$
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Pareto coefficient $a =$	1.5
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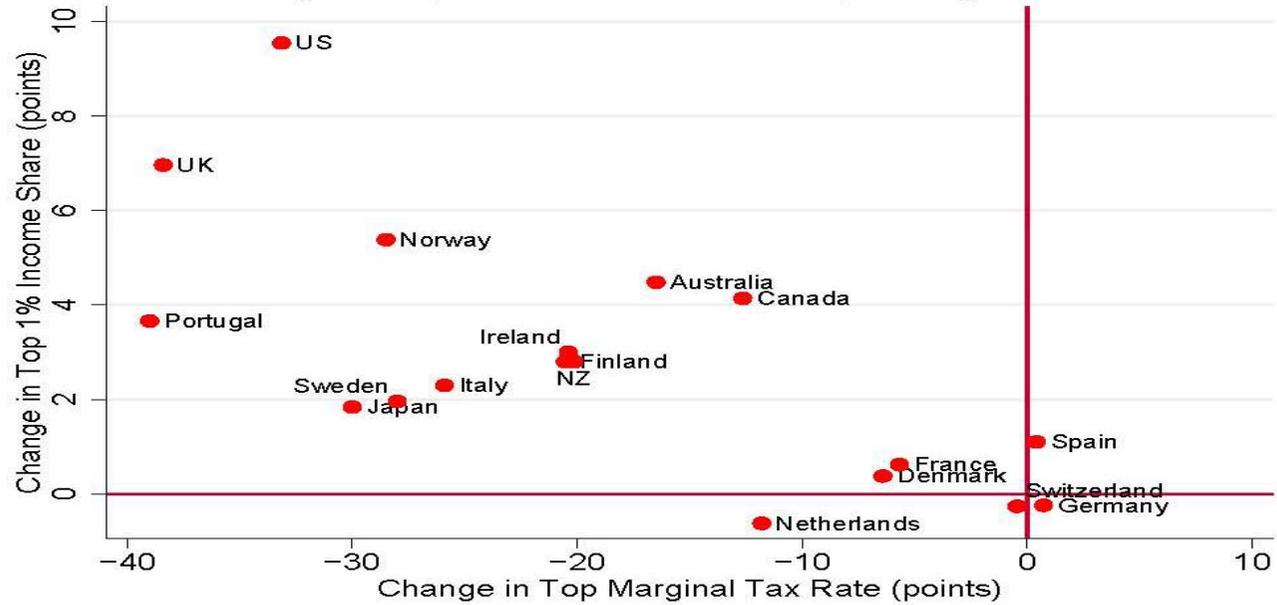
Alternative tax rate $t =$	20%
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Scenario 1	
$\tau^* =$	57%

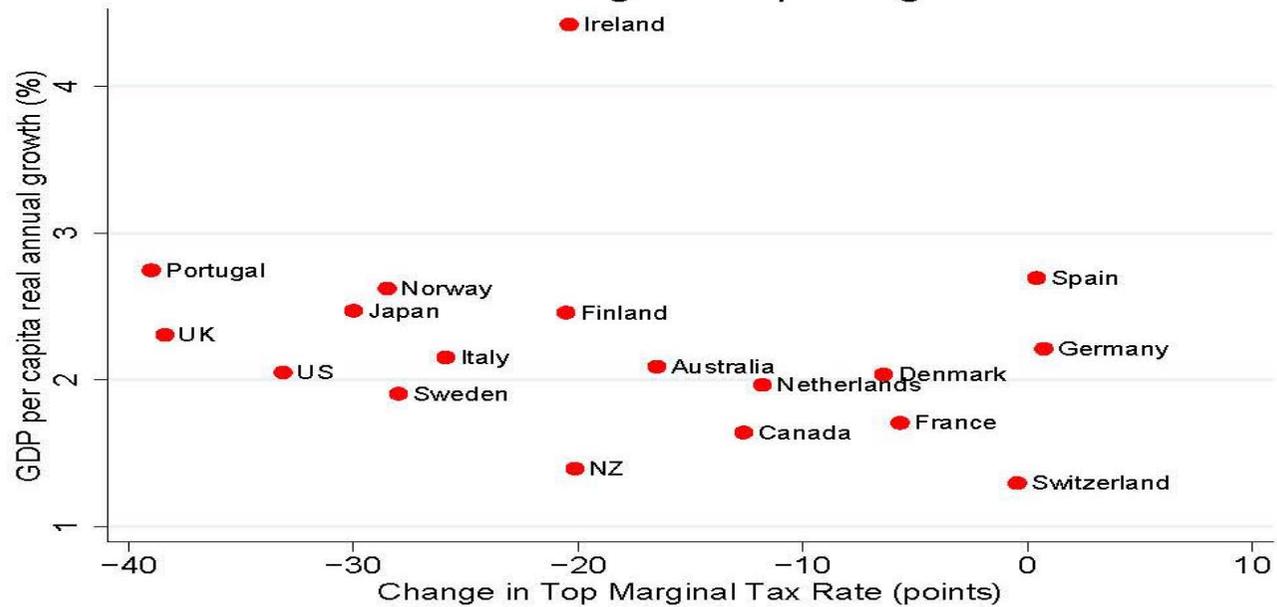
Scenario 2	
(a) $e_2=0.3$	(b) $e_2=0.1$
$\tau^* = 62\%$	$\tau^* = 71\%$

Scenario 3	
$\tau^* =$	83%

A. Changes Top 1% Share and Top Marginal Tax Rate



B. Growth and Change in Top Marginal Tax Rate



2. The return of wealth & inheritance

- The rise of top incomes should fuel the rise of top wealth
- But there are other long-run effects explaining the return of wealth & inheritance
- Two different effects (could go separately):

(2a) The return of wealth

(Be careful with « human capital » illusion: human k did not replace old-style financial & real estate wealth)

(2b) The return of inherited wealth

(Be careful with « war of ages » illusion: the war of ages did not replace class war)

2a. The return of wealth

- The « human capital » illusion: « in today's modern economies, what matters is human capital and education, not old-style financial or real estate wealth »
- Technocratic model : Parsons, Galbraith, Becker
(unidimensional class structure based upon human K)
- But the share of old-style capital income (rent, interest, dividend, etc.) in national income is the same in 2010 as in 1910 (about 30%), and the ratio between aggregate private wealth and national income is also the same in 2010 as in 1910 (about 600%)
- Today in France, Italy, UK: $\beta = W/Y \approx 600\%$
Per adult national income $Y \approx 30\,000\text{€}$
Per adult private wealth $W \approx 200\,000\text{€}$
(wealth = financial assets + real estate assets – financial liabilities)
(on average, households own wealth equal to about 6 years of income)

- There are several long-run effects explaining the return of high wealth-income ratios :
 - it took a long time to recover from world war shocks
(1913 stock mkt & real estate capitalization recovered during 2000s)
 - financial deregulation & tax competition → rising capital shares and wealth-income ratios
 - growth slowdown in rich countries: $r > g$
 - rise of wealth-income and inheritance-income ratios
 - + rise of wealth inequality (amplifying mechanism)
 - (r = rate of return to wealth, g = productivity growth + pop growth)
- **Aggregate effect: Harrod-Domar-Solow formula: $\beta^* = s/g$**
 - (β^* = wealth-income ratio, s = saving rate)
 - (i.e. $s=10\%$, $g=2\%$ → $\beta^*=500\%$; if $g=1\%$, then $\beta^*=1000\%$)
 - (i.e. if we save 10% of income each year, then in the long run we accumulate 5 years of income if growth rate is 2%)
 - highly unstable process if growth rate is low

- Main results from Piketty-Zucman, « Capital is Back: Wealth-Income Ratios in Rich Countries 1870-2010 »
- **How do aggregate wealth-income ratios evolve in the long run, and why?**
- Until recently, it was impossible to address properly this basic question: national accounts were mostly about flows on income, output, savings, etc., and very little about stocks of assets and liabilities
- **In this paper we compile a new data set of national balance sheets in order to address this question:**
 - 1970-2010: US, Japan, Germany, France, UK, Italy, Canada, Australia (= top 8 rich countries)
 - 1870-2010: US, Germany, France, UK(official national accounts + historical estimates)

- **Result 1:** we find in every country a gradual rise of wealth-income ratios over 1970-2010 period, from about 200%-300% in 1970 to 400%-600% in 2010
- **Result 2:** in effect, today's ratios seem to be returning towards the high values observed in 19^c Europe (600%-700%)
- This can be accounted for by a combination of factors:
 - Politics: long run asset price recovery effect (itself driven by changes in capital policies since WWs)
 - Economics: slowdown of productivity and pop growth

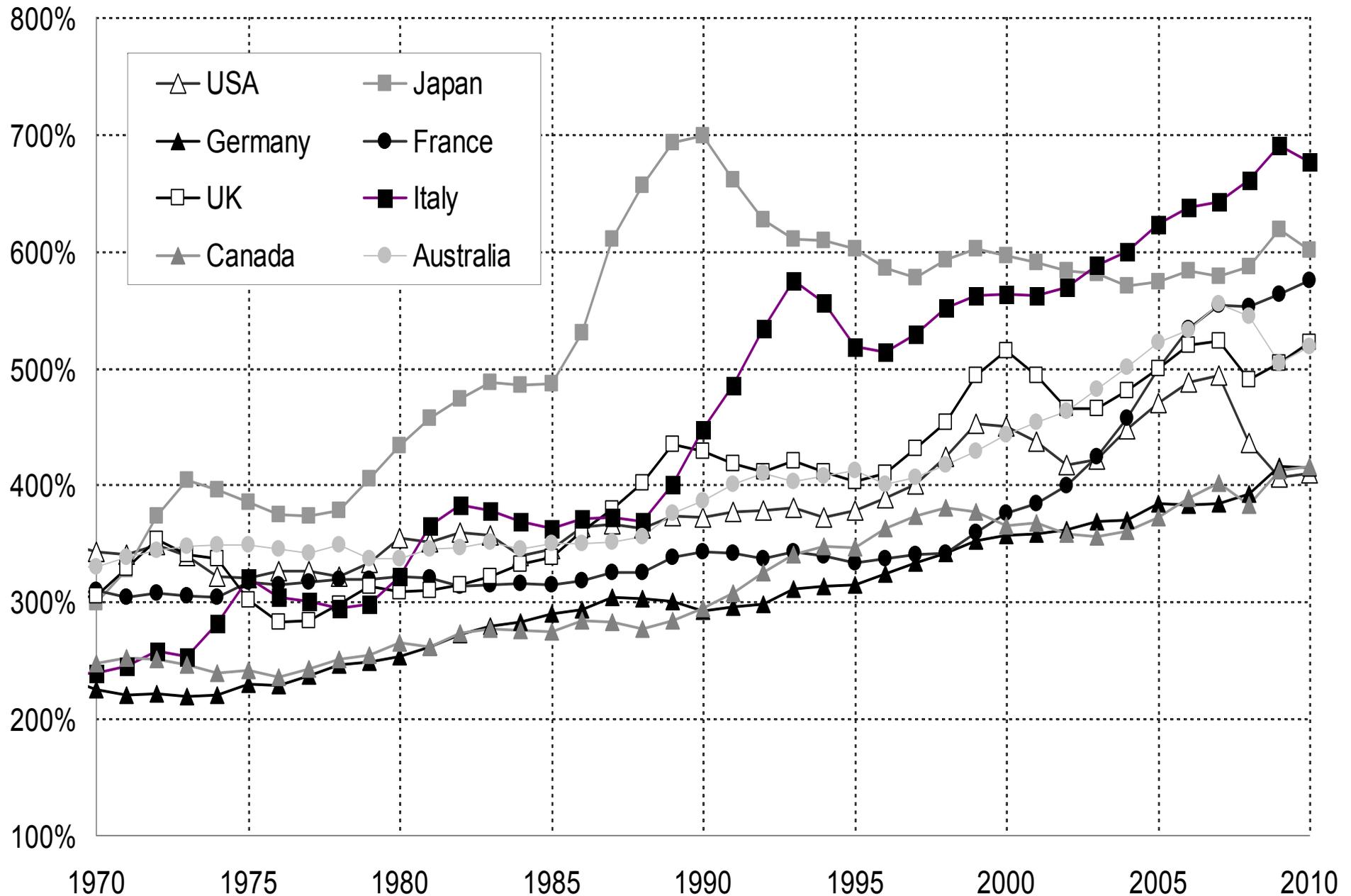
Harrod-Domar-Solow: wealth-income ratio $\beta = s/g$

If saving rate $s=10\%$ & growth rate $g=3\%$, then $\beta \approx 300\%$

But if $s=10\%$ & $g=1.5\%$, then $\beta \approx 600\%$

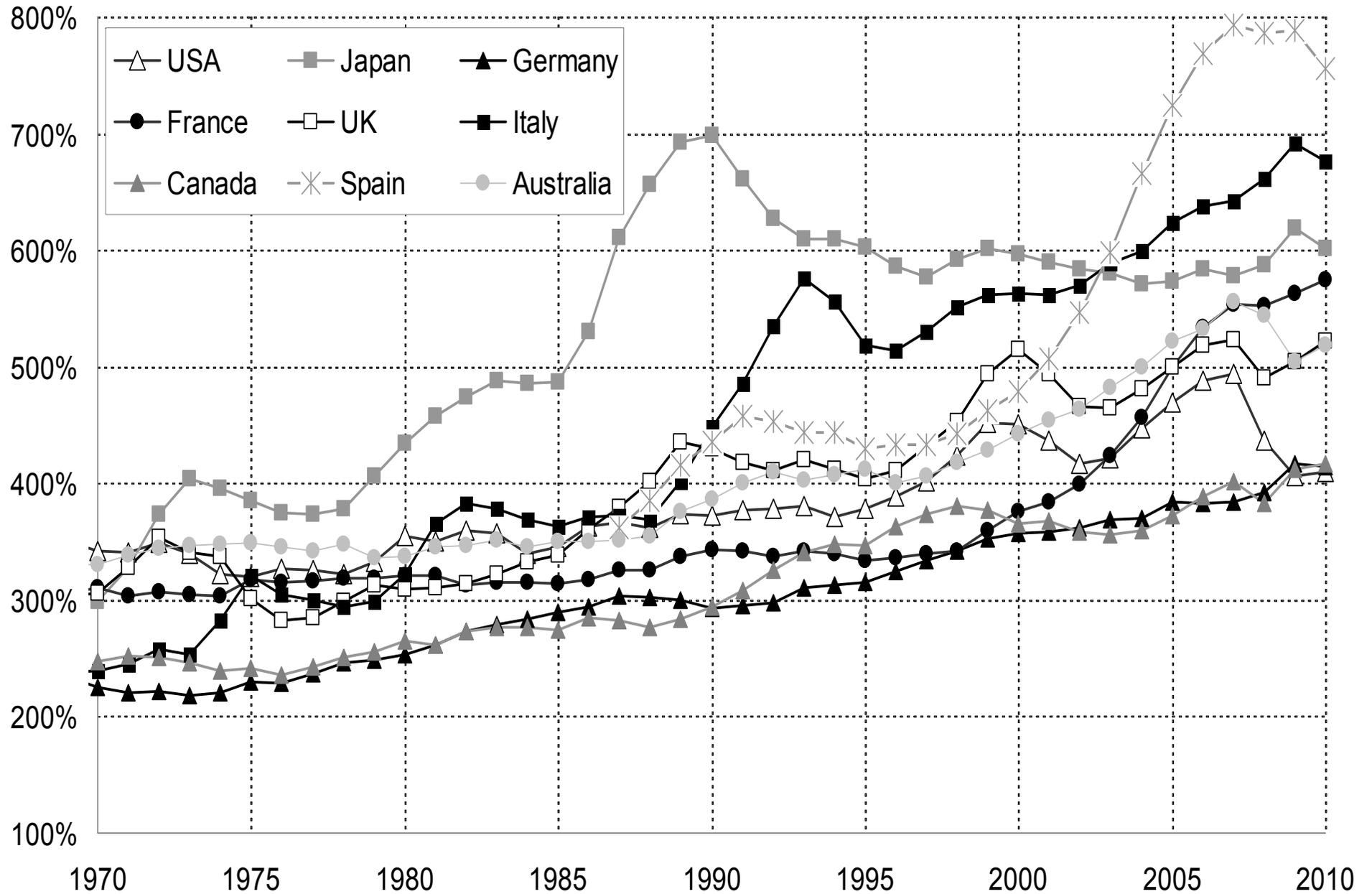
Explains long run change & level diff Europe vs US

Private wealth / national income ratios, 1970-2010



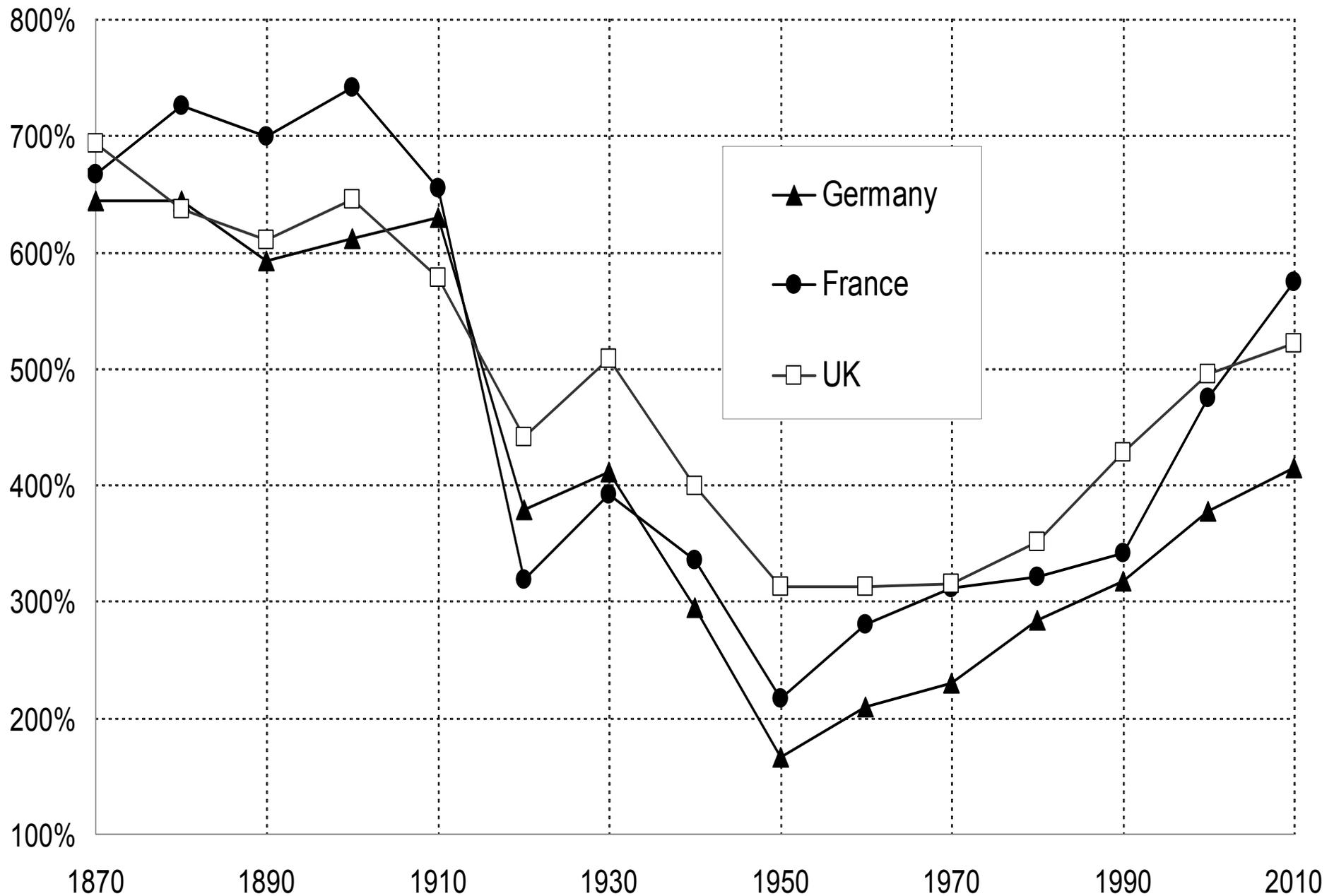
Authors' computations using country national accounts. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors)

Private wealth / national income ratios, 1970-2010 (incl. Spain)



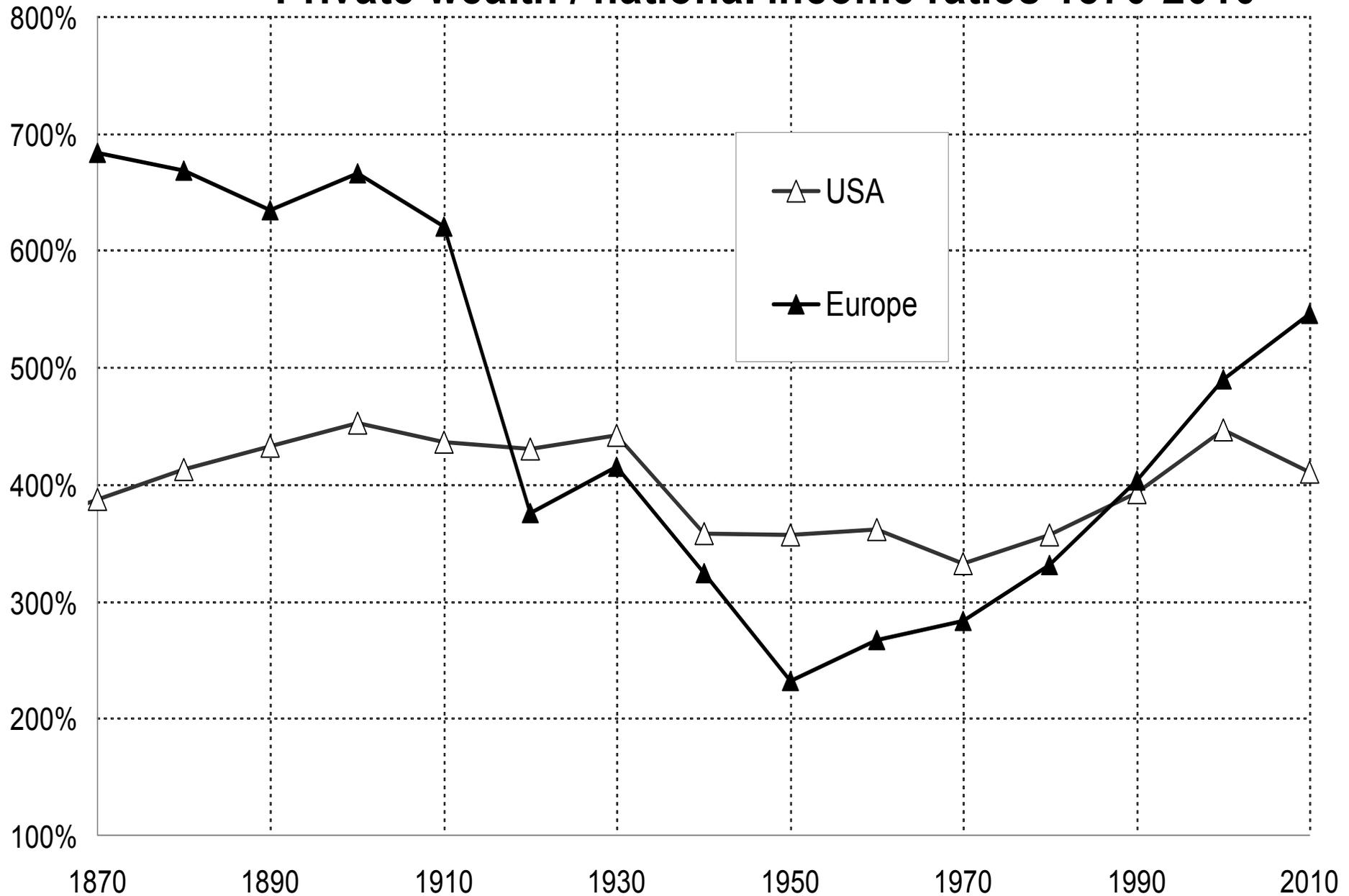
Authors' computations using country national accounts. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors)

Private wealth / national income ratios in Europe, 1870-2010



Authors' computations using country national accounts. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors)

Private wealth / national income ratios 1870-2010



Authors' computations using country national accounts. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors)

- **Lesson 1:** one-good capital accumulation model with factor substitution works relatively well in the long run; but in short & medium run, volume effects (saving flows) can be vastly dominated by relative price effects (capital gains or losses)
- **Lesson 2:** long run wealth-income ratios $\beta = s/g$ can vary a lot btw countries: s and g determined by diff. forces; countries with low g and high s naturally have high β ; high β is not bad per se (capital is useful); but **high β raises new issues about capital regulation and taxation:**
- With integrated capital markets, this can generate large net foreign asset positions, even in the absence of income diff (or reverse to income diff); so far net positions are smaller than during colonial period; but some countries positions are rising fast (Japan, Germany,..)
- With limited capital mobility, and/or home portfolio biases, high β can lead to large domestic asset price bubbles: see Japan, UK, Italy, France, Spain,.

- **Lesson 3: wealth and technology in 21c : $\sigma > 1$**

Global rate of return r doesn't seem to decline as much as the rise in global β , i.e. global capital share $\alpha = r\beta \uparrow$ as $\beta \uparrow$ since 1970
→ long run K/L elasticity of substitution $\sigma > 1$, or rising market power for K, or both ?

- **Lesson 4: wealth and technology in 18c : $\sigma < 1$**

- In the very long run, i.e. using national wealth estimates over 1700-2010 for UK & France, we find β stable around 600%-700%, in spite of huge changes in wealth composition, from agricultural land to manufacturing and housing

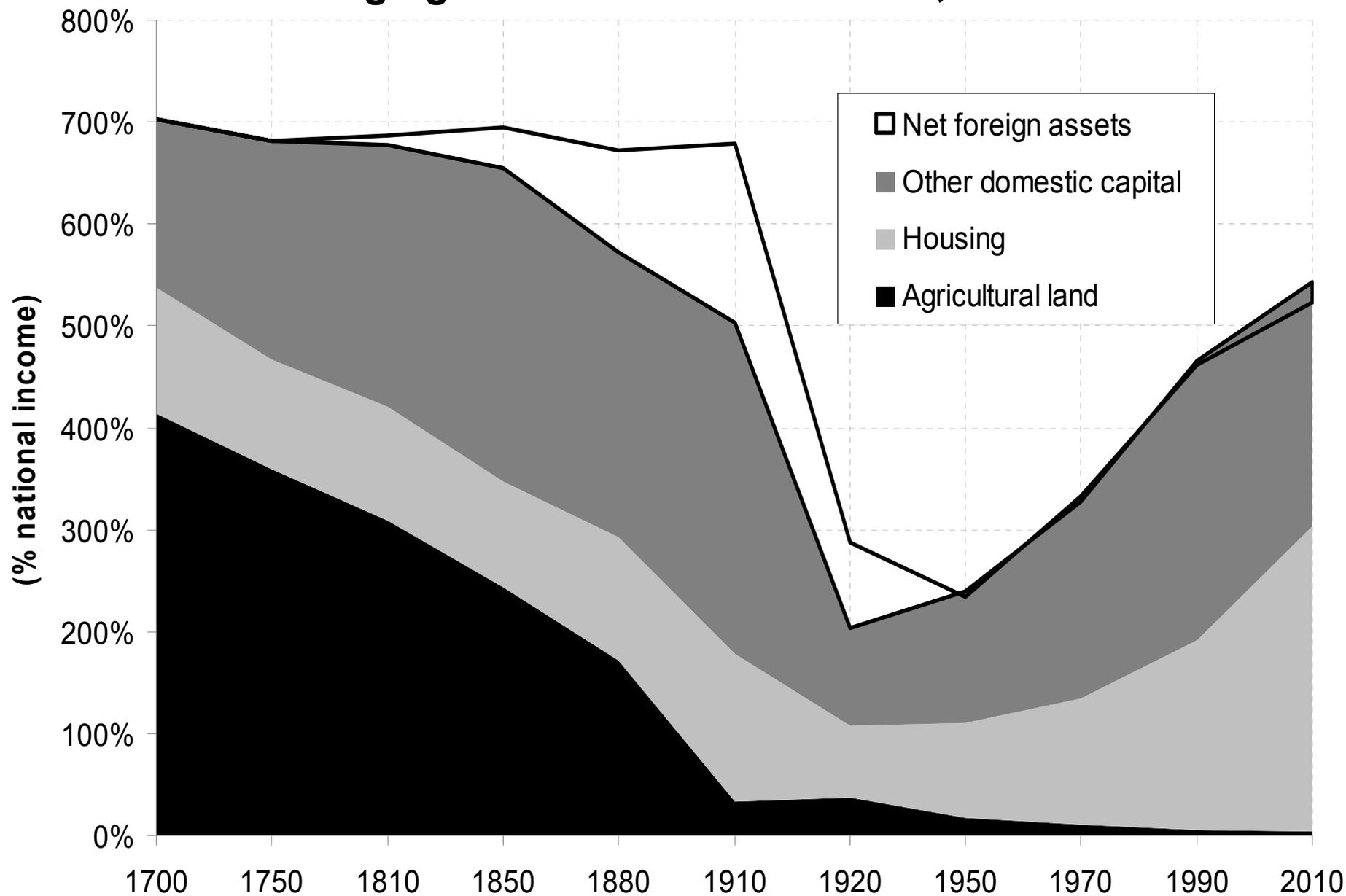
- In agrarian, very-low-growth societies, however, it is unclear which forces dominate: $\beta = s/g$ or $\beta = \alpha/r$? Probably $\beta = \alpha/r$

- I.e. with α = capital share = mostly land rent: determined by technology, politics, & land availability ($\alpha \approx 30\%-40\%$ in Europe, vs 10%-15% in land-rich New world, i.e. elast. subst. $\sigma < 1$), and r = rate of return = 4%-5% = rate of time preference

→ $\beta = 600\%-700\%$ in Europe, vs 200%-300% in New World

(simply bc very abundant land is worthless; nothing to do with the $\beta = s/g$ mechanism, which bumped it in later, with migration)

The changing nature of national wealth, UK 1700-2010



National wealth = agricultural land + housing + other domestic capital goods + net foreign assets

Concepts & methods

- National income $Y = \text{domestic output } Y_d + r \text{ NFA}$
- Private wealth $W = \text{non-financial assets} + \text{financial assets} - \text{financial liabilities}$ (household & non-profit sector)
- $\beta = W/Y = \text{private wealth-national income ratio}$

- Govt wealth $W_g = \text{non-fin} + \text{fin assets} - \text{fin liab}$ (govt sector)
- National wealth $W_n = W + W_g = K + \text{NFA}$

with $K = \text{domestic capital}$ (= land + housing + other domestic k)

$\text{NFA} = \text{net foreign assets}$

- $\beta_n = W_n/Y = \text{national wealth-national income ratio}$
- Domestic output $Y_d = F(K,L)$ ($L = \text{labor input}$) (e.g. $K^\alpha L^{1-\alpha}$)
- Capital share $\alpha = r \beta$ ($r = \text{average rate of return to wealth}$)

- **One-good capital accumulation model:** $W_{t+1} = W_t + s_t Y_t$
 $\rightarrow \beta_{t+1} = \beta_t (1+g_{wt})/(1+g_t)$

With $1+g_{wt} = 1+s_t/\beta_t =$ saving-induced wealth growth rate)

$1+g_t = Y_{t+1}/Y_t =$ exogenous output growth rate (productiv.+pop)

- With fixed saving rate $s_t=s$ and growth rate $g_t=g$, then:
 $\beta_t \rightarrow \beta = s/g$ (Harrod-Domar-Solow steady-state formula)
- E.g. if $s=10\%$ & $g=2\%$, then $\beta = 500\%$

- **Pure accounting formula:** valid with any saving motive or utility function, i.e. wherever s comes from
- Wealth or bequest in the utility function: saving rate s set by $u()$ (intensity of wealth or bequest taste) and/or demographic structure; then $\beta=s/g$ follows
- Dynastic utility: rate or return r set by $u()$; if α set by technology, then $\beta = \alpha/r$ follows ($s=\alpha g/r$, so $\beta=\alpha/r=s/g$)
- With general utility functions, both s and r are jointly determined by $u()$ and technology

- **Two-good capital accumulation model:** one capital good, one consumption good
 - Define $1+q_t$ = real rate of capital gain (or capital loss)
= excess of asset price inflation over consumer price inflation
 - Then $\beta_{t+1} = \beta_t (1+g_{wt})(1+q_t)/(1+g_t)$
- With $1+g_{wt} = 1+s_t/\beta_t$ = saving-induced wealth growth rate
 $1+q_t$ = capital-gains-induced wealth growth rate

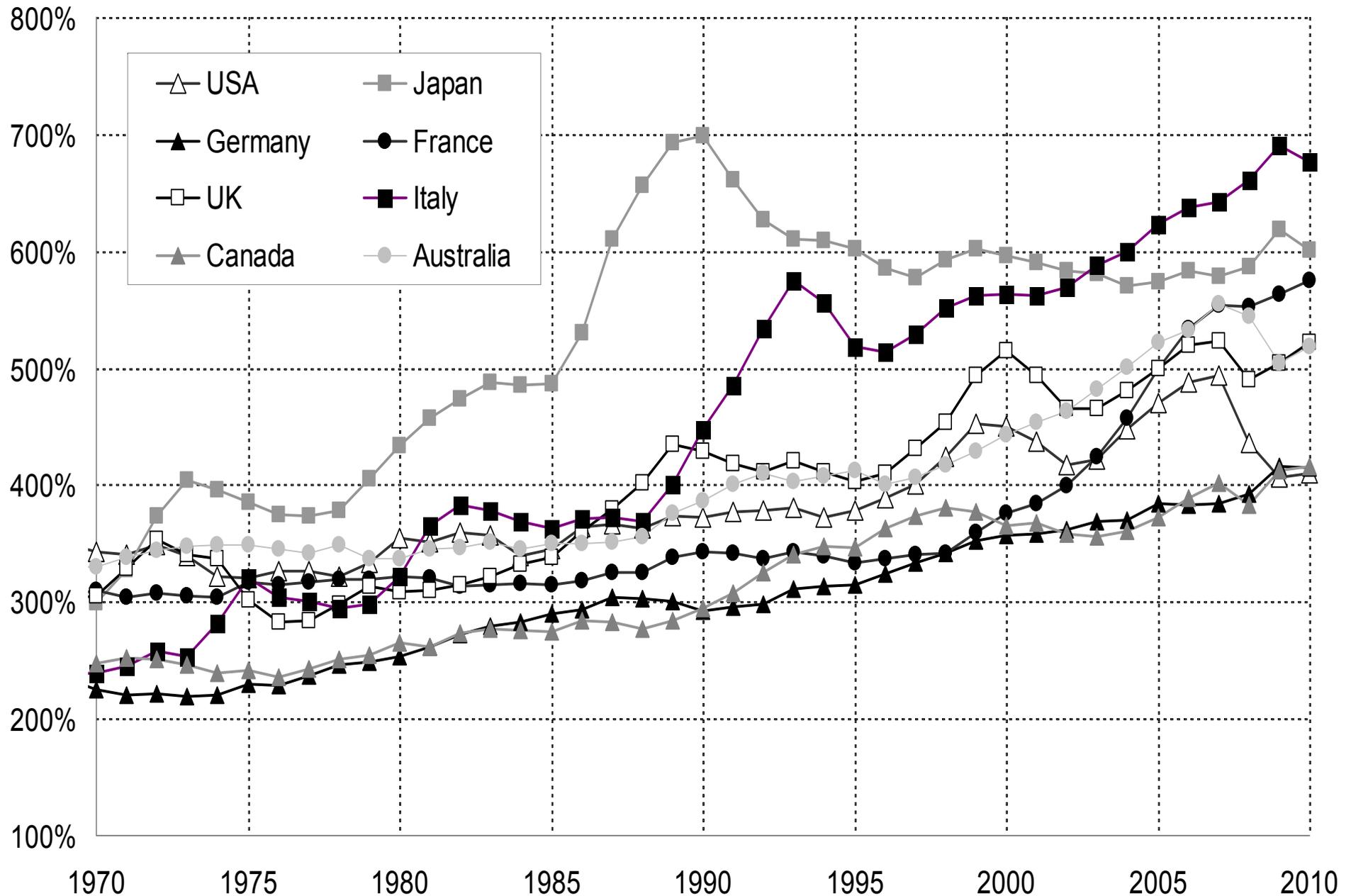
Our empirical strategy:

- we do not specify where q_t come from (maybe stochastic production functions to produce capital vs consumption good, with diff. rates of technical progress);
- we observe $\beta_t, \dots, \beta_{t+n}$, s_t, \dots, s_{t+n} , g_t, \dots, g_{t+n} , and we decompose the wealth accumulation equation between years t and $t+n$ into volume (saving) vs price effect (capital gain or loss)

Decomposition results: 1970-2010

- Annual series for top 8 rich countries, 1970-2010
 - Additive vs multiplicative decomposition of wealth accumulation equation into volume vs price effects
 - Private saving (personal + corporate) vs personal
 - Private wealth vs national wealth accumulation
 - Domestic capital vs foreign wealth accumulation
 - **Main conclusion:** capital gains account for a small part of the aggregate level of 2010 wealth accumulation (10%-20%), but for a significant part of the rise in wealth-income ratios between 1970 and 2010 (30%-50%+)
- we need to put 1970-2010 period into longer perspective

Private wealth / national income ratios, 1970-2010

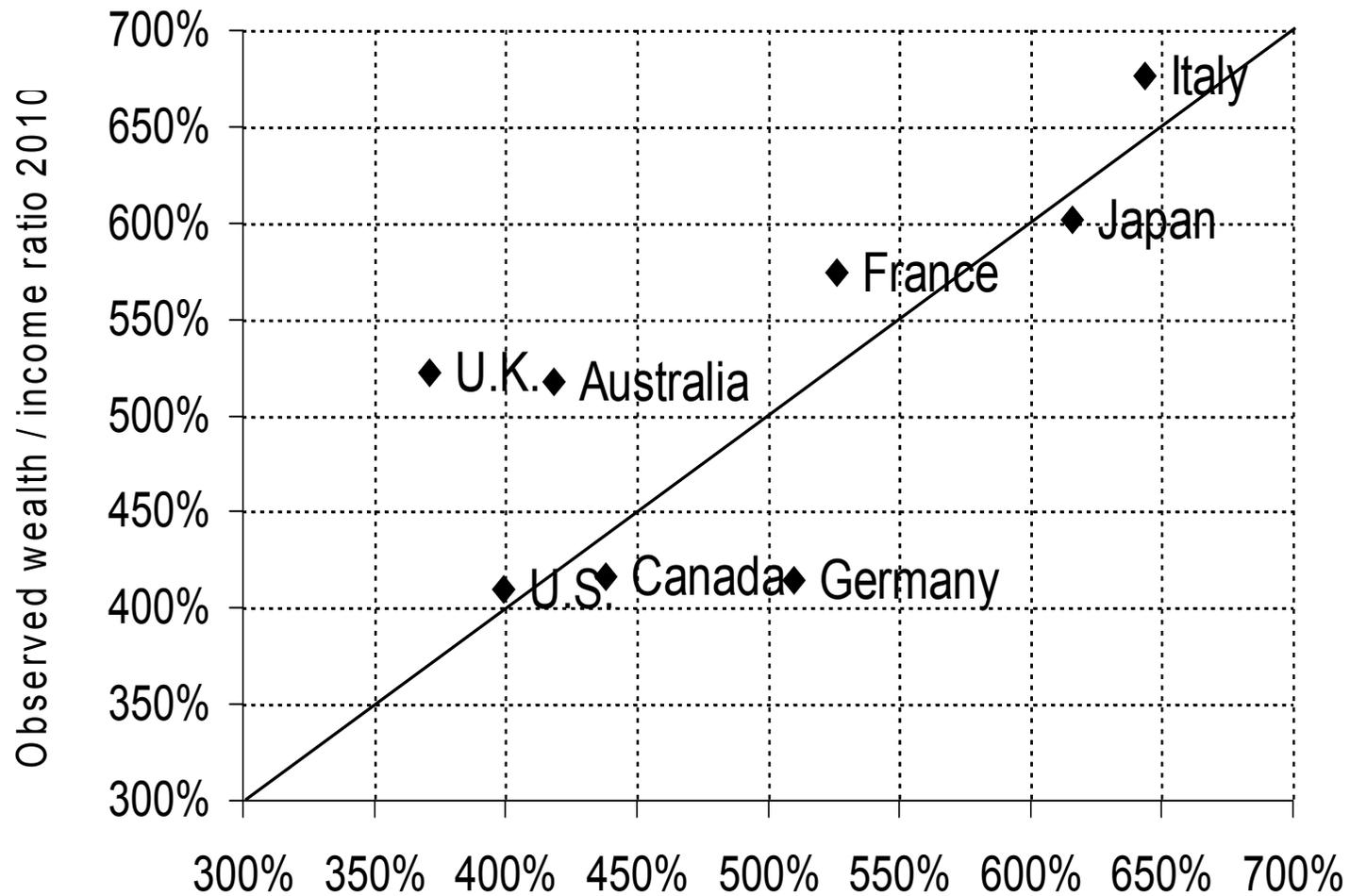


Authors' computations using country national accounts. Private wealth = non-financial assets + financial assets - financial liabilities (household & non-profit sectors)

Table 2: Growth rate vs private saving rate in rich countries, 1970-2010

	Real growth rate of national income	Population growth rate	Real growth rate of per capita national income	Net private saving rate (personal + corporate) (% national income)
U.S.	2.8%	1.0%	1.8%	7.7%
Japan	2.5%	0.5%	2.0%	14.6%
Germany	2.0%	0.2%	1.8%	12.2%
France	2.2%	0.5%	1.7%	11.1%
U.K.	2.2%	0.3%	1.9%	7.3%
Italy	1.9%	0.3%	1.6%	15.0%
Australia	3.2%	1.4%	1.7%	9.9%

Observed vs predicted private wealth / national income ratio (2010)



Predicted wealth / income ratio 2010 (on the basis of 1970 initial wealth and 1970-2010 cumulated saving flows) (additive decomposition, incl. R&D)

**Table 3: Accumulation of private wealth in rich countries, 1970-2010
(additive decomposition)**

	Private wealth-national income ratios		Decomposition of 2010 private wealth-national income ratio		
	β (1970)	β (2010)	Initial wealth effect	Cumulated new savings	Capital gains or losses
U.S.	342%	410%	113%	236%	60%
			28%	58%	15%
				80%	20%
Japan	299%	601%	110%	456%	35%
			18%	76%	6%
				93%	7%
Germany	225%	415%	104%	356%	-45%
			25%	86%	-11%
				115%	-15%
France	310%	575%	130%	346%	98%
			23%	60%	17%
				78%	22%
U.K.	306%	522%	128%	193%	201%
			25%	37%	39%
				49%	51%
Italy	239%	676%	114%	480%	83%
			17%	71%	12%
				85%	15%
Canada	247%	416%	80%	308%	28%
			19%	74%	7%
				92%	8%
Australia	330%	518%	94%	275%	149%
			18%	53%	29%
				65%	35%

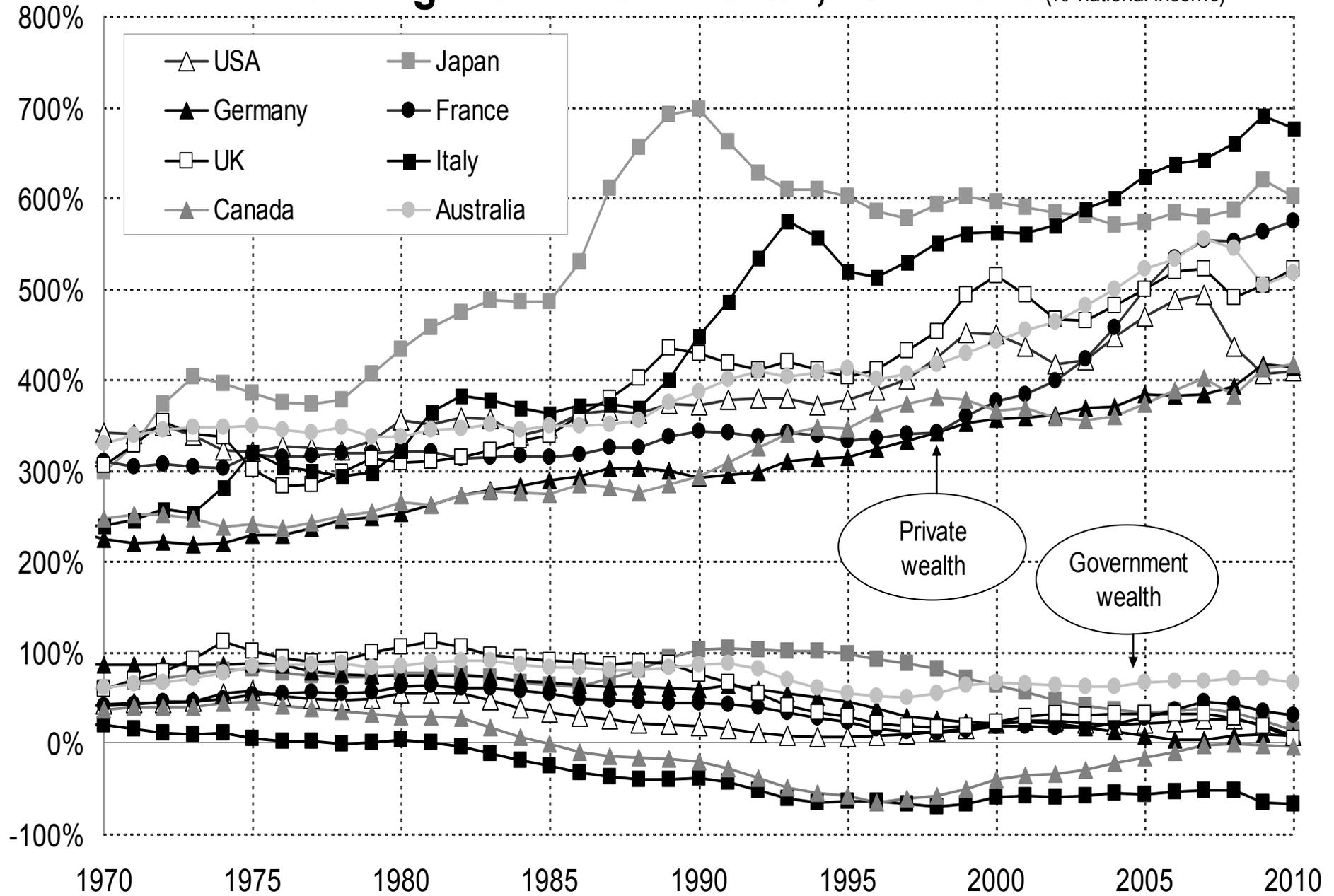
**Table 4: Accumulation of private wealth in rich countries, 1970-2010
(multiplicative decomposition)**

	Private wealth-national income ratios		Decomposition of 1970-2010 wealth growth rate		
			Real growth rate of private wealth	Savings- induced wealth growth rate	Capital-gains- induced wealth growth rate
	β (1970)	β (2010)	g_w	$g_{ws} = s/\beta$	q
U.S.	342%	410%	3.3%	2.9% 88%	0.4% 12%
Japan	299%	601%	4.3%	3.4% 78%	0.9% 22%
Germany	225%	415%	3.5%	4.3% 121%	-0.7% -21%
France	310%	575%	3.8%	3.4% 90%	0.4% 10%
U.K.	306%	522%	3.6%	1.9% 55%	1.6% 45%
Italy	239%	676%	4.6%	4.2% 92%	0.4% 8%
Canada	247%	416%	4.2%	4.3% 103%	-0.1% -3%
Australia	330%	518%	4.4%	3.4% 79%	0.9% 21%

Table 6: Private savings 1970-2010: personal vs corporate

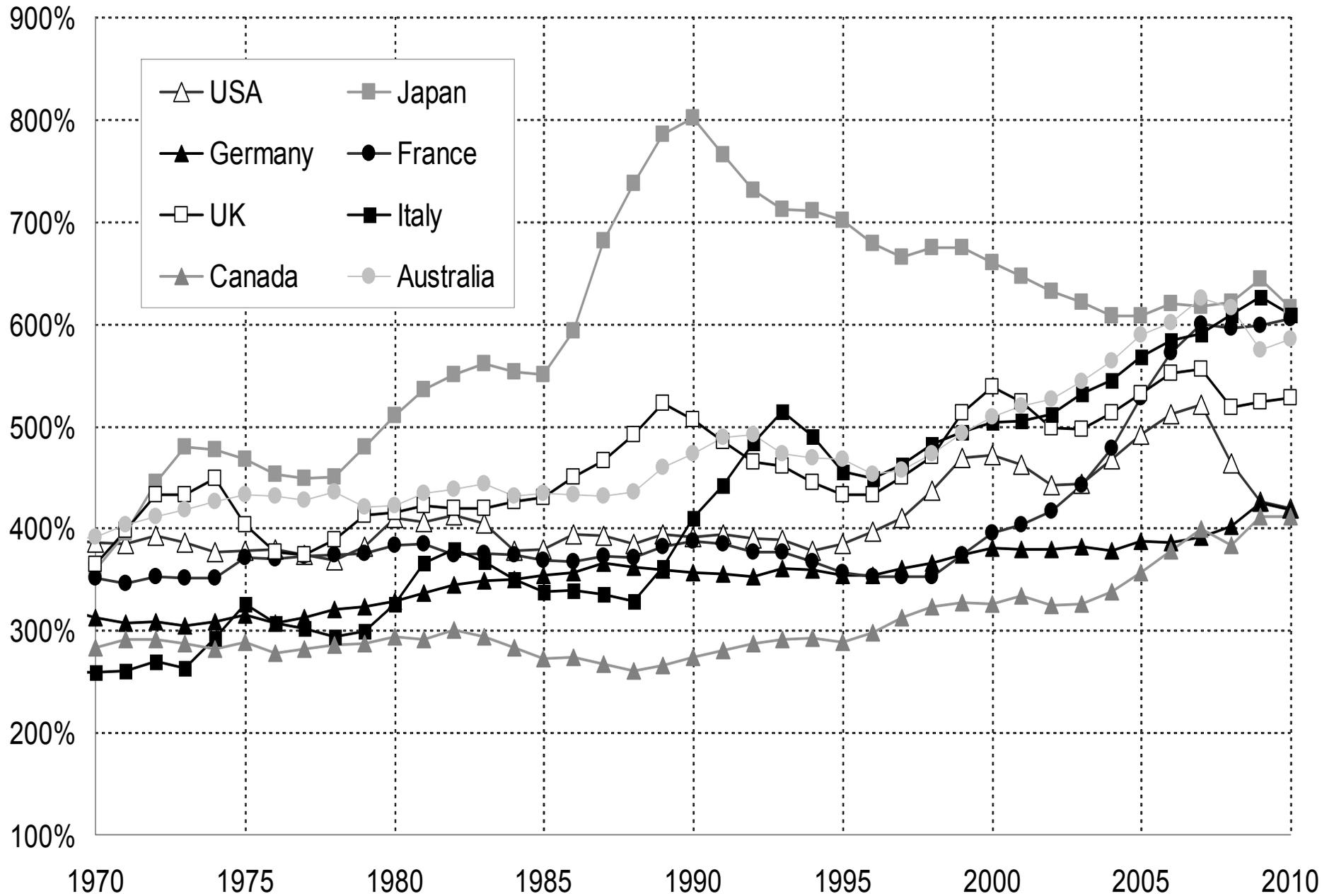
<i>Average saving rates 1970-2010 (% national income)</i>	Net private savings (personal + corporate)	incl. personal savings	incl. corporate savings (retained earnings)
U.S.	7.7%	4.6% 60%	3.1% 40%
Japan	14.6%	6.8% 47%	7.8% 53%
Germany	12.2%	9.4% 76%	2.9% 24%
France	11.1%	9.0% 81%	2.1% 19%
U.K.	7.3%	2.8% 38%	4.6% 62%
Italy	15.0%	14.6% 97%	0.4% 3%
Canada	12.1%	7.2% 60%	4.9% 40%
Australia	9.9%	5.9% 60%	3.9% 40%

Private vs government wealth, 1970-2010 (% national income)



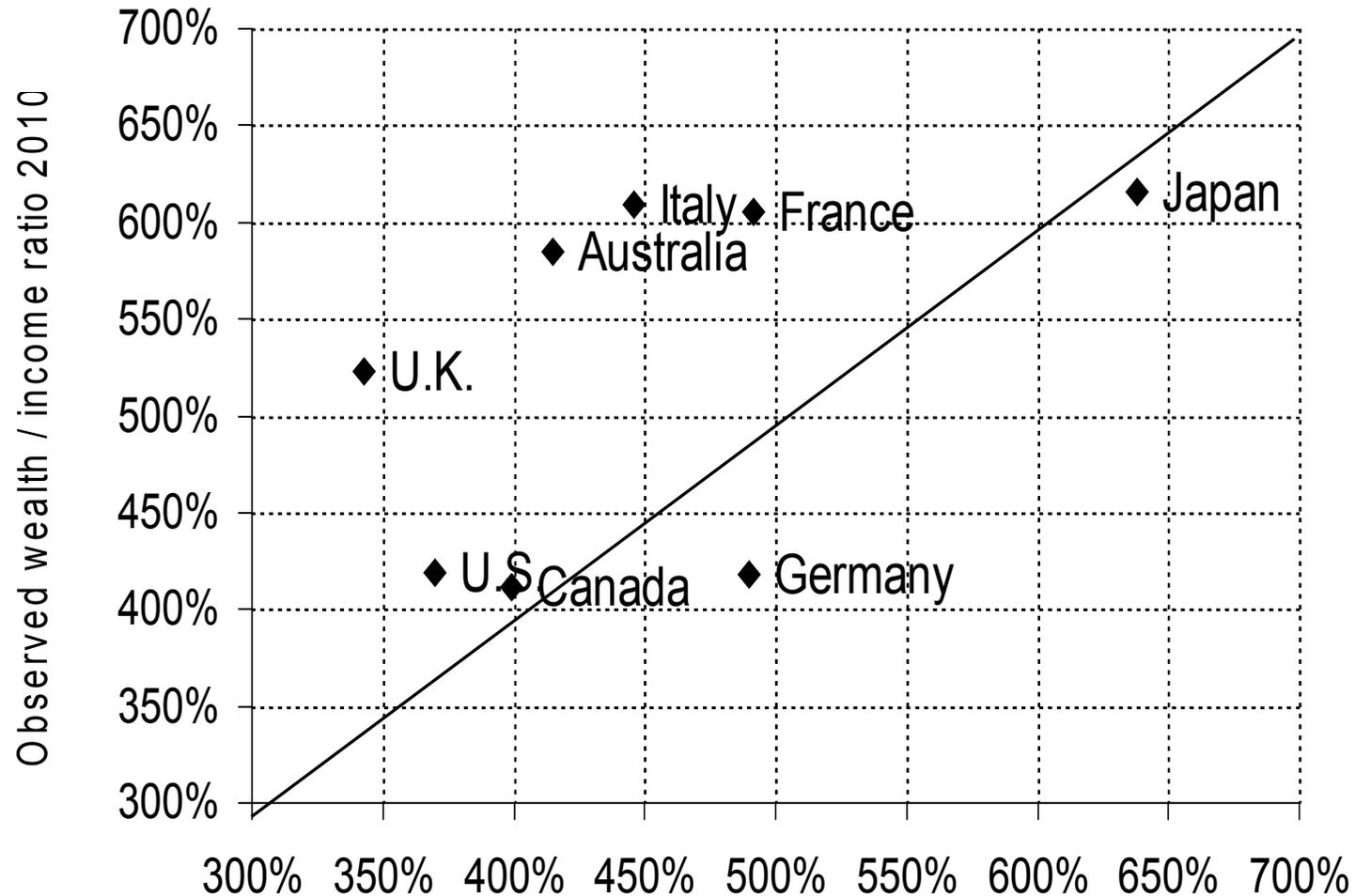
Authors' computations using country national accounts. Government wealth = non-financial assets + financial assets - financial liabilities (govt sector)

National wealth / national income ratios, 1970-2010



Authors' computations using country national accounts. National wealth = private wealth + government wealth

Observed vs predicted national wealth/national income ratio (2010)

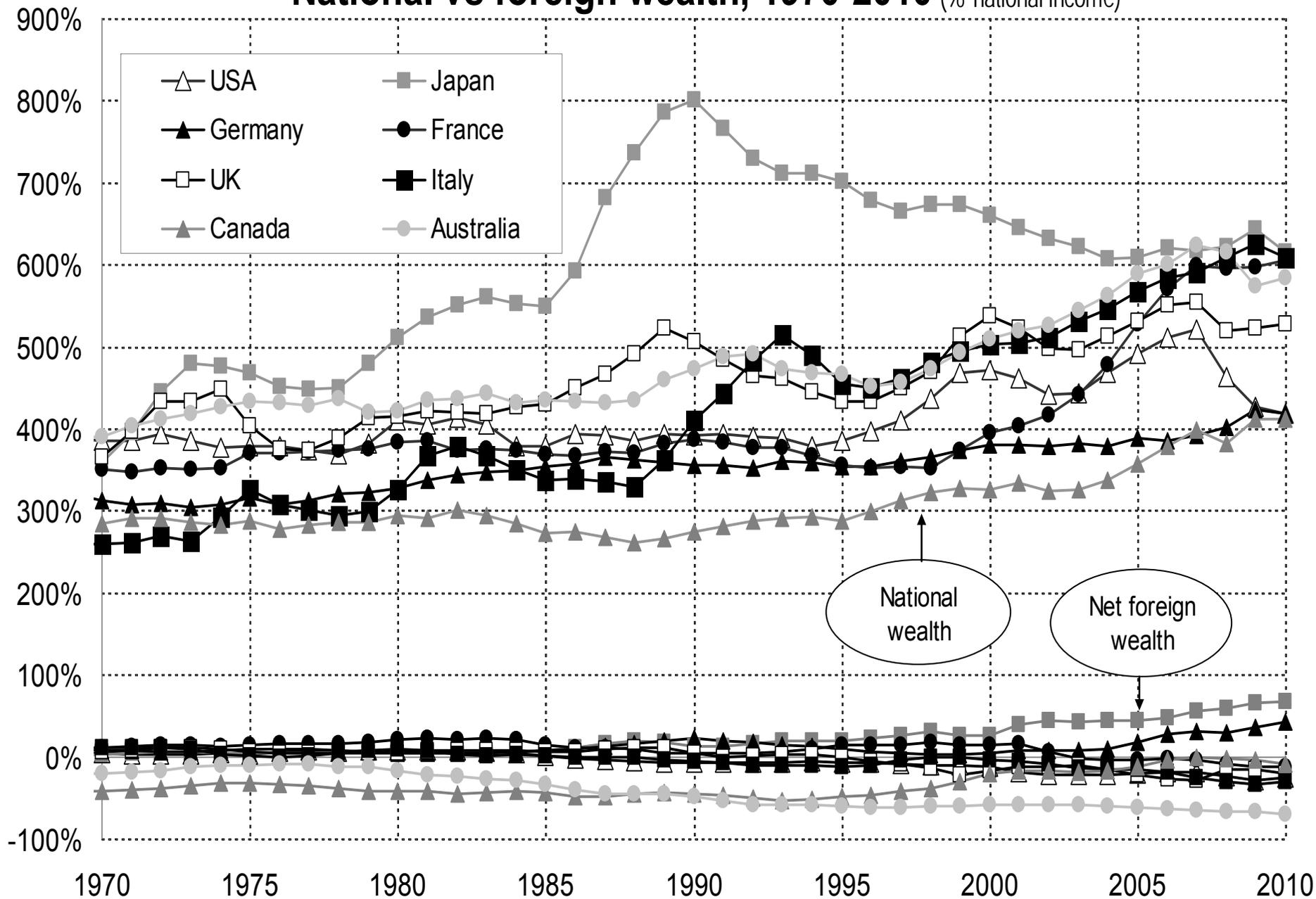


Predicted wealth / income ratio 2010 (on the basis of 1970 initial wealth and 1970-2010 cumulated saving flows) (additive decomposition, incl. R&D)

Table 9: National saving 1970-2010: private vs government

<i>Average saving rates 1970-2010 (% national income)</i>	Net national saving (private + government)	incl. private saving	incl. government saving
U.S.	5.2%	7.7%	-2.4%
Japan	14.6%	14.6%	0.0%
Germany	10.2%	12.2%	-2.1%
France	9.2%	11.1%	-1.9%
U.K.	5.3%	7.3%	-2.0%
Italy	8.5%	15.0%	-6.5%
Canada	10.1%	12.1%	-2.0%
Australia	8.9%	9.9%	-0.9%

National vs foreign wealth, 1970-2010 (% national income)

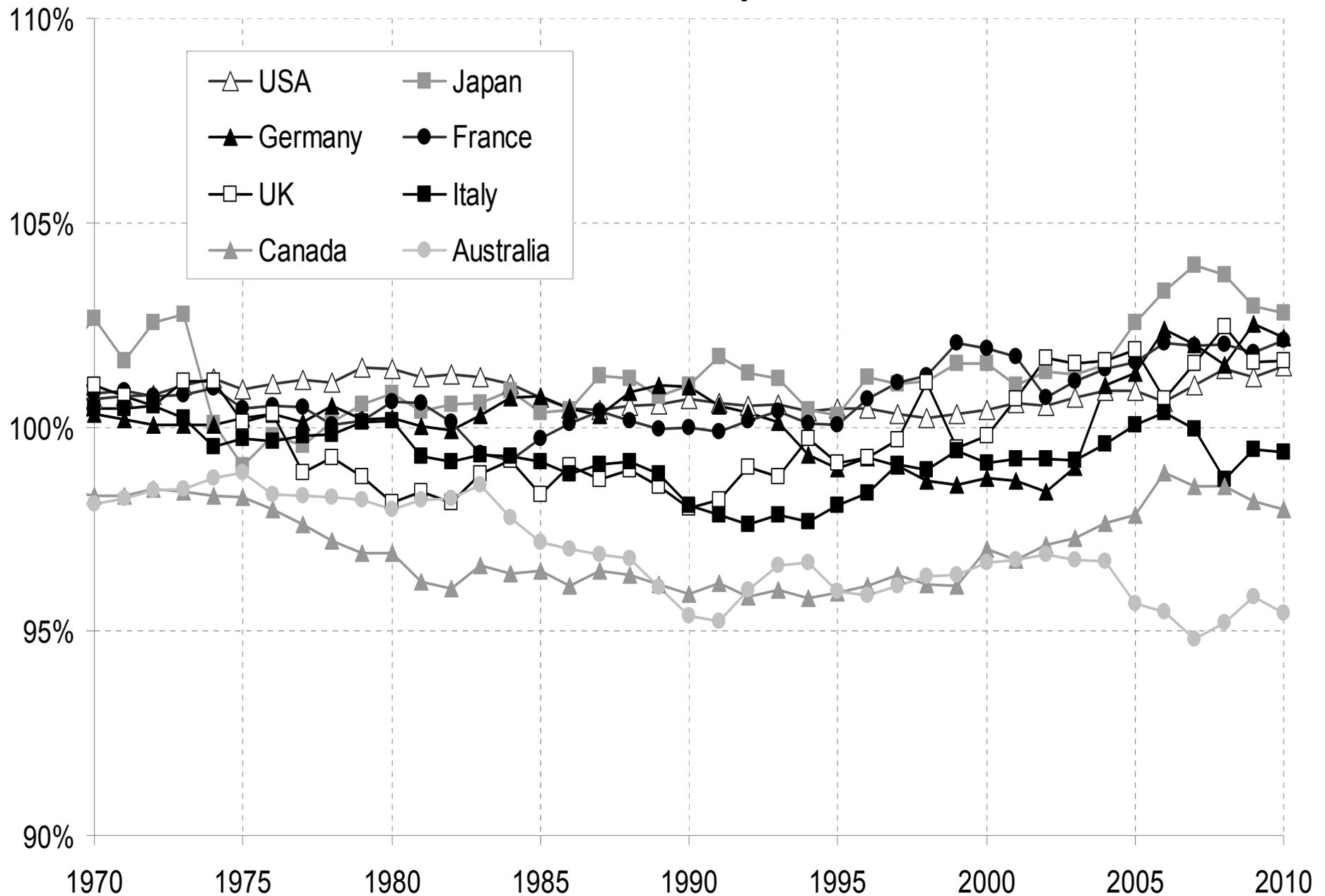


Authors' computations using country national accounts. Net foreign wealth = net foreign assets owned by country residents in rest of the world (all sectors)

**Table 12: National wealth accumulation in rich countries, 1970-2010:
domestic capital vs foreign wealth**

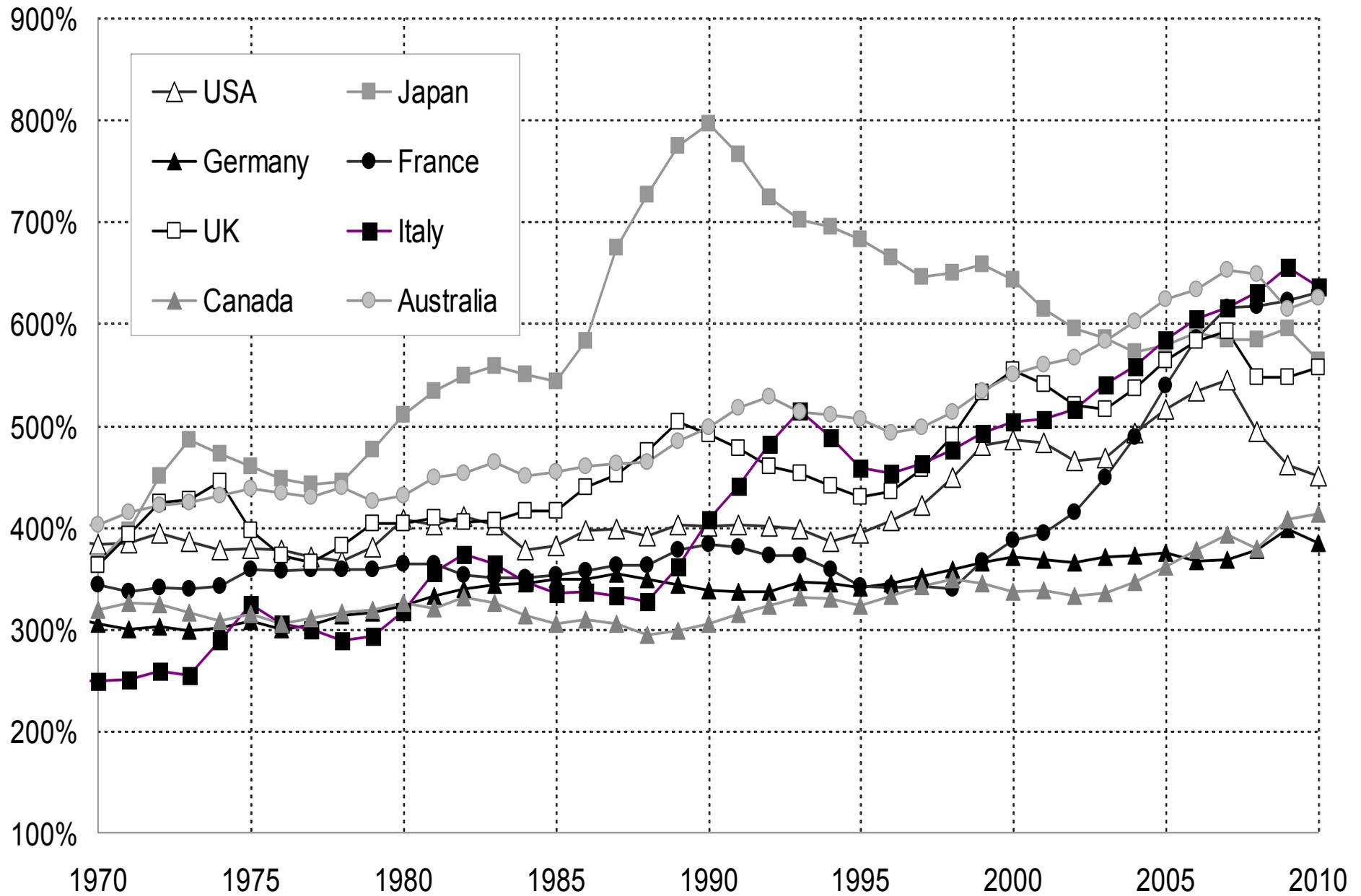
	National wealth / national income ratio (1970)		National wealth / national income ratio (2010)		Rise in national wealth / national income ratio (1970-2010)	
	<i>incl. Domestic capital</i>	<i>incl. Foreign wealth</i>	<i>incl. Domestic capital</i>	<i>incl. Foreign wealth</i>	<i>incl. Domestic capital</i>	<i>incl. Foreign wealth</i>
U.S.	385%		419%		33%	
	381%	4%	444%	-25%	63%	-30%
Japan	359%		616%		256%	
	356%	3%	548%	67%	192%	64%
Germany	312%		418%		106%	
	304%	8%	376%	42%	72%	34%
France	351%		605%		254%	
	340%	11%	618%	-13%	278%	-24%
U.K.	365%		527%		163%	
	359%	6%	548%	-20%	189%	-26%
Italy	259%		609%		350%	
	247%	12%	640%	-31%	392%	-42%
Canada	284%		412%		128%	
	325%	-41%	422%	-10%	97%	31%
Australia	391%		584%		194%	
	410%	-20%	655%	-70%	244%	-50%

National income / domestic product ratios, 1970-2010



Authors' computations using country national accounts. National income = domestic product + net foreign income

Domestic capital / output ratios, 1970-2010



Authors' computations using country national accounts. Domestic capital/output ratio = (national wealth - foreign wealth)/domestic product

**Table 16: Domestic capital accumulation in rich countries, 1970-2010:
housing vs other domestic capital**

	Domestic capital / national income ratio (1970)		Domestic capital / national income ratio (2010)		Rise in domestic capital / national income ratio (1970-2010)	
	<i>incl. Housing</i>	<i>incl. Other domestic capital</i>	<i>incl. Housing</i>	<i>incl. Other domestic capital</i>	<i>incl. Housing</i>	<i>incl. Other domestic capital</i>
U.S.	381%		444%		63%	
	142%	239%	182%	262%	41%	23%
Japan	356%		548%		192%	
	131%	225%	220%	328%	89%	103%
Germany	304%		376%		72%	
	129%	175%	241%	135%	112%	-40%
France	340%		618%		278%	
	104%	236%	371%	247%	267%	11%
U.K.	359%		548%		189%	
	98%	261%	300%	248%	202%	-13%
Italy	247%		640%		392%	
	107%	141%	386%	254%	279%	113%
Canada	325%		422%		97%	
	108%	217%	208%	213%	101%	-4%
Australia	410%		655%		244%	
	172%	239%	364%	291%	193%	52%

Decomposition results: 1870-2010

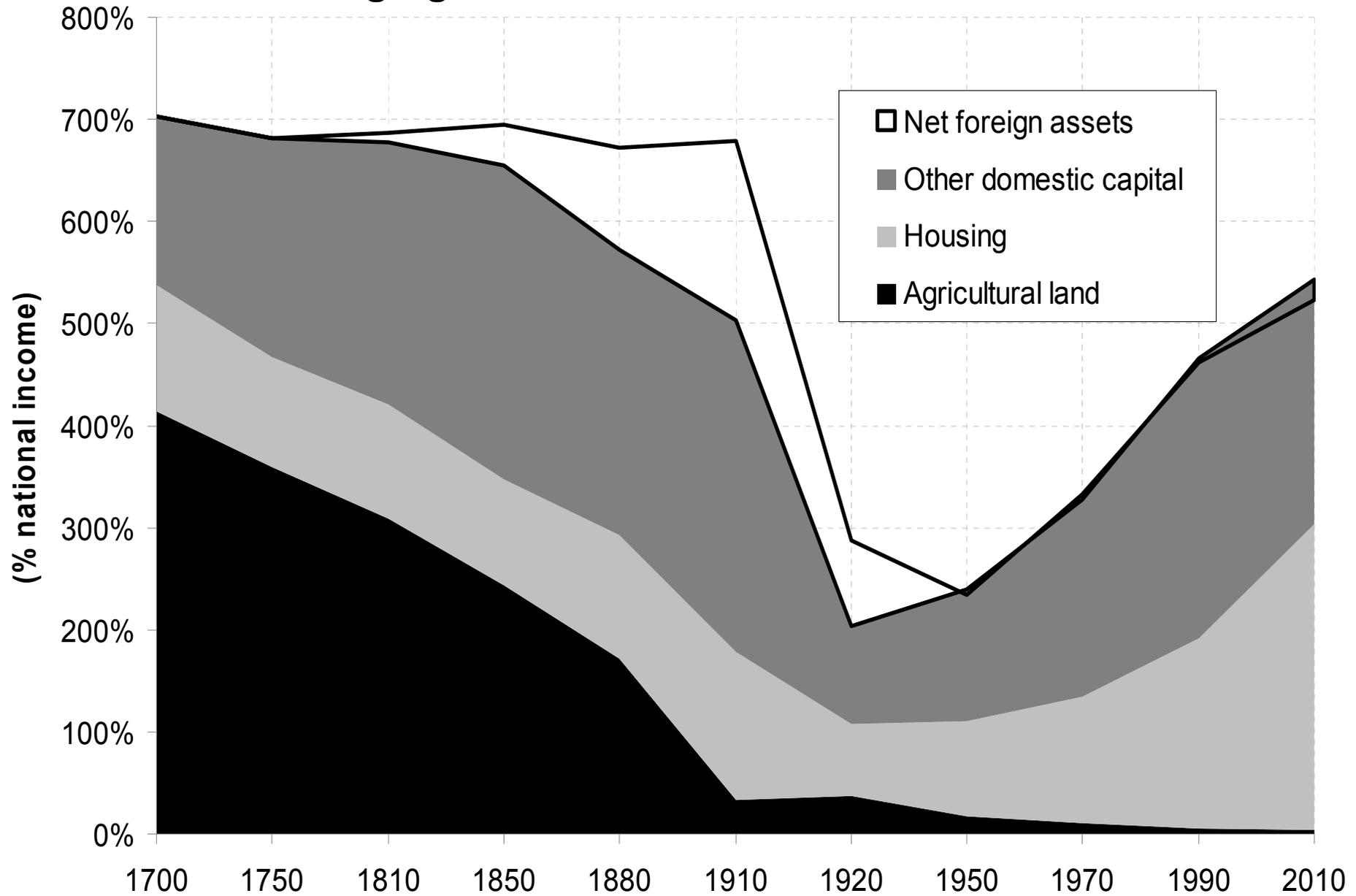
- Annual series for US, Germany, France, UK, 1870-2010
- Additive vs multiplicative decomposition of wealth accumulation equation into volume vs price effects
- Private saving (personal + corporate) vs personal
- Private wealth vs national wealth accumulation
- Domestic vs foreign wealth accumulation

- **Main conclusion:** over the entire 1910-2010 period, capital gains wash out; i.e. 1910-1950 fall in relative asset price compensated by 1950-2010 (except in Germany, where asset prices seem abnormally low: stakeholder effect?)
- In the long run (1870-2010 or 1910-2010), changes in wealth-income ratios are well accounted for by $\beta = s/g$

Very long run results: 1700-2010

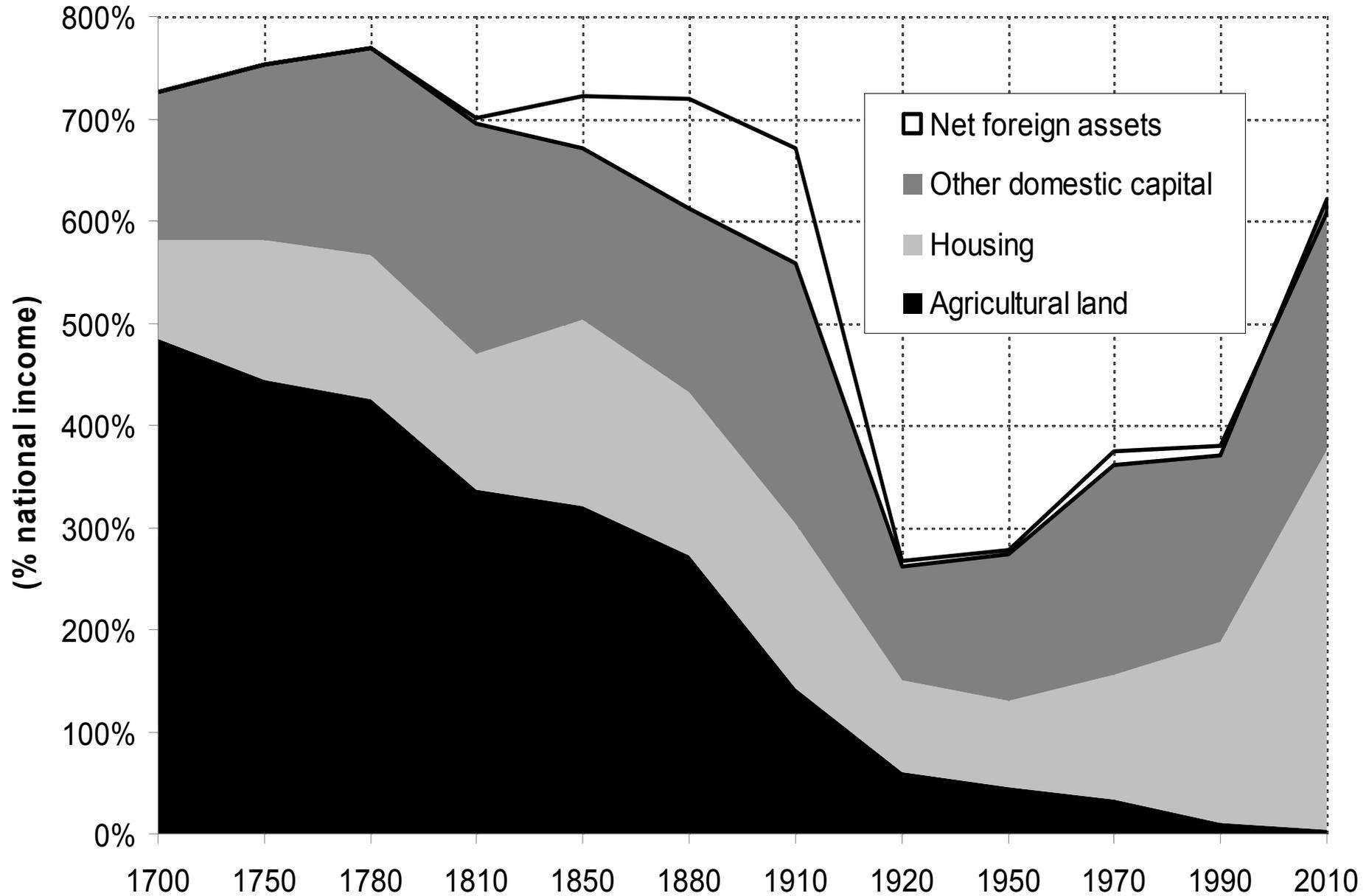
- For the UK and France, there are national balance sheets estimates starting around 1700-1750 (and for the US, starting around 1770-1800)
- These estimates are less precise than post-1870 series; in particular one cannot properly identify volume vs price effects in wealth accumulation equations: saving and investment series are too approximate, and with g very small (typically 1% or less), any small change in s generates huge changes in $\beta = s/g$
- However it is still interesting to use these estimates, because they reveal interesting patterns about the changing nature of wealth and technology in the very long run
- **Main conclusion:** In the very long run, we find β relatively stable around 600%-700% in UK & France, in spite of huge changes in wealth composition, from agricultural land to manufacturing capital and housing

The changing nature of national wealth, UK 1700-2010



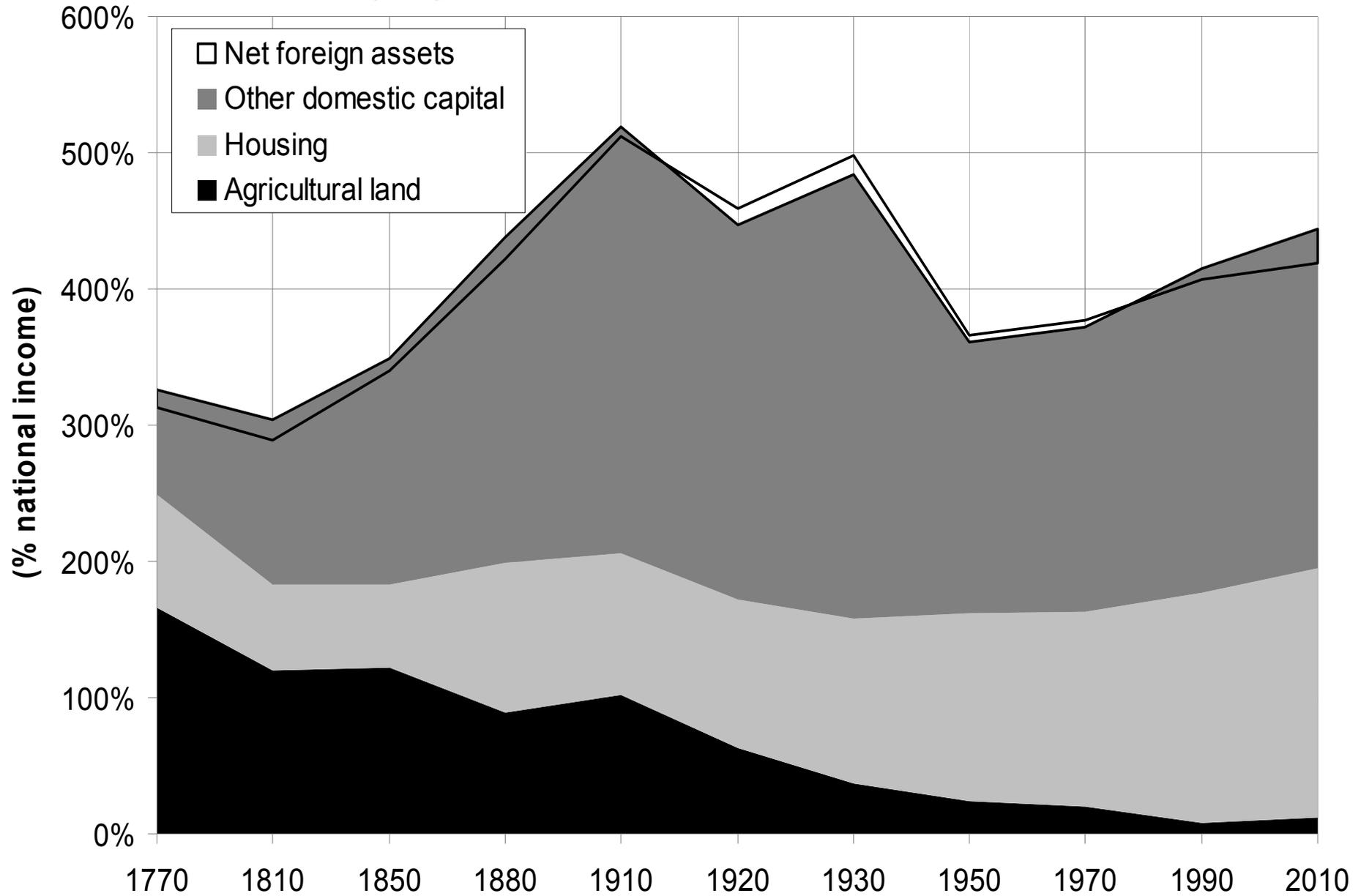
National wealth = agricultural land + housing + other domestic capital goods + net foreign assets

The changing nature of national wealth, France 1700-2010



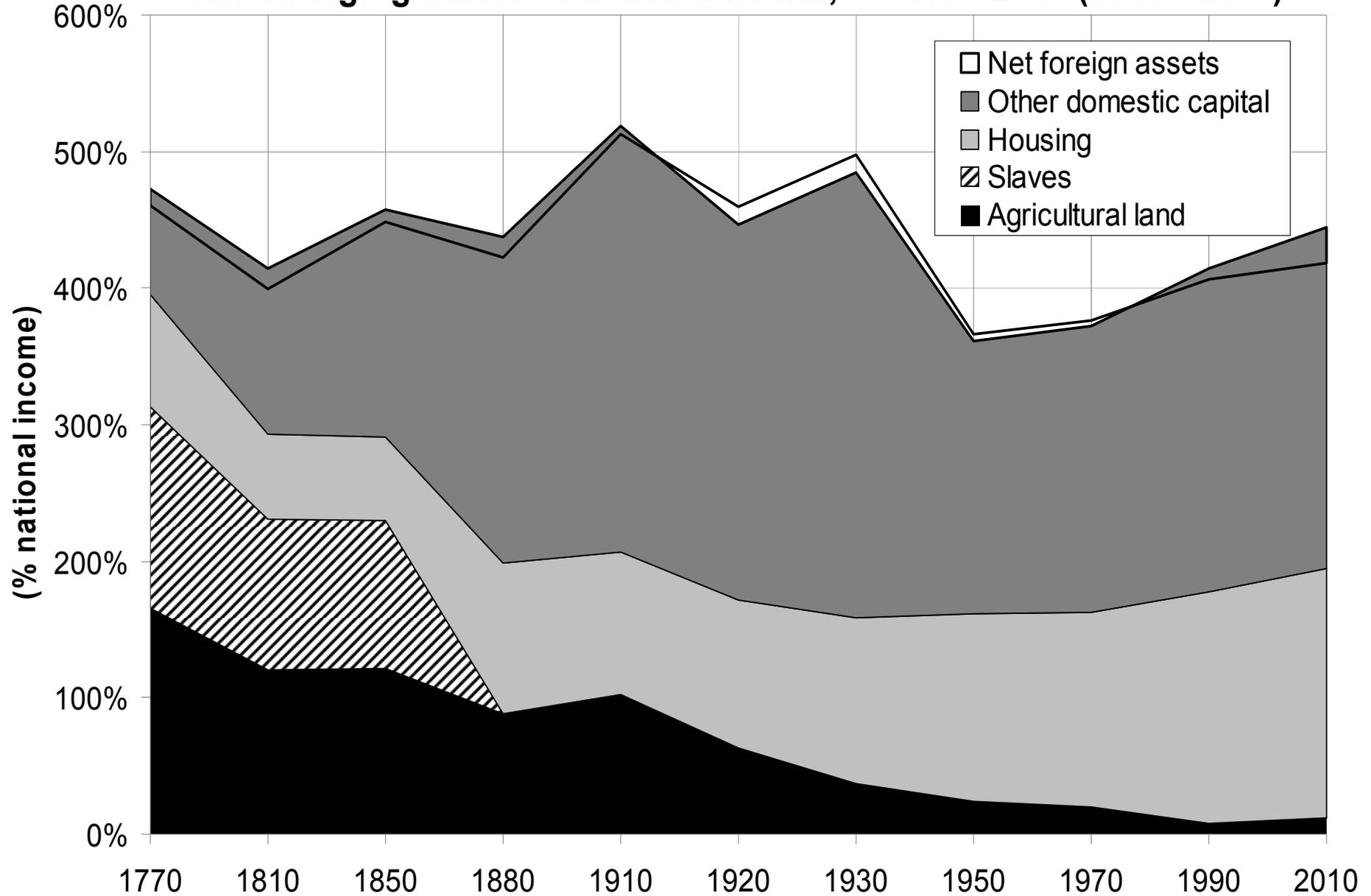
National wealth = agricultural land + housing + other domestic capital goods + net foreign assets

The changing nature of national wealth, US 1770-2010



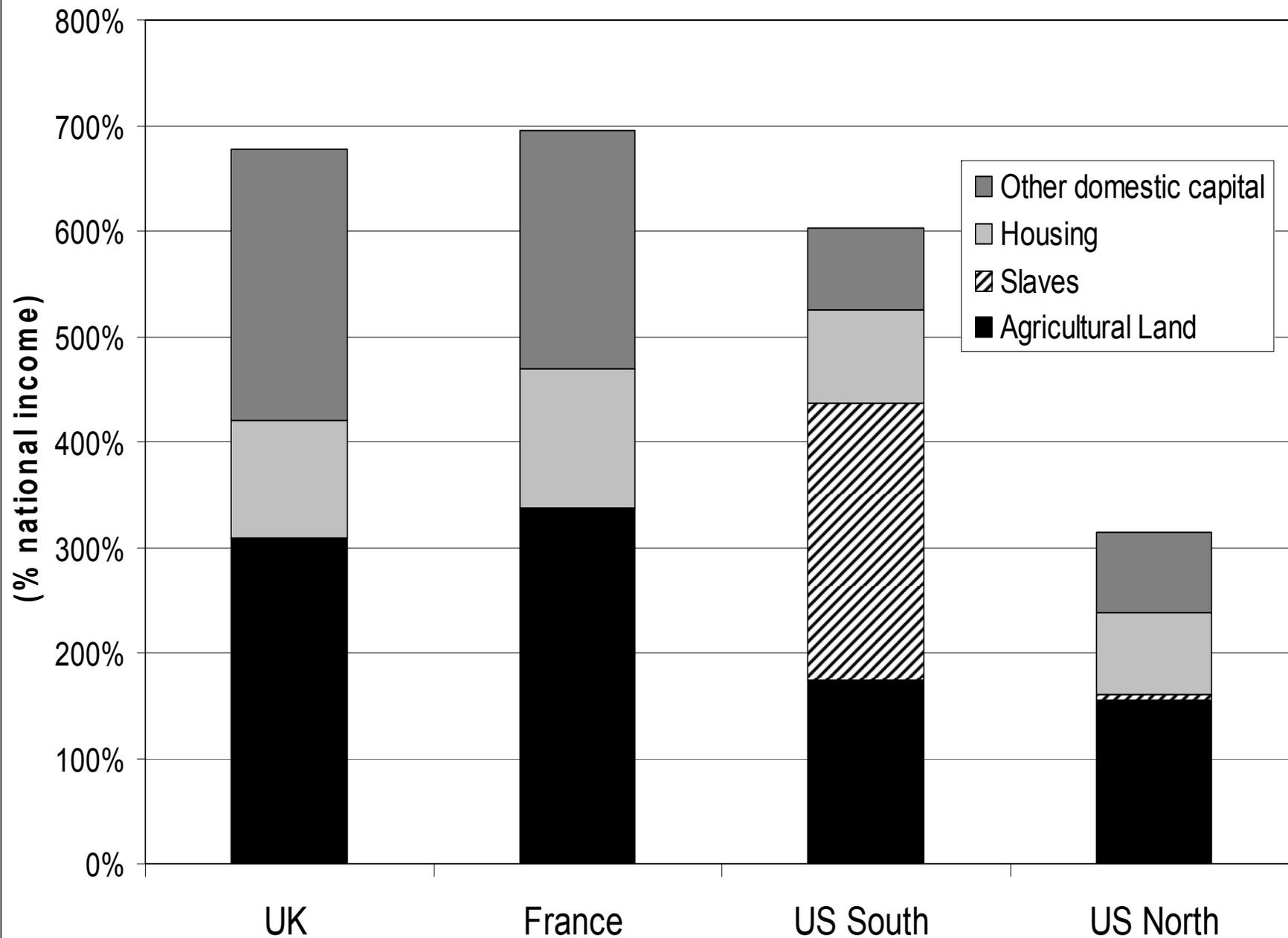
National wealth = agricultural land + housing + other domestic capital goods + net foreign assets

The changing nature of national wealth, US 1770-2010 (incl. slaves)

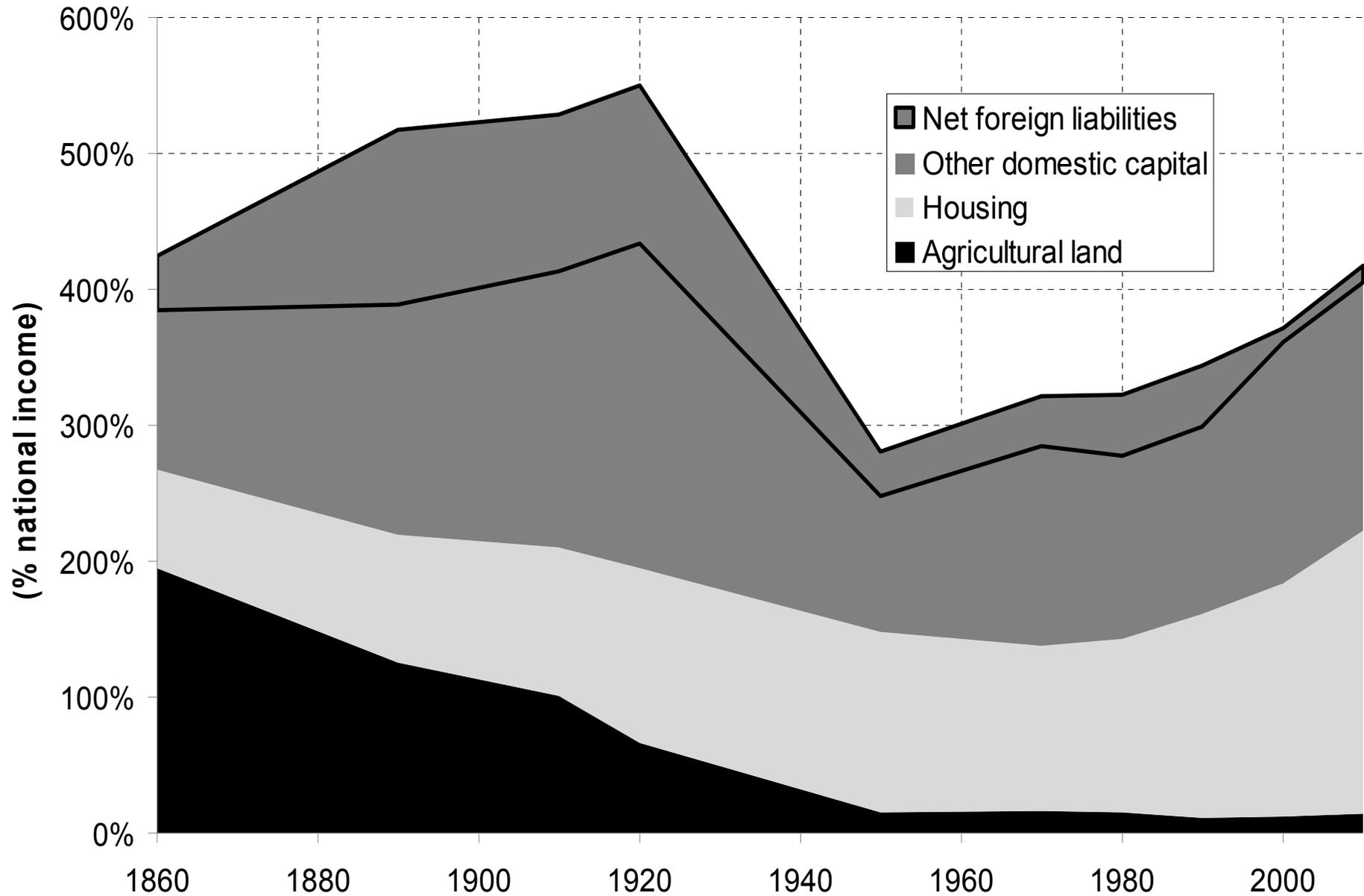


National wealth = agricultural land + housing + other domestic capital goods + net foreign assets

National wealth in 1770-1810: Old vs New world



The changing nature of national wealth, Canada 1860-2010



National wealth = agricultural land + housing + other domestic capital - net foreign liabilities

- **Why is β** stable around 600%-700% in the very long run in UK & France?
- In agrarian, very-low-growth societies, it is unclear which forces dominate: $\beta = s/g$ or $\beta = \alpha/r$? Probably $\beta = \alpha/r$
- I.e. with α = capital share = mostly land rent: determined by technology, politics, & land availability ($\alpha \approx 30\%$ - 40% in Europe, vs 10% - 15% in land-rich New world, i.e. elasticity of substitution $\sigma < 1$), and r = rate of return = 4% - 5% = rate of time preference
 → $\beta = 600\%$ - 700% in Europe, vs 200% - 300% in New World

(simply because very abundant land is worthless: new world had more land in volume, but less land in value)

(nothing to do with the $\beta = s/g$ mechanism, which bumped it in later, with migration)

- **Capital is back:** the low wealth-income ratios observed in Europe in 1950s-1970s (200%-300%) were an anomaly; with low growth, long run wealth-income ratios are naturally very large (600%-700%); key is $\beta = s/g$
- There's nothing bad about the return of capital: k is useful; but it raises new issues about k regulation & taxation
- National accounts used to be mostly about flows; we now need to focus on stocks
- Next steps: **Dynamics of world distribution of wealth:** Will China or global billionaires own the world? Both divergence can occur, but 2nd one more likely, esp. if $r > g$
- **Inherited vs self-made wealth:** long-run U-shaped pattern in France; on-going work on UK, Germany & US

2b. The return of inherited wealth

- In principle, one could very well observe a return of wealth without a return of inherited wealth
- I.e. it could be that the rise of aggregate wealth-income ratio is due mostly to the rise of life-cycle wealth (pension funds)
- Modigliani life-cycle theory: people save for their old days and die with zero wealth, so that inheritance flows are small
- However the Modigliani story happens to be wrong (except in the 50s-60s, when there's not much left to inherit...)
- Inheritance flow-private income ratio $B/Y = \mu m W/Y$
(with m = mortality rate, μ = relative wealth of decedents)
- B/Y has almost returned to 1910 level, both because of W/Y and because of μ : with g low & $r > g$, $B/Y \rightarrow \beta/H$
→ with $\beta=600\%$ & H =generation length=30 years, then $B/Y \approx 20\%$, i.e. annual inheritance flow $\approx 20\%$ national income

Figure 1: Annual inheritance flow as a fraction of national income, France 1820-2008

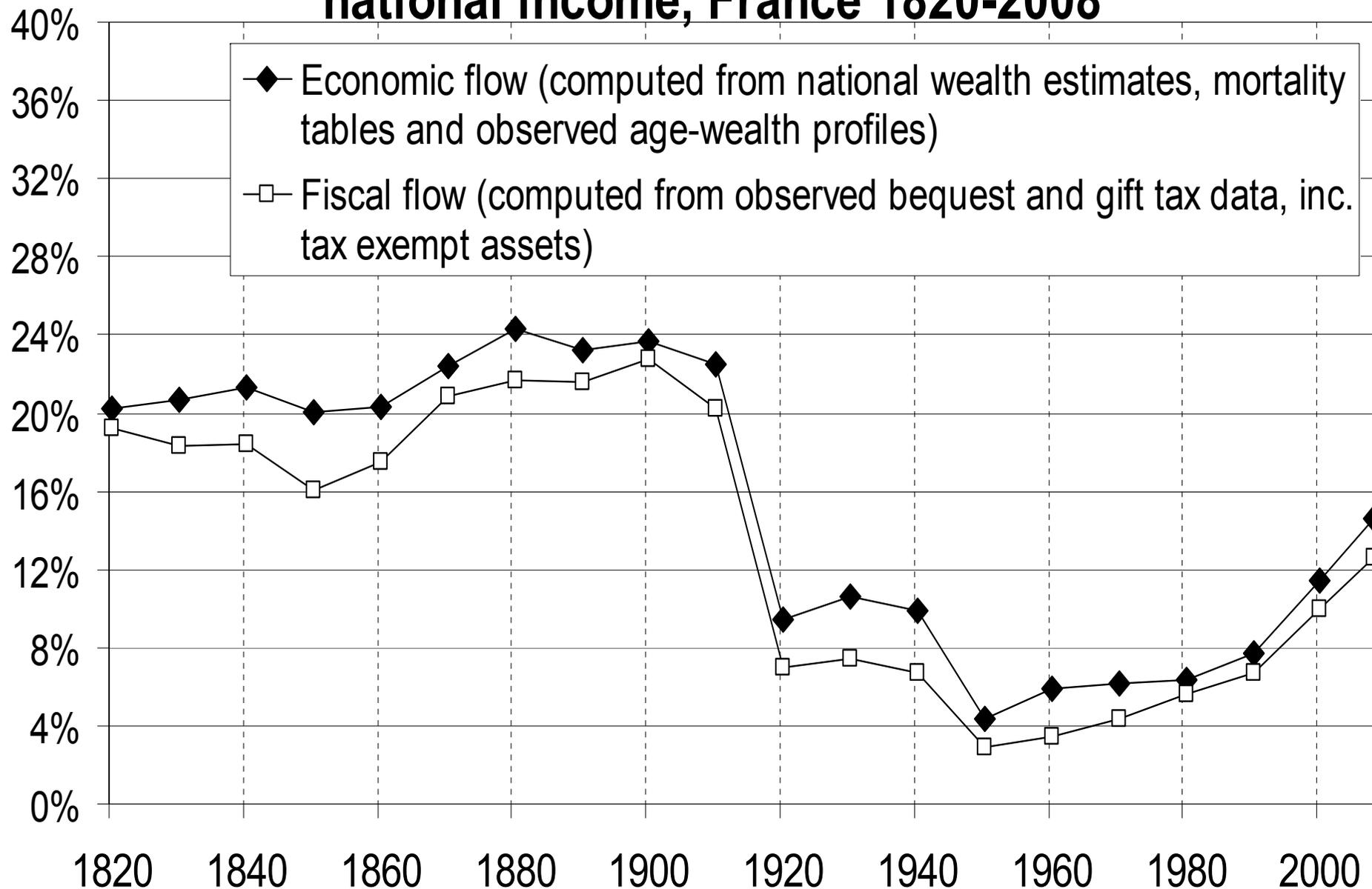
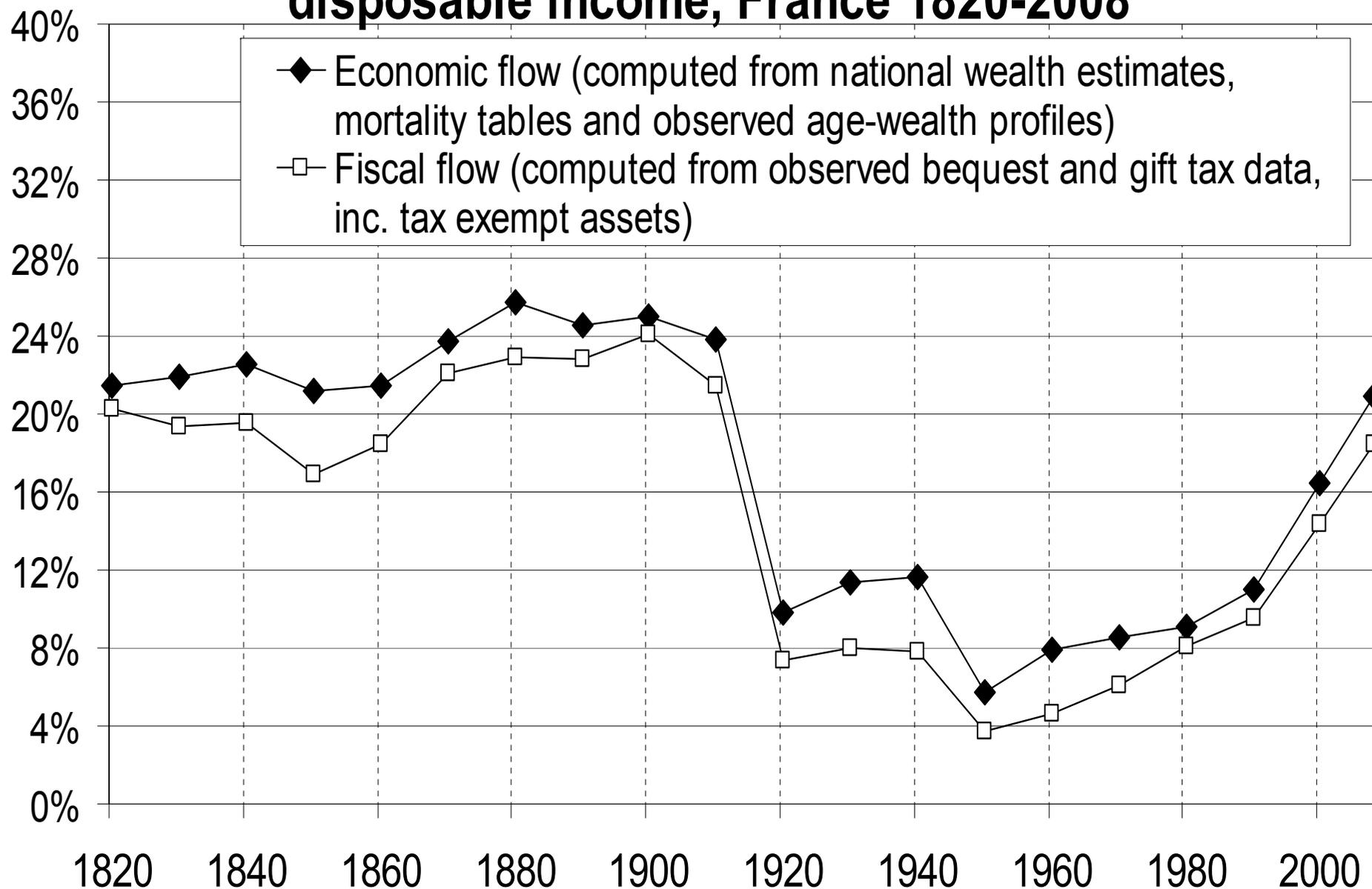


Figure 2: Annual inheritance flow as a fraction of disposable income, France 1820-2008



- An annual inheritance flow around 20%-25% of disposable income is a very large flow
- E.g. it is much larger than the annual flow of new savings (typically around 10%-15% of disposable income), which itself comes in part from the return to inheritance (it's easier to save if you have inherited your house & have no rent to pay)
- An annual inheritance flow around 20%-25% of disposable income means that total, cumulated inherited wealth represents the vast majority of aggregate wealth (typically above 80%-90% of aggregate wealth), and vastly dominates self-made wealth

- **Main lesson: with $r > g$, inheritance is bound to dominate new wealth; the past eats up the future**

Note: r = rate of return to capital = (net profits + rents)/(net financial + real estate wealth) ; g = growth rate ($g+n$)

- **Intuition:** with $r > g$ & g low (say $r=4\%-5\%$ vs $g=1\%-2\%$), wealth coming from the past is being capitalized faster than growth; heirs just need to save a fraction g/r of the return to inherited wealth $\rightarrow b_y = \beta/H$ (with $\beta = W/Y$)
 \rightarrow with $\beta=600\%$ & $H=30$, then $b_y=20\%$
- It is only in countries & time periods with g exceptionally high that self-made wealth dominates inherited wealth (OECD in 1950s-70s or China today)
- $r > g$ also has an amplifying effect on wealth inequality

Table 3: Intra-cohort distributions of labor income and inheritance, France, 1910 vs 2010

Shares in aggregate labor income or inherited wealth	Labor income 1910-2010	Inherited wealth	
		1910	2010
Top 10% "Upper Class"	30%	90%	60%
<i>incl. Top 1% "Very Rich"</i>	<i>6%</i>	<i>50%</i>	<i>25%</i>
<i>incl. Other 9% "Rich"</i>	<i>24%</i>	<i>40%</i>	<i>35%</i>
Middle 40% "Middle Class"	40%	5%	35%
Bottom 50% "Poor"	30%	5%	5%

2c. Implications for optimal capital taxation

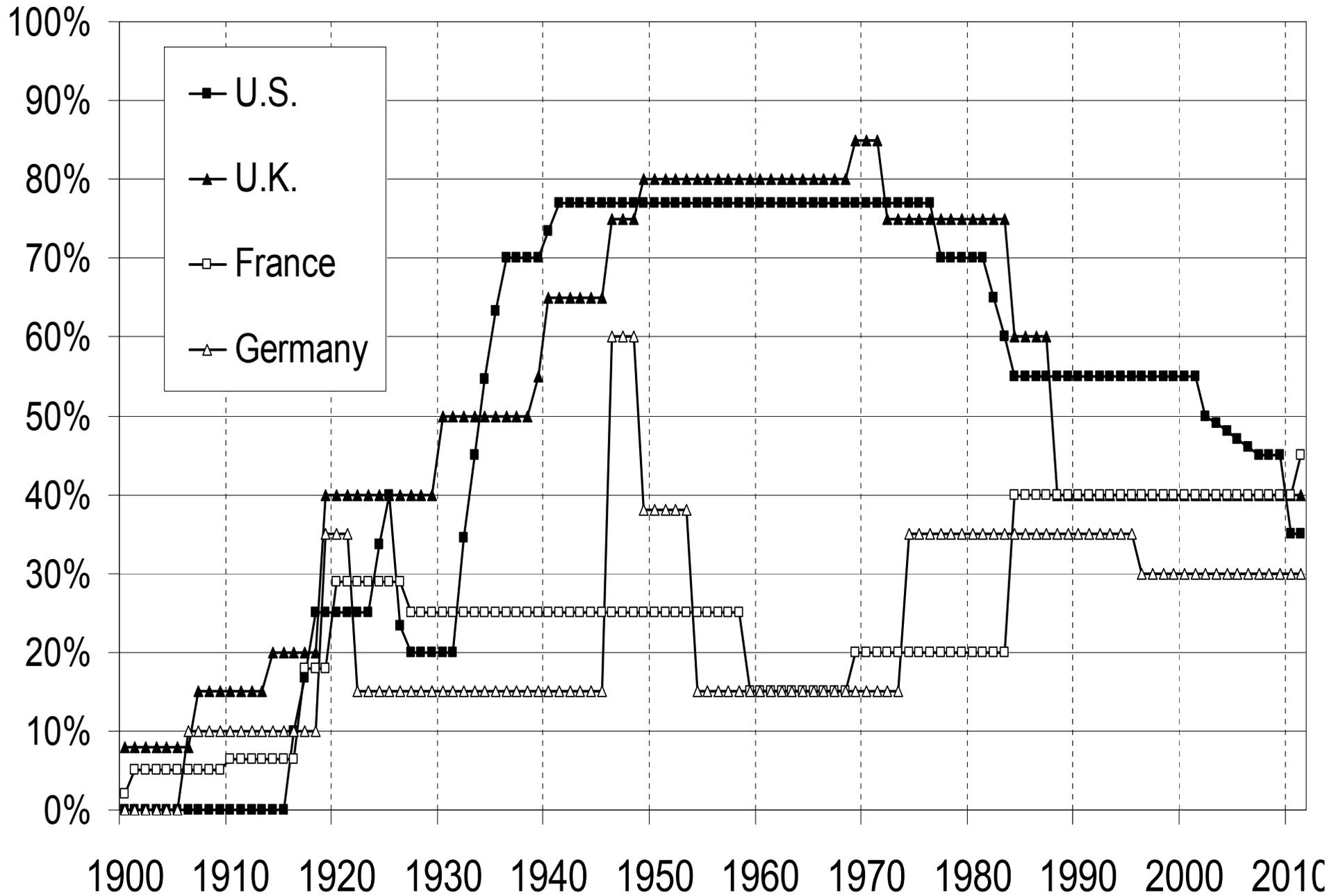
- Main results from Piketty-Saez, « A Theory of Optimal Capital Taxation »
- **Result 1: Optimal Inheritance Tax Formula**
- Simple formula for optimal bequest tax rate expressed in terms of estimable parameters:

$$\tau_B = \frac{1 - (1 - \alpha - \tau) s_{b0} / b_y}{1 + e_B + s_{b0}}$$

with: b_y = bequest flow, e_B = elasticity, s_{b0} = bequest taste
→ τ_B increases with b_y and decreases with e_B and s_{b0}

- For realistic parameters: $\tau_B = 50-60\%$ (or more..or less...)
→ **our theory can account for the variety of observed top bequest tax rates (30%-80%)**

Top Inheritance Tax Rates 1900-2011



- **Result 2: Optimal Capital Tax Mix**
 - **K market imperfections** (e.g. uninsurable idiosyncratic shocks to rates of return) can justify shifting one-off inheritance taxation toward lifetime capital taxation (property tax, K income tax,..)
 - **Intuition:** what matters is capitalized bequest, not raw bequest; but at the time of setting the bequest tax rate, there is a lot of uncertainty about what the rate of return is going to be during the next 30 years → so it is more efficient to split the tax burden
- **our theory can explain the actual structure & mix of inheritance vs lifetime capital taxation**
(& why high top inheritance and top capital income tax rates often come together, e.g. US-UK 1930s-1980s)

- Meritocratic rawlsian optimum, i.e. social optimum from the viewpoint of zero bequest receivers ($z=0$):

Proposition (zero-receivers tax optimum)

$$\tau_B = \frac{1 - (1 - \alpha - \tau) s_{b0} / b_y}{1 + e_B + s_{b0}}$$

with: s_{b0} = average bequest taste of zero receivers

- τ_B increases with b_y and decreases with e_B and s_{b0}
- If bequest taste $s_{b0}=0$, then $\tau_B = 1/(1+e_B)$
→ standard revenue-maximizing formula
- If $e_B \rightarrow +\infty$, then $\tau_B \rightarrow 0$: back to Chamley-Judd
- If $e_B=0$, then $\tau_B < 1$ as long as $s_{b0} > 0$
- I.e. zero receivers do not want to tax bequests at 100%, because they themselves want to leave bequests
→ **trade-off between taxing rich successors from my cohort vs taxing my own children**

Example 1: $\tau=30\%$, $\alpha=30\%$, $s_{bo}=10\%$, $e_B=0$

- If $b_y=20\%$, then $\tau_B=73\%$ & $\tau_L=22\%$
- If $b_y=15\%$, then $\tau_B=67\%$ & $\tau_L=29\%$
- If $b_y=10\%$, then $\tau_B=55\%$ & $\tau_L=35\%$
- If $b_y=5\%$, then $\tau_B=18\%$ & $\tau_L=42\%$

→ with high bequest flow b_y , zero receivers want to tax inherited wealth at a higher rate than labor income (73% vs 22%); with low bequest flow they want the opposite (18% vs 42%)

Intuition: with low b_y (high g), not much to gain from taxing bequests, and this is bad for my own children

With high b_y (low g), it's the opposite: it's worth taxing bequests, so as to reduce labor taxation and allow zero receivers to leave a bequest

Example 2: $\tau=30\%$, $\alpha=30\%$, $s_{bo}=10\%$, $b_y=15\%$

- If $e_B=0$, then $\tau_B=67\%$ & $\tau_L=29\%$
- If $e_B=0.2$, then $\tau_B=56\%$ & $\tau_L=31\%$
- If $e_B=0.5$, then $\tau_B=46\%$ & $\tau_L=33\%$
- If $e_B=1$, then $\tau_B=35\%$ & $\tau_L=35\%$

→ behavioral responses matter but not hugely as long as the elasticity e_B is reasonable

Kopczuk-Slemrod 2001: $e_B=0.2$ (US)

(French experiments with zero-children savers: $e_B=0.1-0.2$)

General conclusion

- One substantial conclusion: a world with g low & $r > g$ is gloomy for workers with zero initial wealth... especially if global tax competition drives capital taxes to 0%... especially if top labor incomes take a rising share of aggregate labor income → divergence forces can be stronger than convergence forces
- One methodological conclusion: there is a lot to learn from the long run evolution of income and wealth concentration; the analysis of socially optimal tax policy must be more closely related to empirical parameters