#### **Economics of Inequality**

(Master PPD & APE, Paris School of Economics)

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Lecture 3: The dynamics of capital/income ratios: β=s/g

(Tuesday December 10<sup>th</sup> 2013) (check on line for updated versions)

### Summing up: what have we learned?

- National wealth-income ratios  $\beta_n$ = $W_n$ /Y followed a large U-shaped curve in Europe: 600-700% in 18c-19c until 1910, down to 200-300% around 1950, back to 500-600% in 2010
- U-shaped curve much less marked in the US
- Most of the long run changes in  $\beta_n$  are due to changes in the private wealth-income ratios  $\beta=W/Y$
- But changes in public wealth-income ratios  $\beta_g = W_g/Y$  (>0 or <0) also played an important role (e.g. amplified the  $\beta$  decline between 1910 and 1950)
- Changes in net foreign assets NFA (>0 or <0) also played an important role (e.g. account for a large part of the  $\beta$  decline between 1910 and 1950)

800% 700% Value of private and public capital (% national income) 600% Europe 500% 400% Private 300% capital 200% **Public** capital 100% 0% -100% 1870 1890 1910 1930 1950 1970 1990 2010

Figure 5.1. Private and public capital: Europe and America, 1870-2010

The fluctuations of national capital in the long run correspond mostly to the fluctuations of private capital (both in Europe and in the U.S.). Sources and series: see piketty.pse.ens.fr/capital21c.

800% 700% ■United States Value of national and foreign capital (% national income) 600% Europe 500% 400% National 300% capital Net foreign 200% capital 100% 0% -100% 1870 1890 1910 1930 1950 1970 1990 2010

Figure 5.2. National capital in Europe and America, 1870-2010

National capital (public and private) is worth 6,5 years of national income in Europe in 1910, vs. 4,5 years in America.

Sources and series: see piketty.pse.ens.fr/capital21c.

## The rise of wealth-income ratios in rich countries 1970-2010

- Over 1970-2010 period, the analysis can be extented to top 8 developed economies: US, Japan, Germany, France, UK, Italy, Canada, Australia
- Around 1970, β≈200-350% in all rich countries
- Around 2010, β≈400-700% in all rich countries
- Asset price bubbles (real estate and/or stock market) are important in the short-run and medium-run
- But the long-run evolution over 1970-2010 is more than a bubble: it happens in every rich country, and it is consistent with the basic theoretical model  $\beta=s/g$

800% -**∆**-U.S. ---Japan 700% Germany France -□-U.K. -Italy ---Canada ---Australia 200% 100% 1970 1975 1980 1985 1990 1995 2000 2005 2010

Figure 5.3. Private capital in rich countries, 1970-2010

Private capital is worth between 2 and 3,5 years of national income in rich countries in 1970, and between 4 and 7 years of national income in 2010. Sources and series: see piketty.pse.ens.fr/capital21c.

- The rise of β would be even larger is we were to divide private wealth W by disposable household income Y<sub>h</sub> rather than by national income Y
- Y<sub>h</sub> used to be ≈90% of Y until early 20c (=very low taxes and govt spendings); it is now ≈70-80% of Y (=rise of in-kind transfers in education and healh)
- $\beta_h$ =W/Y<sub>h</sub> is now as large as 800-900% in some countries (Italy, Japan, France...)
- But in order to make either cross-country or timeseries comparisons, it is better to use national income Y as a denominator (=more comprehensive and comparable income concept)

1000% -t-U.S. -III-Japan 900% Germany France Private capital (% disposable household income) -D-U.K. Italy 800% Canada Australia 700% 600% 500% 400% 300% 200% 1975 1980 1970 1985 1990 1995 2000 2005 2010

Figure 5.4. Private capital measured in years of disposable income

Expressed in years of household disposable income (about 70-80% of national income), the capital/income ratio appears to be larger than when it is expressed in years of national income. Sources and series : see piketty.pse.ens.fr/capital21c.

- 1970-2010: rise of private wealth-income ratio  $\beta$ , decline in public wealth-inccome ratio  $\beta_g$
- But the rise in  $\beta$  was much bigger than the decline in  $\beta_g$ , so that national wealth-income ratio  $\beta_n = \beta + \beta_g$  rose substantially
- Exemple: Italy.  $\beta$  rose from 240% to 680%,  $\beta_g$  declined from 20% to -70%, so that  $\beta_n$  rose from 260% to 610%. I.e. at most 1/4 of total increase in  $\beta$  can be attributed to a transfer from public to private wealth (privatisation and public debt).

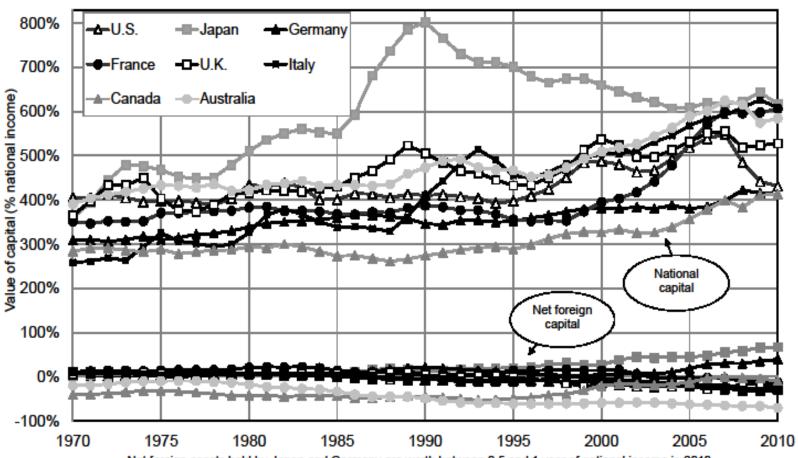
800% —U.S. -**II**-Japan 700% Germany France -□-U.K. Italy (e) 600% Agine of capital (% national income) 500% 400% 300% 200% ----Australia Canada Private capital Public capital 100% 0% -100% 1970 1975 1980 1985 1990 1995 2000 2005 2010 In Italy, private capital rose from 240% to 680% of national income between 1970 and 2010, while public capital

Figure 5.5. Private and public capital in rich countries, 1970-2010

In Italy, private capital rose from 240% to 680% of national income between 1970 and 2010, while public capital droptped from 20% to -70%. Sources and series: see piketty.pse.ens.fr/capital21c.

• In most countries, NFA  $\approx$  0, so rise in national wealth-income ratio  $\approx$  rise in domestic capital-output ratio; in Japan and Germany, a non-trivial part of the rise in  $\beta_n$  was invested abroad ( $\approx$  1/4)

Figure 5.7. National capital in rich countries, 1970-2010



Net foreign assets held by Japan and Germany are worth between 0,5 and 1 year of national income in 2010. Sources and series: see piketty.pse.ens.fr/capital21c. • Main explanation for rise in wealth-income ratio: growth slowdown and  $\beta = s/g$ 

(Harrod-Domar-Solow steady-state formula)

- One-good capital accumulation model:  $W_{t+1} = W_t + s_t Y_t$   $\rightarrow$  dividing both sides by  $Y_{t+1}$ , we get:  $\beta_{t+1} = \beta_t (1+g_{wt})/(1+g_t)$ With  $1+g_{wt} = 1+s_t/\beta_t =$  saving-induced wealth growth rate  $1+g_t = Y_{t+1}/Y_t =$  total income growth rate (productivity+population)
- If saving rate  $s_t \rightarrow s$  and growth rate  $g_t \rightarrow g$ , then:

$$\beta_t \rightarrow \beta = s/g$$

- E.g. if s=10% & g=2%, then  $\beta=500\%$ : this is the only wealth-income ratio such that with s=10%, wealth rises at 2% per year, i.e. at the same pace as income
- If s=10% and growth declines from g=3% to g=1,5%, then the steady-state wealth-income ratio goes from about 300% to 600%
- the large variations in growth rates and saving rates (g and s are determined by different factors and generally do not move together) explain the large variations in β over time and across countries

Table 5.1. Growth rates and saving rates in rich coutries, 1970-2010

	Growth rate of national income	Growth rate of per capita national income		Private saving (net of depreciation) (% national income)	
U.S.	2,8%	1,0%	1,8%	7,7%	
Japan	2,5%	0,5%	2,0%	14,6%	
Germany	2,0%	0,2%	1,8%	12,2%	
France	2,2%	0,5%	1,7%	11,1%	
U.K.	2,2%	0,3%	1,9%	7,3%	
Italy	1,9%	0,3%	1,6%	15,0%	
Canada	2,8%	1,1%	1,7%	12,1%	
Australia	3,2%	1,4%	1,7%	9,9%	

Saving rates and demographic growth vary a lot within rich countries; growth rates of per capita national income vary much less.

Sources: see piketty.pse.ens.fr/capital21c

Table 5.2. Private saving in rich countries, 1970-2010

	Private saving (net of depreciation) (% national income)	incl. Household net saving	incl. Corporate net saving (net retained earnings)
U.S.	7,7%	4,6% <b>60%</b>	3,1% <b>40%</b>
Japan	14,6%	6,8% <b>47%</b>	7,8% <b>53%</b>
Germany	12,2%	9,4% <b>77%</b>	2,8% <b>23%</b>
France	11,1%	9,0% <b>81%</b>	2,1% <b>19%</b>
U.K.	7,4%	2,8% <b>38%</b>	4,6% <b>62%</b>
Italy	15,0%	14,6% <b>97%</b>	0,4% <b>3%</b>
Canada	12,1%	7,2% <b>60%</b>	4,9% <b>40%</b>
Australia	9,9%	5,9% <b>60%</b>	3,9% <b>40%</b>

A large part (variable across countries) of private saving comes from corporate retained earnings (undistributed profits).

Sources: see piketty.pse.ens.fr/capital21c

Table 5.3. Gross and net saving in rich countries, 1970-2010

	Gross private savings (% national income)	Minus: Capital depreciation	Equal: Net private saving
U.S.	18,8%	11,1%	7,7%
Japan	33,4%	18,9%	14,6%
Germany	28,5%	16,2%	12,2%
France	22,0%	10,9%	11,1%
U.K.	19,7%	12,3%	7,3%
Italy	30,1%	15,1%	15,0%
Canada	24,5%	12,4%	12,1%
Australia	25,1%	15,2%	9,9%

A large part of gross saving (generally about half) corresponds to capital depreciation; i.e. it is used solely to repair or replace used capital.

Sources: see piketty.pse.ens.fr/capital21c

Table 5.4. Private and public saving in rich countries, 1970-2010

	National saving (private + public) (net of depreciation) (% national income)	incl. Private saving	incl. Public saving		
U.S.	5,2%	7,6%	-2,4%		
Japan	14,6%	14,5%	0,1%		
Germany	10,2%	12,2%	-2,0%		
France	9,2%	11,1%	-1,9%		
U.K.	5,3%	7,3%	-2,0%		
Italy	8,5%	15,0%	-6,5%		
Canada	10,1%	12,1%	-2,0%		
Australia	8,9%	9,8%	-0,9%		

A large part (variable across countries) of private saving is absorved by public deficits, so that national saving (private + public) is less than private saving.

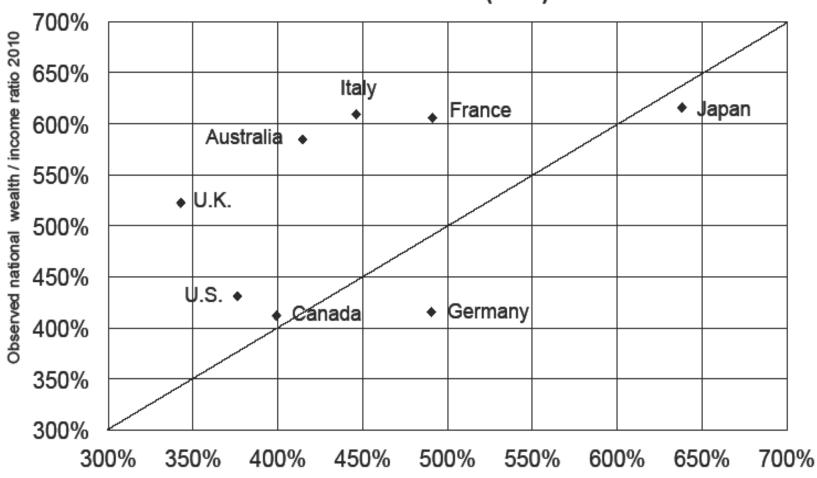
Sources: voir piketty.pse.ens.fr/capital21c

- Two-good capital accumulation model: one capital good, one consumption good
- Define 1+q<sub>t</sub> = real rate of capital gain (or capital loss)
- = excess of asset price inflation over consumer price inflation • Then  $\beta_{t+1} = \beta_t (1+g_{wt})(1+q_t)/(1+g_t)$
- With  $1+g_{wt} = 1+s_t/\beta_t = \text{saving-induced wealth growth rate}$  $1+q_t = \text{capital-gains-induced wealth growth rate}$  (=residual term)
- → Main finding: relative price effects (capital gains and losses) are key in the short and medium run and at local level, but volume effects (saving and investment) dominate in the long run and at the national or continental level

See the detailed decomposition results for wealth accumulation into volume and relative price effects in Piketty-Zucman, "Capital is Back: Wealth-Income Ratios in Rich Countries 1700-2010", 2013, slides, data appendix

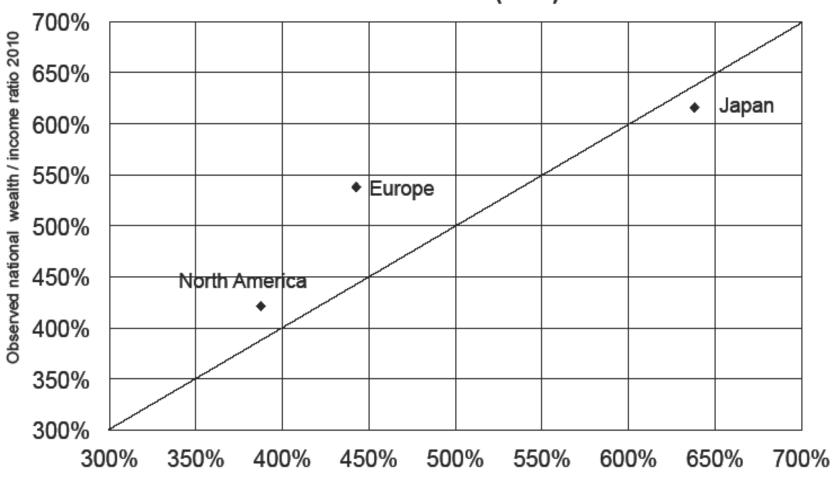
(see also Gyourko et al, « Superstar cities », AEJ 2013)

Figure 7a: Observed vs. predicted national wealth / national income ratios (2010)



Predicted national wealth / income ratio 2010 (on the basis of 1970 initial wealth and 1970-2010 cumulated saving flows) (additive decomposition, incl. R&D)

Figure 7b: Observed vs. predicted national wealth / national income ratios (2010)



Predicted national wealth / income ratio 2010 (on the basis of 1970 initial wealth and 1970-2010 cumulated saving flows) (additive decomposition, incl. R&D)

Table 10: Accumulation of national wealth in rich countries, 1910-1950

1						
	National wealth- national income ratios		Decomposition of 1950 national wealth-national income ratio			
			Initial wealth	Cumulated	Cumulated war	Capital gains
	β (1910)	β (1950)	effect	new savings	destructions	or losses
U.S.	469%	380%	132%	193%	0%	55%
Germany	637%	223%	400%	109% 31%	-120% <b>29%</b>	-165% <b>40%</b>
France	747%	261%	421%	144% 38%	-132% <b>27%</b>	-172% 35%
U.K.	719%	208%	409%	75% 46%	-19% <b>4</b> %	-256% <b>50%</b>

Germany's national wealth-income ratio fell from 637% to 223% between 1910 and 1950. 31% of the fall can be attributed to insufficient saving, 29% to war destructions, and 40% to real capital losses.

- Harrod-Domar-Solow formula  $\beta = s/g$  is a pure accounting formula and is valid with any saving motive and utility function
- Wealth increase in the utility function: Max  $U(c_t, \Delta w_t = w_{t+1} w_t)$
- $\rightarrow$  if  $U(c,\Delta)=c^{1-s}\Delta^s$ , then fixed saving rate  $s_t=s$ ,  $\beta_t \rightarrow \beta=s/g$  (i.e. Max  $U(c_t,\Delta w_t)$  under  $c_t+\Delta w_t \le y_t \rightarrow \Delta w_t=s y_t$ )
- Total wealth or bequest in the utility function: Max  $U(c_t, w_{t+1})$
- $\rightarrow$  if U(c,w)=c<sup>1-s</sup> w<sup>s</sup>, then w<sub>t+1</sub>=s(w<sub>t</sub> + y<sub>t</sub>),  $\beta_t \rightarrow \beta$  = s/(g+1-s) = s'/g (with s'=s(1+ $\beta$ )- $\beta$  = corresponding saving rate out of income)
- Pure OLG lifecycle model: saving rate s determined by demographic structure (more time in retirement  $\rightarrow$  higher s), then  $\beta_t \rightarrow \beta = s/g$
- Dynastic utility:

Max Σ U(c<sub>t</sub>)/(1+δ)<sup>t</sup>, with U(c)= $c^{1-1/\xi}/(1-1/\xi)$ 

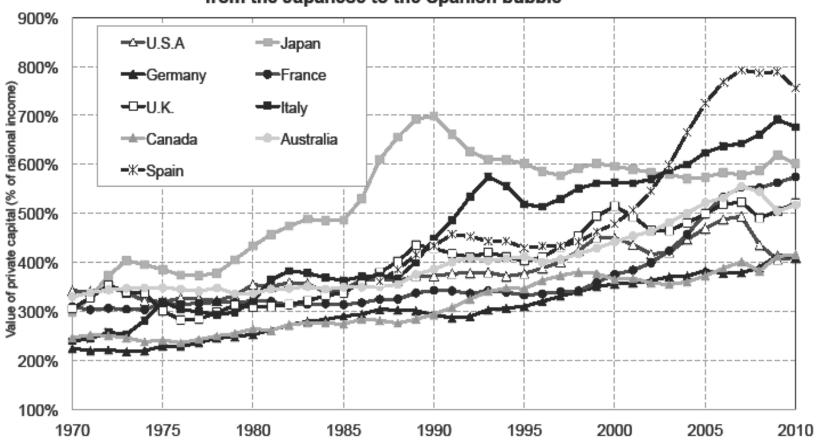
- $\rightarrow$  unique long rate rate of return  $r_{t} \rightarrow r = \delta + \xi g > g$
- $\rightarrow$  long run saving rate  $s_t \rightarrow s = \alpha g/r$ ,  $\beta_t \rightarrow \beta = \alpha/r = s/g$

(on these models, see next lecture and PZ 2013 section 3)

# Gross vs net foreign assets: financial globalization in action

- Net foreign asset positions are smaller today than what they were in 1900-1910
- But they are rising fast in Germany, Japan and oil countries
- And gross foreign assets and liabilities are a lot larger than they have ever been, especially in small countries: about 30-40% of total financial assets and liabilities in European countries (even more in smaller countries)
- This potentially creates substantial financial fragility (especially if link between private risk and sovereign risk)
- This destabilizing force is probably even more important than the rise of top income shares (=important in the US, but not so much in Europe; see lecture 5 & PS, « Top incomes and the Great Recession », IMF Review 2013)

Figure S5.2. Private capital in rich countries: from the Japanese to the Spanish bubble



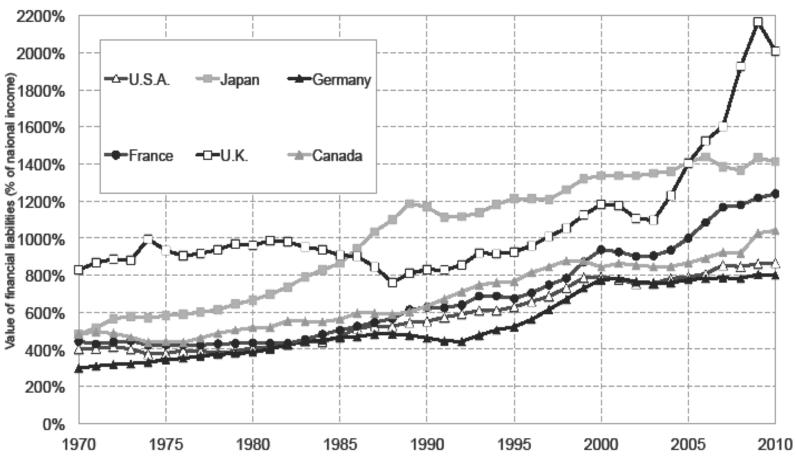
Private capital almost reached 8 years of national income in Spain at the end of the 2000s (ie. one more year than Japan in 1990). Sources et series: see piketty.pse.ens.fr/capital21c.

2200% 2000% ---U.S.A Germany (emula 1800%) 1600% of unational income of a seets (%) 1200% 1200% 1200% 800% 600% 400% Japan ---France -D-U.K. Canada 200% 0% 1970 1975 1980 1985 1990 1995 2000 2005 2010

Figure S5.3. Financial assets in rich countries

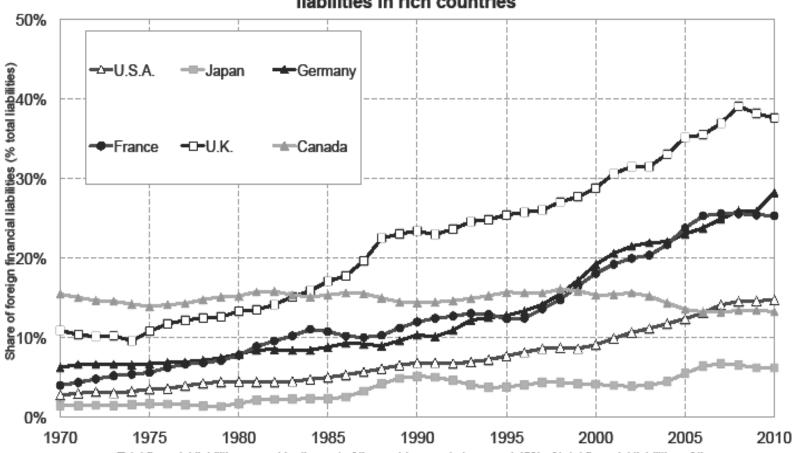
Total financial assets owned by the domestic sector (firms, households, administration) reached 20 years of national income in 2010 in the U.K.. Sources et series: voir piketty.pse.ens.fr/capital21c.

Figure S5.4. Financial liabilities in rich countries



Total of financial liabilities owned by the domestic sector (firms, households, administration) reached 20 years of national income in 2010 in the U.K. Sources et series: voir piketty.pse.ens.fr/capital21c.

Figure S5.5. Share of foreign financial liabilities in the total financial liabilities in rich countries



Total financial liabilities owned by the rest of the world amounts to around 40% of total financial liabilities of the domestic sector in the U.K. in 2010. Sources et series: see piketty.pse.ens.fr/capital21c.

140% 120% Foreign assets Foreign assets and liabilities (% national income) 80% 60% 40% 0% 0% →Foreign liabilities Net position -20% -40% 1970 1975 2005 1980 1985 1990 1995 2000 2010

Figure S5.6. Foreign assets and liabilities in the U.S.A. 1970-2010

Foreign liabilities (what the rest of the world owns in the US) has outweighted foreign liabilities (what the US own in the rest of the world) since 1985-1986. Sources et series: see piketty.pse.ens.fr/capital/21c.

180% 160% Foreign assets (emanul land) septemblishes (% 140%) 120% 100% 80% 60% 40% 20% 0% →Foreign liabilities Net position 0% -20%

Figure S5.7. Foreign assets and liabilities in Japan 1970-2010

Foreign assets (what Japan owns in the rest of the world) are almost twice bigger than foreign liabilities (what the rest of the world owns in Japan) in 2010. Sources et series: see piketty.pse.ens.fr/capital21c.

1990

1995

2000

2005

2010

-40%

1970

1975

1980

1985

280% 240% 200% 200% 160% 120% 80% 40% Foreign assets →Foreign liabilities Net position 0% -40% 1970 1975 1980 1990 2000 2005 2010 1985 1995

Figure S5.8. Foreign assets and liabilities in Germany, 1970-2010

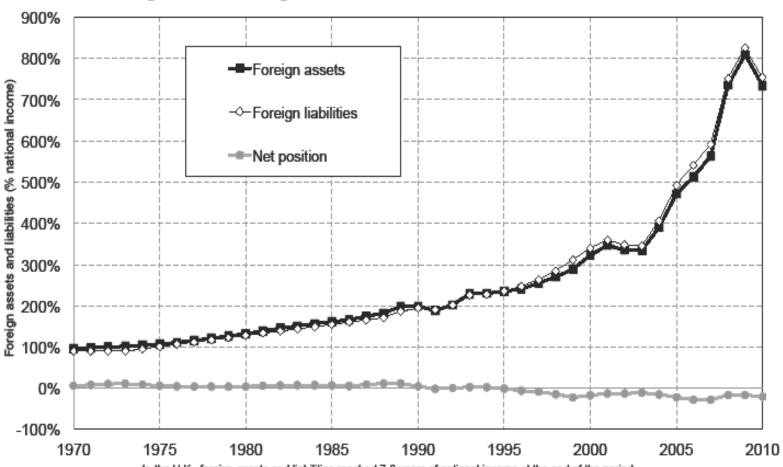
Foreign assets and liabilities in Germany have risen a lot since the 1980s-1990s. Sources et series: see piketty.pse.ens.fr/capital21c.

320% 280% -Foreign assets (eucoid assets and liabilities (% national income) 200% 160% 120% 80% 40% → Foreign liabilities Net position 0% -40% 1970 1975 1980 1985 1995 2000 2005 2010 1990

Figure S5.9. Foreign assets and liabilities in France, 1970-2010

Like in Germany, foreign assets and liabilities have risen a lot since 1980s-1990s (but with a negative net position at the end of the period. Sources et series: see piketty.pse.ens.fr/capital21c.

Figure S5.10. Foreign assets and liabilities in the U.K. 1970-2010



In the U.K., foreign assets and liabilities reached 7-8 years of national income at the end of the period Sources et series: see piketty.pse.ens.fr/capital21c.

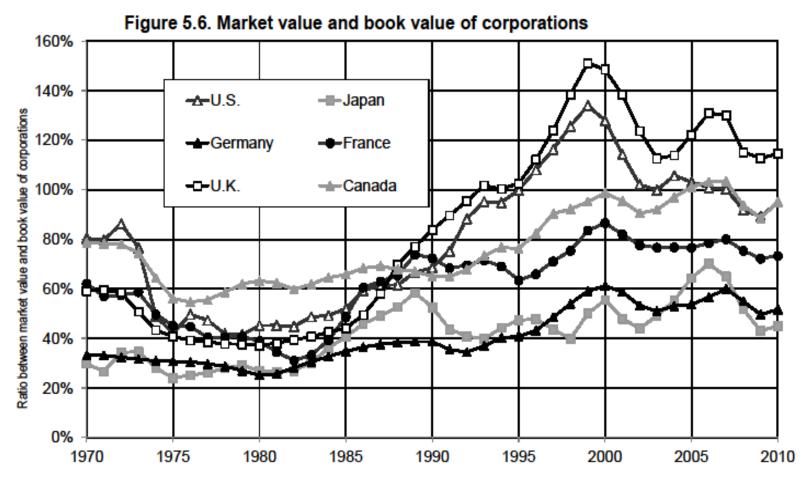
280% 240% ---Foreign assets Foreign assets and liabilities (% national income) 200% →Foreign liabilities 160% Net position 120% 80% 40% 0% -40% -80% -120% 1980 1985 1990 1995 2000 2005 2010

Figure S5.11. Foreign assets and liabilities in Spain, 1980-2010

Net foreign debt of Spain exceeds a year of national income in 2010. Sources et series: see piketty.pse.ens.fr/capital21c.

### Market vs book value of corporations

- So far we used a market-value definition of national wealth W<sub>n</sub>: corporations valued at stock market prices
- Book value of corporations = assets debt
- Tobin's Q ratio = (market value)/(book value) (>1 or <1)</li>
- Residual corporate wealth W<sub>c</sub> = book value market value
- Book-value national wealth W<sub>b</sub> = W<sub>n</sub> + W<sub>c</sub>
- In principe, Q ≈ 1 (otherwise, investment should adjust), so that W<sub>c</sub> ≈ 0 and W<sub>b</sub> ≈ W<sub>n</sub>
- But Q can be systematically >1 if immaterial investment not well accounted in book assets
- But Q can be systemativally <1 if shareholders have imperfect control of the firm (stakeholder model): this can explain why Q lower in Germany than in US-UK, and the general rise of Q since 1970s-80s
- From an efficiency viewpoint, unclear which model is best



Tobin's Q (i.e. the ratio between market vaue and book value of corporations) has risen in rich countries since the 1970s-1980s. Sources and series: see piketty.pse.ens.fr/capital21c.

### Summing up

- Wealth-income ratios  $\beta$  and  $\beta_n$  have no reason to be stable over time and across countries
- If global growth slowdown in the future (g≈1,5%) and saving rates remain high (s≈10-12%), then the global β might rise towards 700% (or more... or less...)
- What are the consequences for the share  $\alpha$  of capital income in national income? See next lecture

800% Projections 700% (central Value of private capital (% national income) 000% 000% 000% 000% 000% scenario) Observed series 200% 100% 1870 1890 1910 1930 1950 1970 1990 2010 2030 2050 2070 2090

Figure 5.8. The world capital/income ratio, 1870-2100

According to simulations (central scenario), the world capital/income ratio could be near to 700% by the end of the 21st century. Sources and series: see piketty.pse.ens.fr/capital21c.